

GENERATIVE ADVERSARIAL NETWORKS - PART I

11785- Introduction to Deep Learning

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Slides Inspired by Benjamin Striner

“This (GANs), and the variations that are now being proposed is the most interesting idea in the last 10 years in ML, in my opinion”

—Yann LeCun

Video: <https://www.youtube.com/watch?v=QiiSAvKJIHo>

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- Motivation
- Generative vs Discriminative Models
- GANs vs VAEs
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ORIGINAL PAPER (GANs, 2014)

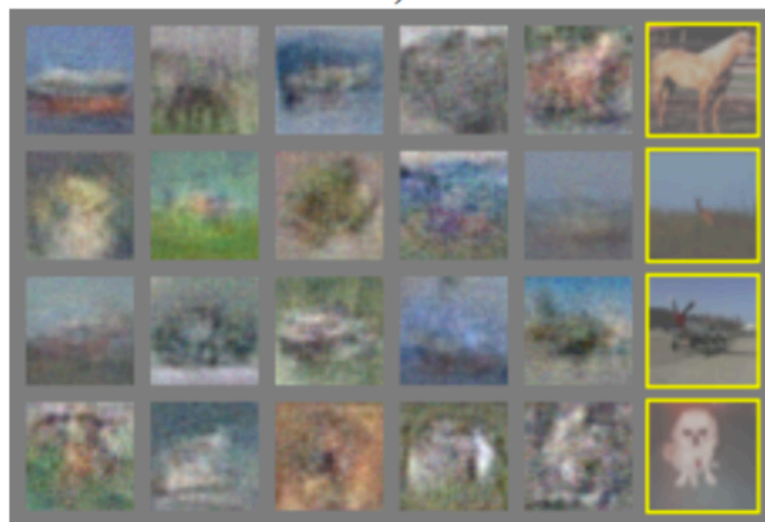
Output of original GAN paper, 2014 [GPM⁺14]



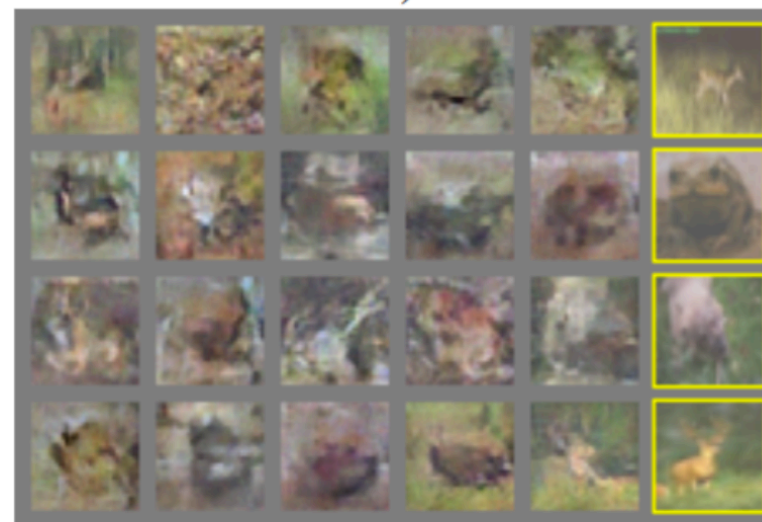
a)



b)



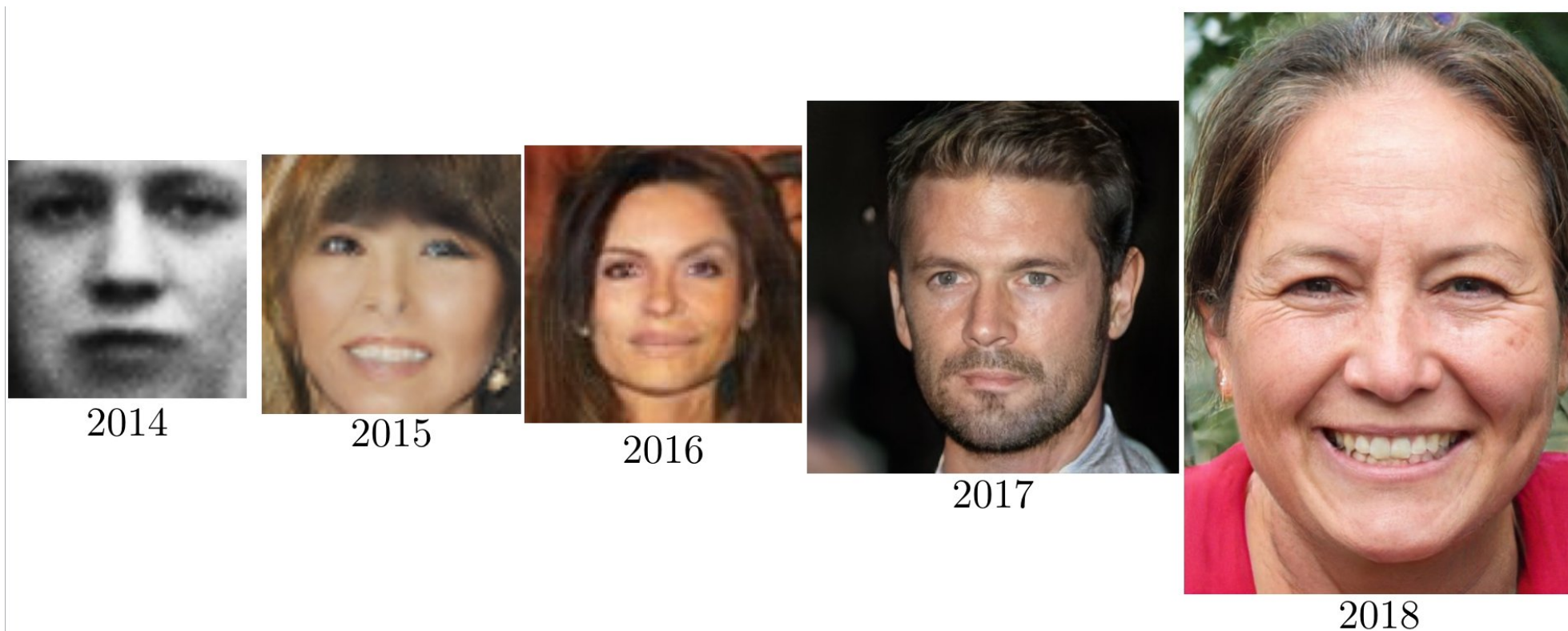
c)



d)

GANs PROGRESSION

- Better quality
- High Resolution



https://twitter.com/goodfellow_ian/status/1084973596236144640?lang=en

STARGAN(2018)

Manipulating Celebrity Faces [CCK⁺17]

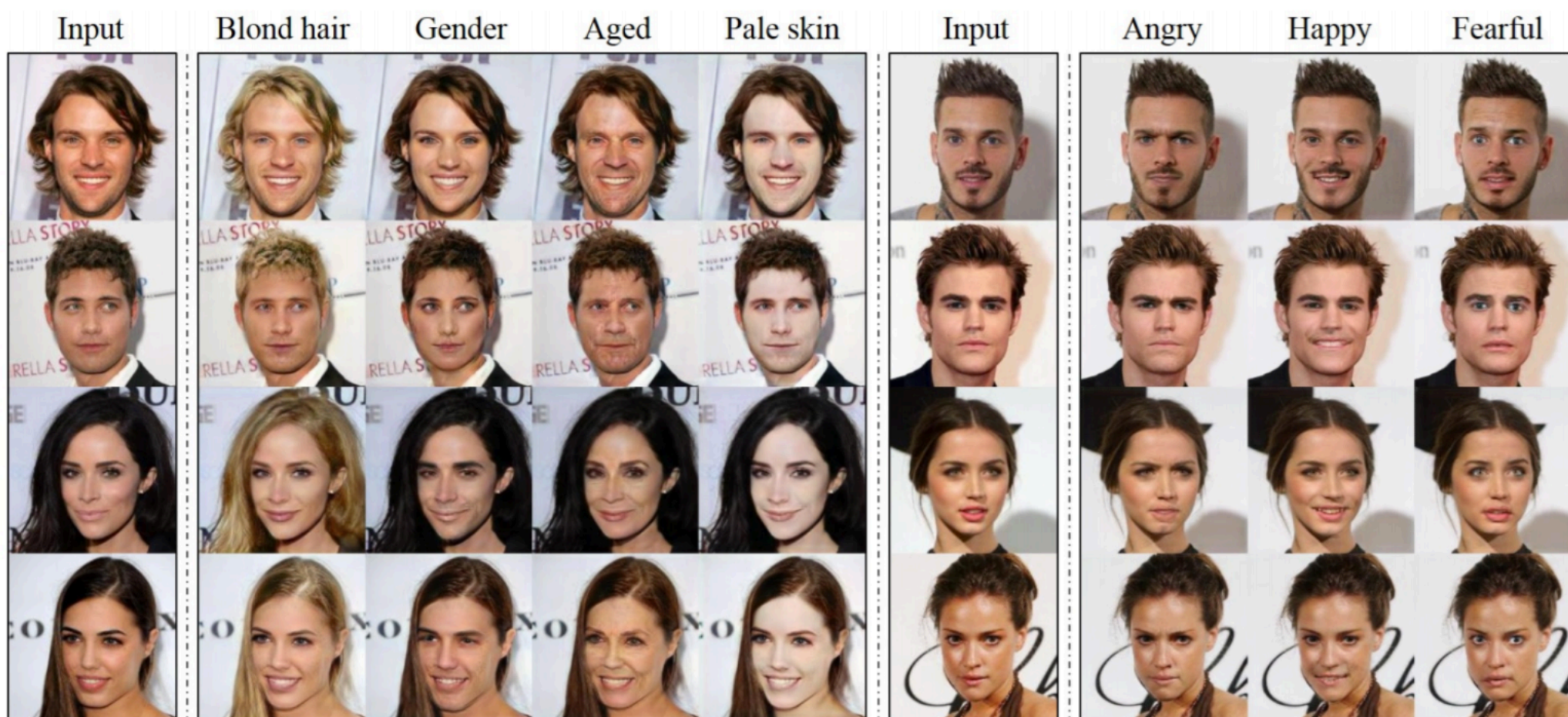


Figure 1. Multi-domain image-to-image translation results on the CelebA dataset via transferring knowledge learned from the RaFD dataset. The first and sixth columns show input images while the remaining columns are images generated by StarGAN. Note that the images are generated by a single generator network, and facial expression labels such as angry, happy, and fearful are from RaFD, not CelebA.

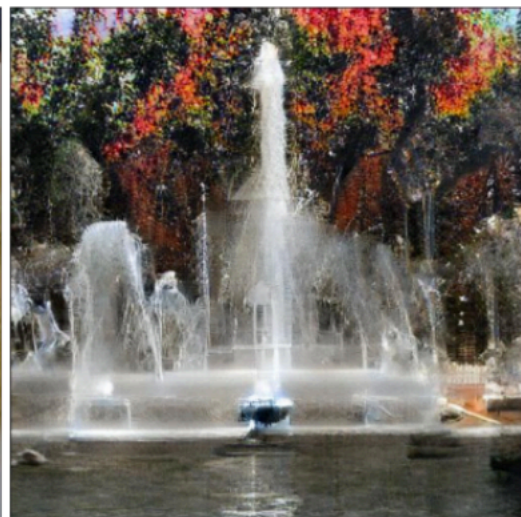
PROGRESSIVE GROWING OF GANS (2018)



Figure 5: 1024×1024 images generated using the CELEBA-HQ dataset. See Appendix F for a larger set of results, and the accompanying video for latent space interpolations.

HIGH FIDELITY NATURAL IMAGES (2019)

Generating High-Quality Images [BDS18]



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DISCRIMINATIVE vs GENERATIVE MODELS

Given a distribution of inputs X and labels Y .

DISCRIMINATIVE MODELS

- Discriminative models learn conditional distribution $P(Y | X)$

GENERATIVE MODELS

- Generative models learn the joint distribution $P(Y, X)$

DISCRIMINATIVE vs GENERATIVE MODELS

Given a distribution of inputs X and labels Y .

DISCRIMINATIVE MODELS

- Discriminative models learn conditional distribution $P(Y | X)$
- Learns decision boundary between classes.
- Limited scope. Can only be used for classification tasks.

GENERATIVE MODELS

- Generative models learn the joint distribution $P(Y, X)$
- Learns actual probability distribution of data.
- Can do both generative and discriminative tasks.

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GENERATIVE MODELS

- Generative models learn the joint distribution $P(Y, X)$
- Learns actual probability distribution of data.
- Can do both generative and discriminative tasks. distribution $P(Y, X)$
- Harder problem. Requires a deeper understanding of the distribution than discriminative models.

EXPLICIT VS IMPLICIT DISTRIBUTION MODELLING

EXPLICIT DISTRIBUTION MODELS

- Calculates $P(x \sim X)$ for all x

IMPLICIT DISTRIBUTION MODELS

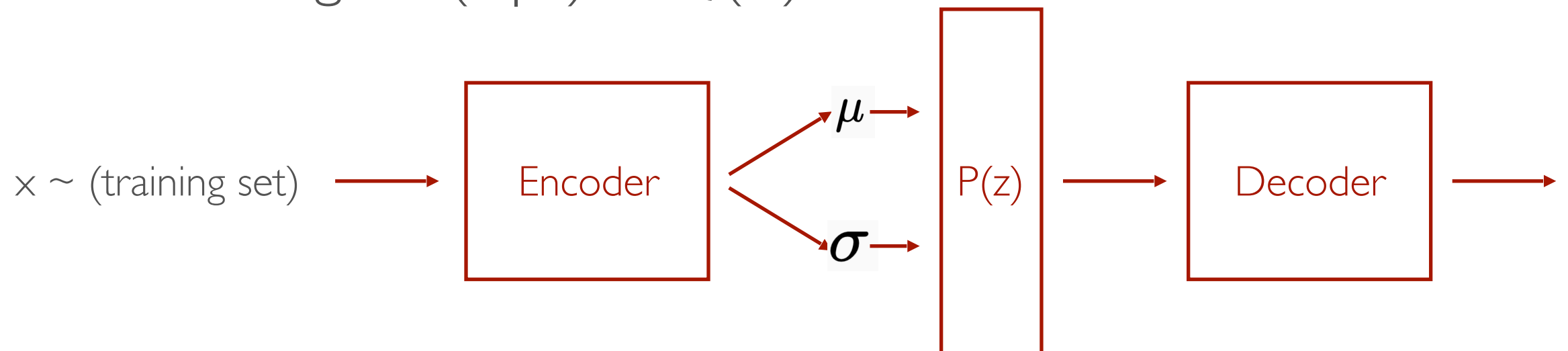
- Generate $x \sim X$

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VARIATIONAL AUTOENCODERS (VAE)

- Encoder models $P(Z|X)$
- Decoder models $P(X|Z)$
- Loss encourages $P(Z|X) \sim Q(Z)$



VAEs vs GANs

VAEs

- Minimizing the KL-divergence
- Minimize a bound on the divergence between generated distribution and target distribution
- Simpler optimization. Trains faster and more reliably
- Results are blurry

GANs

- Minimizing the Jensen-Shannon Divergence
- Minimize divergence between generated distribution and target distribution
- Noisy and difficult optimization
- Sharper results

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WHAT ARE GANS?

Generative Adversarial Networks

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Generative Adversarial Networks

Generative Models

We try to learn the underlying the distribution
from which our dataset comes from.

Eg: Variational AutoEncoders (VAE)

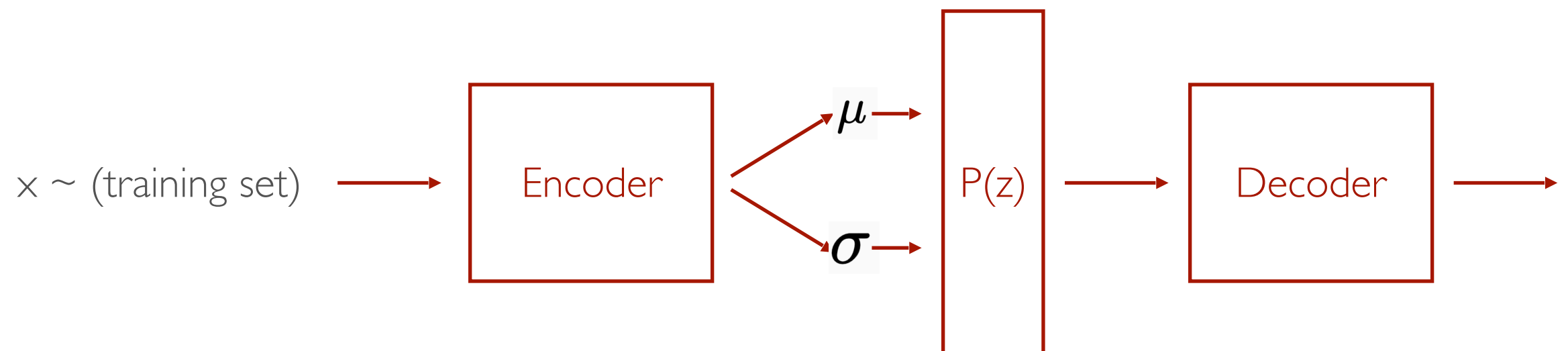
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Adversarial Training

GANS are made up of two competing networks (adversaries) that are trying beat each other.

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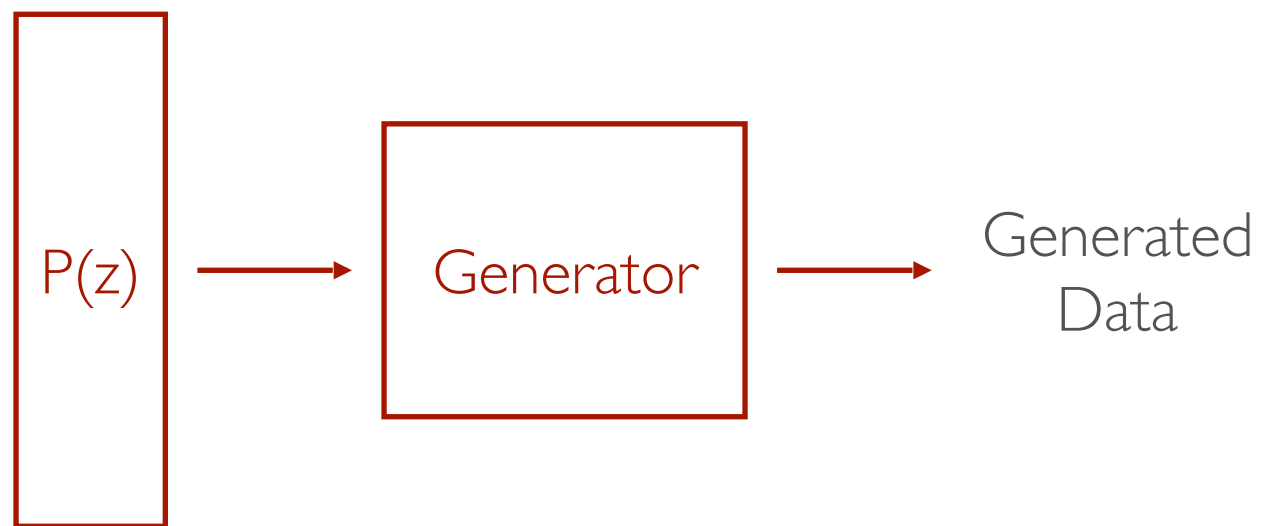
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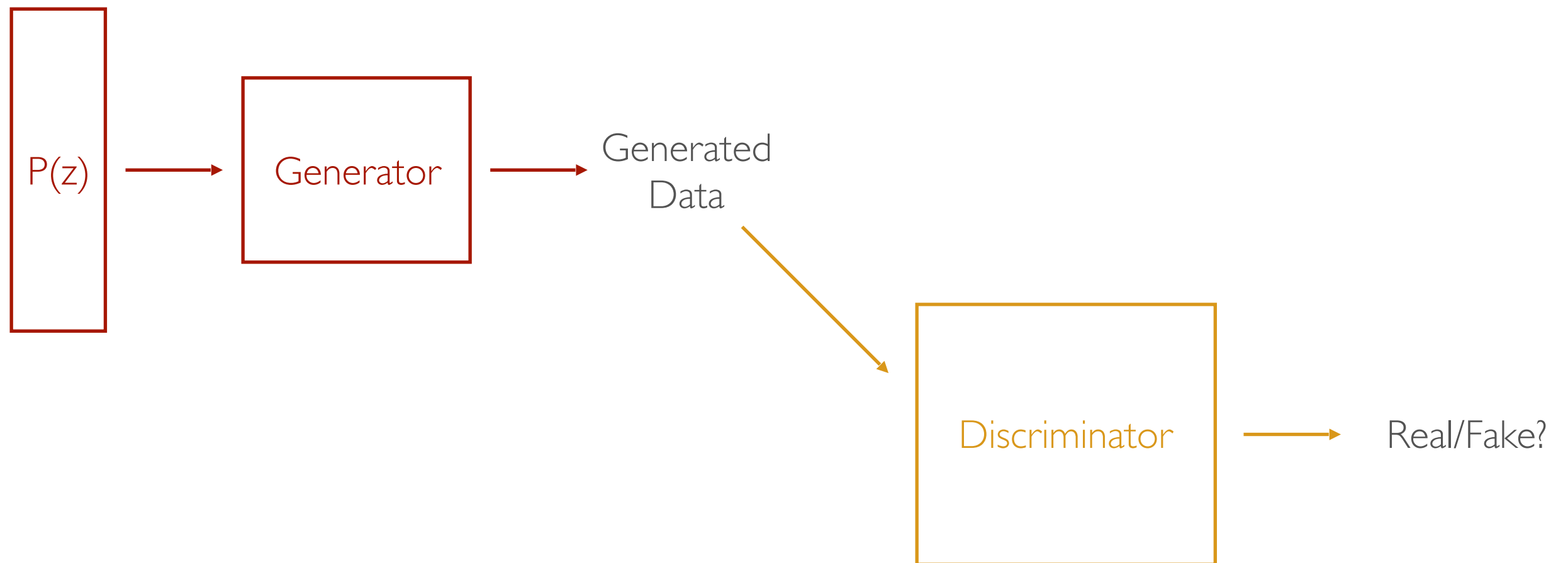
Neural Networks

GOAL: Generate data from an unlabelled distribution.

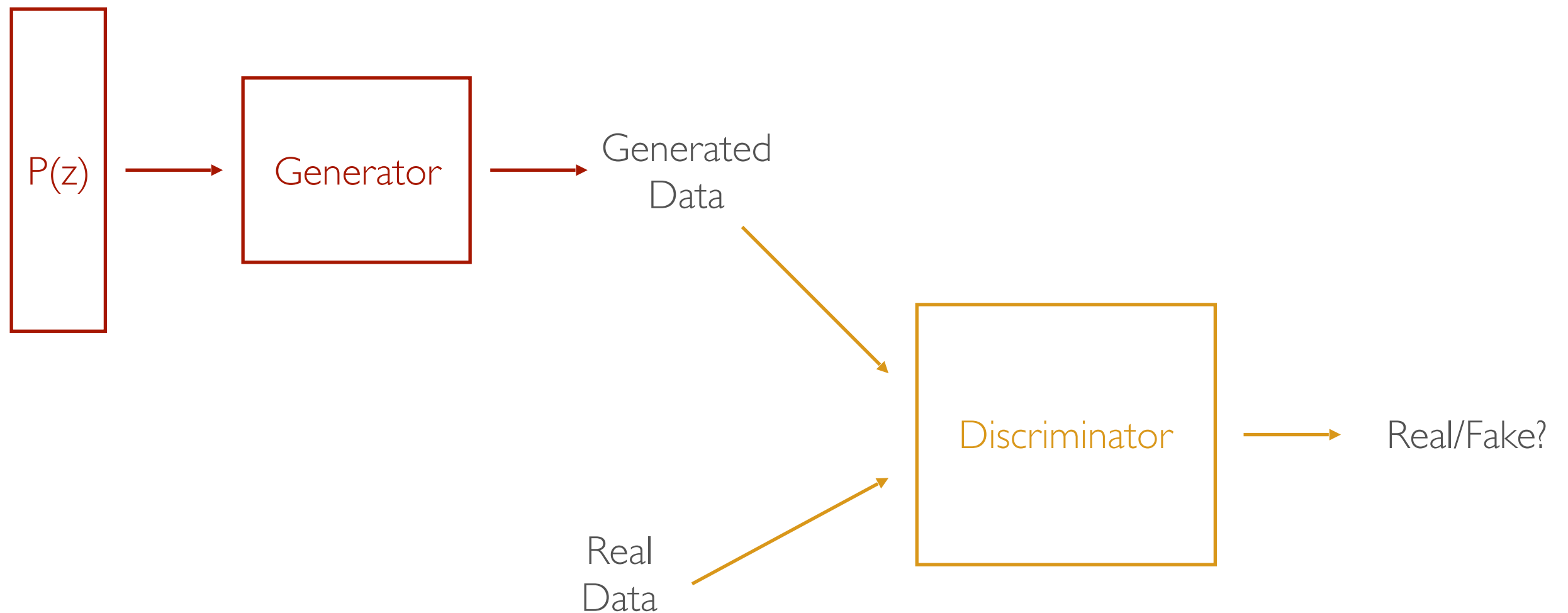
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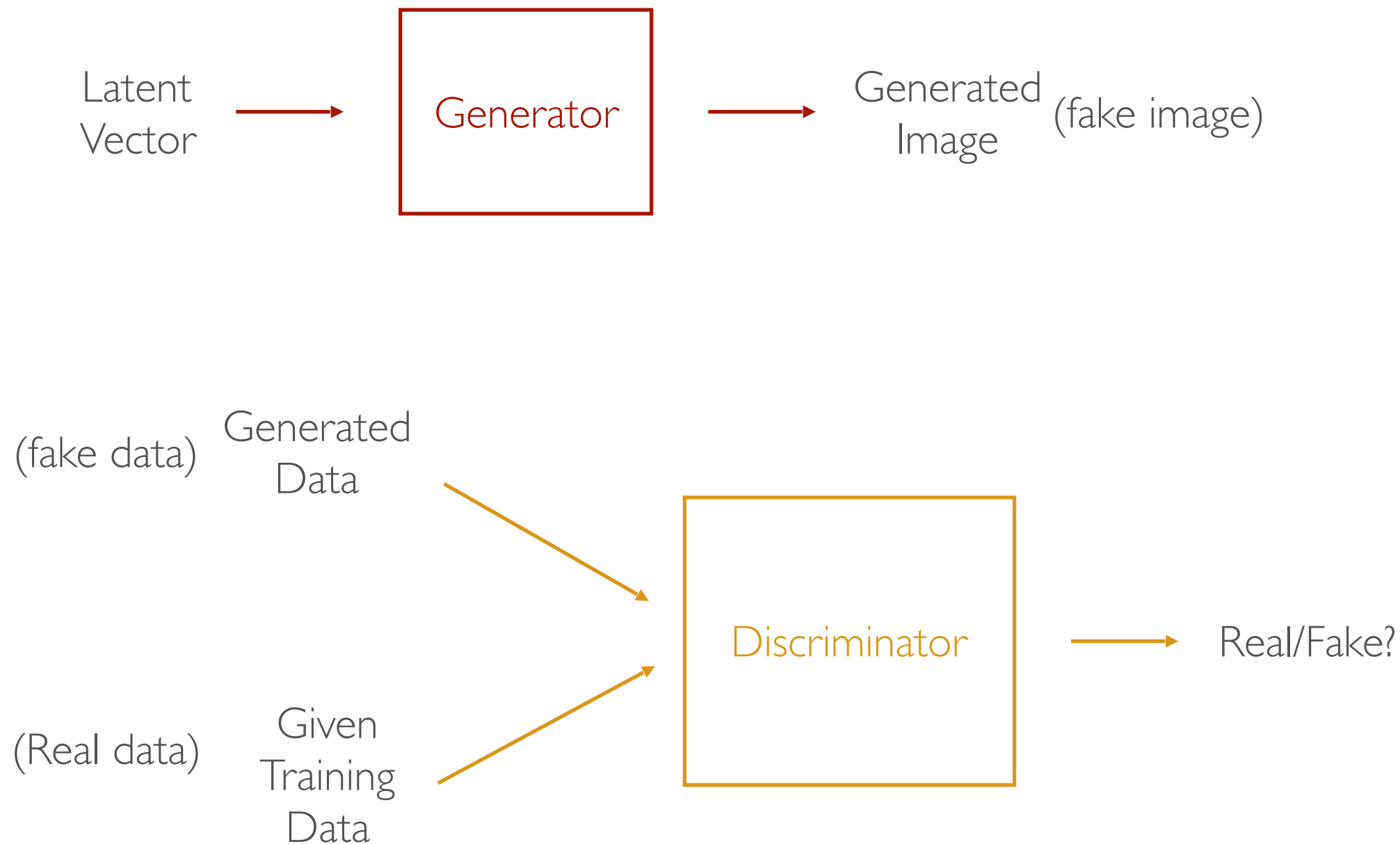
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HOW TO TRAIN A GAN?

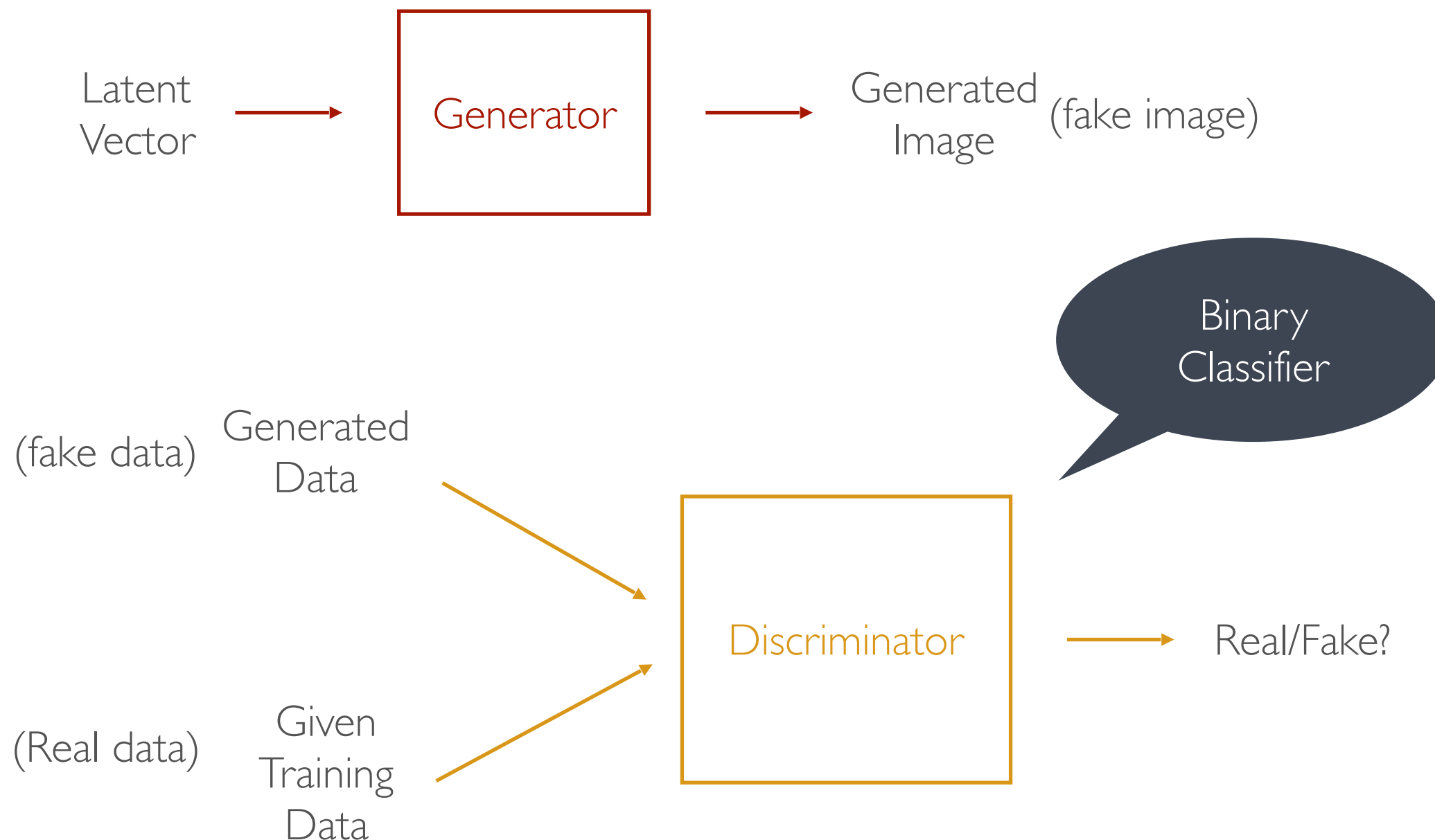
HOW TO TRAIN A GAN?

At $t = 0$,



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HOW TO TRAIN A GAN?

Which network should I train first?

HOW TO TRAIN A GAN?

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Discriminator!

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But with what training data?

HOW TO TRAIN A GAN?

Which network should I train first?

Discriminator!

But with what training data?

The Discriminator is a Binary classifier.

The Discriminator has two class - Real and Fake.

The data for Real class is already given: THE TRAINING DATASET

The data for Fake class? -> generate from the Generator

HOW TO TRAIN A GAN?

What's next? -> Train the Generator

But how? What's our training objective?

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But how? What's our training objective?

**Generate images from the Generator
such that they are classified incorrectly by the Discriminator!**

HOW TO TRAIN A GAN?



Step 1:
Train the Discriminator
using the current ability
of the Generator.

HOW TO TRAIN A GAN?



Discriminator

Step 1:

Train the Discriminator
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Generator

Step 2:

Train the Generator
to beat
the Discriminator.

HOW TO TRAIN A GAN?



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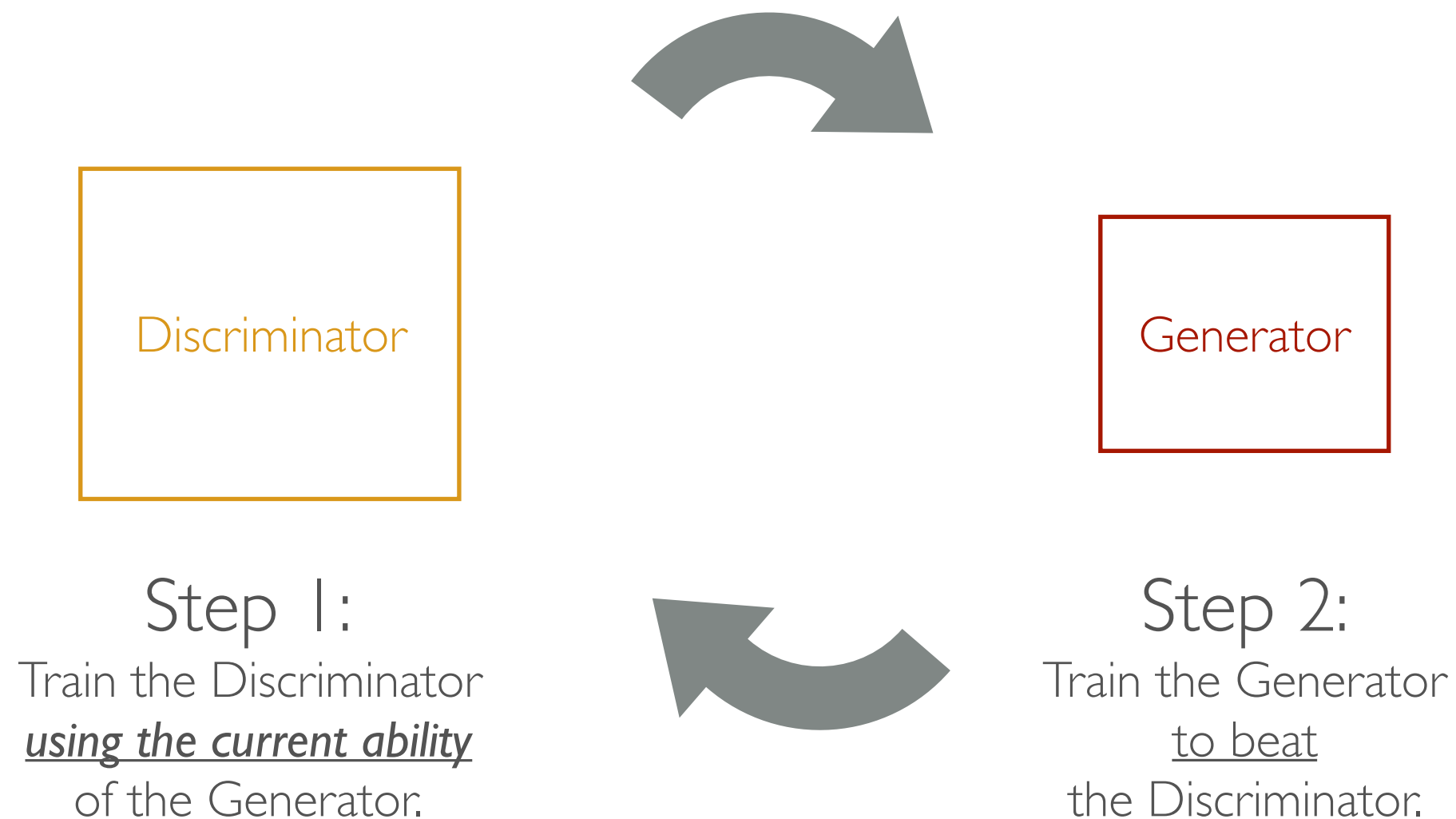


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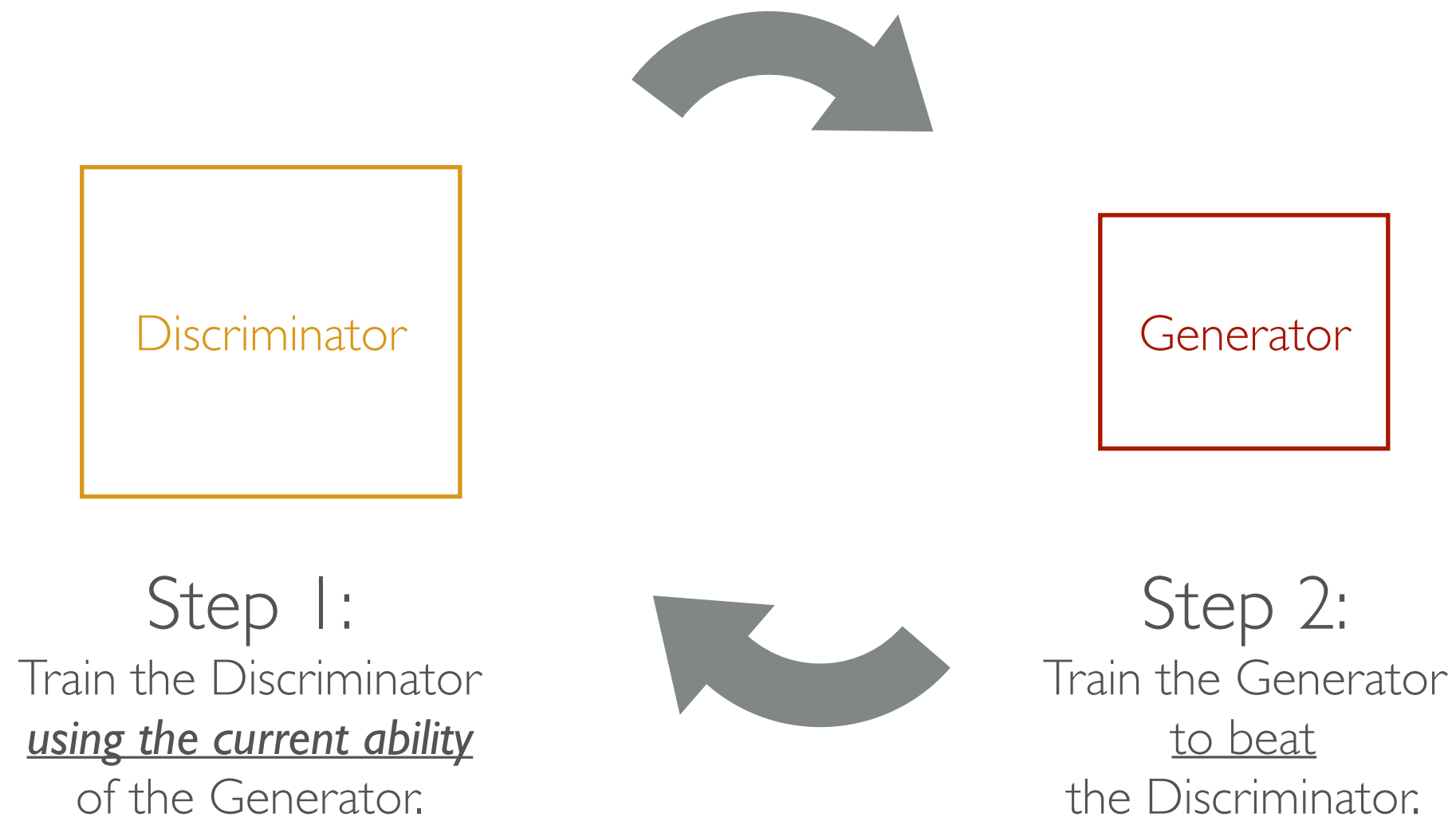
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GENERATIVE ADVERSARIAL NETWORKS

- Introduced in 2014
- Goal is to model $P(X)$, the distribution of training data
- Model can generate samples from $P(X)$
- Trained using a pair of “adversaries”

THE GENERATOR

- The generator learns $P(X|Z)$: Produces realistic looking data X from a latent vector Z
- Z is sampled from a known prior, such as a Gaussian
- Maps a simple known distribution to a complicated data distribution
- GOAL : Generated distribution, $G(z)$, matches the true data distribution $P(X)$

THE DISCRIMINATOR

- Trained to tell the difference between real and generated (fake) data
- Backpropagates its expectations to the generator
- “Thrown away” after generator is trained

ORIGINAL GAN FORMULATION

The original GAN formulation is the following min-max game

$$\min_G \max_D V(D, G) = \mathbb{E}_X \log D(X) + \mathbb{E}_Z \log(1 - D(G(Z)))$$

- D wants $D(X) = 1$ and $D(G(Z)) = 0$
- G wants $D(G(Z)) = 1$

THE OPTIMAL DISCRIMINATOR

P_D = actual data distribution

P_G = generated data distribution

$D(X)$ = discriminator output

Objective: $\min_G \max_D V(D, G) = \mathbb{E}_X \log D(X) + \mathbb{E}_Z \log(1 - D(G(Z)))$

What is the optimal discriminator?

$$f := \mathbb{E}_{X \sim P_D} \log D(X) + \mathbb{E}_{X \sim P_G} \log(1 - D(X))$$

$$= \int_X [P_D(X) \log D(X) + P_G(X) \log(1 - D(X))] dX$$

$$\frac{\partial f}{\partial D(X)} = \frac{P_D(X)}{D(X)} - \frac{P_G(X)}{1 - D(X)} = 0$$

$$\frac{P_D(X)}{D(X)} = \frac{P_G(X)}{1 - D(X)}$$

$$(1 - D(X))P_D(X) = D(X)P_G(X)$$

$$D(X) = \frac{P_D(X)}{P_G(X) + P_D(X)}$$

THE OPTIMAL DISCRIMINATOR

P_D = actual data distribution

P_G = generated data distribution

$D(X)$ = discriminator output

$$D(X) = \frac{P_D(X)}{P_G(X) + P_D(X)}$$

CASE - I : BAD GENERATOR

“There’s no way the input $X = G(z)$ looks like my data”

THE OPTIMAL DISCRIMINATOR

P_D = actual data distribution

P_G = generated data distribution

$D(X)$ = discriminator output

$$D(X) = \frac{P_D(X)}{P_G(X) + P_D(X)}$$

CASE - I : BAD GENERATOR

“There’s no way the input $X = G(z)$ looks like my data”

$$P_D(X) = 0, P_G(X) = 1$$

$$D(X) = 0$$

THE OPTIMAL DISCRIMINATOR

P_D = actual data distribution

P_G = generated data distribution

$D(X)$ = discriminator output

$$D(X) = \frac{P_D(X)}{P_G(X) + P_D(X)}$$

CASE -II : GOOD GENERATOR

“I cannot tell the difference between $X = G(z)$ and my data”

THE OPTIMAL DISCRIMINATOR

P_D = actual data distribution

P_G = generated data distribution

$D(X)$ = discriminator output

$$D(X) = \frac{P_D(X)}{P_G(X) + P_D(X)}$$

CASE -II : GOOD GENERATOR

“I cannot tell the difference between $X = G(z)$ and my data”

$$P_D(X) = 1, P_G(X) = 1$$
$$D(X) = 0.5$$

THE OPTIMAL GENERATOR

P_D = actual data distribution

$D(X)$ = discriminator output

P_G = generated data distribution

$G(Z)$ = generator output

Objective: $\min_G \max_D V(D, G) = \mathbb{E}_X \log D(X) + \mathbb{E}_Z \log(1 - D(G(Z)))$

$$\begin{aligned} f &:= \mathbb{E}_{X \sim P_D} \log D(X) + \mathbb{E}_{X \sim P_G} \log(1 - D(X)) \\ &= \mathbb{E}_{P_D} \log \frac{P_D(X)}{P_D(X) + P_G(X)} + \mathbb{E}_{P_G} \log \frac{P_G(X)}{P_D(X) + P_G(X)} \\ &= \text{JSD}(P_D|P_G) - \log 4 \end{aligned}$$

THE OPTIMAL GENERATOR

P_D = actual data distribution

$D(X)$ = discriminator output

P_G = generated data distribution

$G(Z)$ = generator output

Objective: $\min_G \max_D V(D, G) = \mathbb{E}_X \log D(X) + \mathbb{E}_Z \log(1 - D(G(Z)))$

Generator wants to minimize this!

$$\begin{aligned} f &:= \mathbb{E}_{X \sim P_D} \log D(X) + \mathbb{E}_{X \sim P_G} \log(1 - D(X)) \\ &= \mathbb{E}_{P_D} \log \frac{P_D(X)}{P_G(X) + P_D(X)} + \mathbb{E}_{P_G} \log \frac{P_G(X)}{P_G(X) + P_D(X)} \\ &= JSD(P_D | P_G) - \log 4 \end{aligned}$$

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Jensen-Shannon Divergence

$$\begin{aligned} m(X) &= \frac{P_D + P_G}{2} \\ \text{JS}(P_D \| P_G) &= \frac{1}{2} \text{KL}(P_D \| m) + \frac{1}{2} \text{KL}(P_G \| m) \end{aligned}$$

THE OPTIMAL GENERATOR

What is the optimal generator?

$$\min_G JSD(P_D \| P_G) - \log 4$$

Minimize the Jensen-Shannon divergence between the real and generated distributions (make the distributions similar)

MIN-MAX STATIONARY POINT

- There exists a stationary point:
 - If the generated data exactly matches the real data, the discriminator outputs 0.5 for all inputs
 - If discriminator outputs 0.5, the gradients for the generator is flat, so generator does not learn

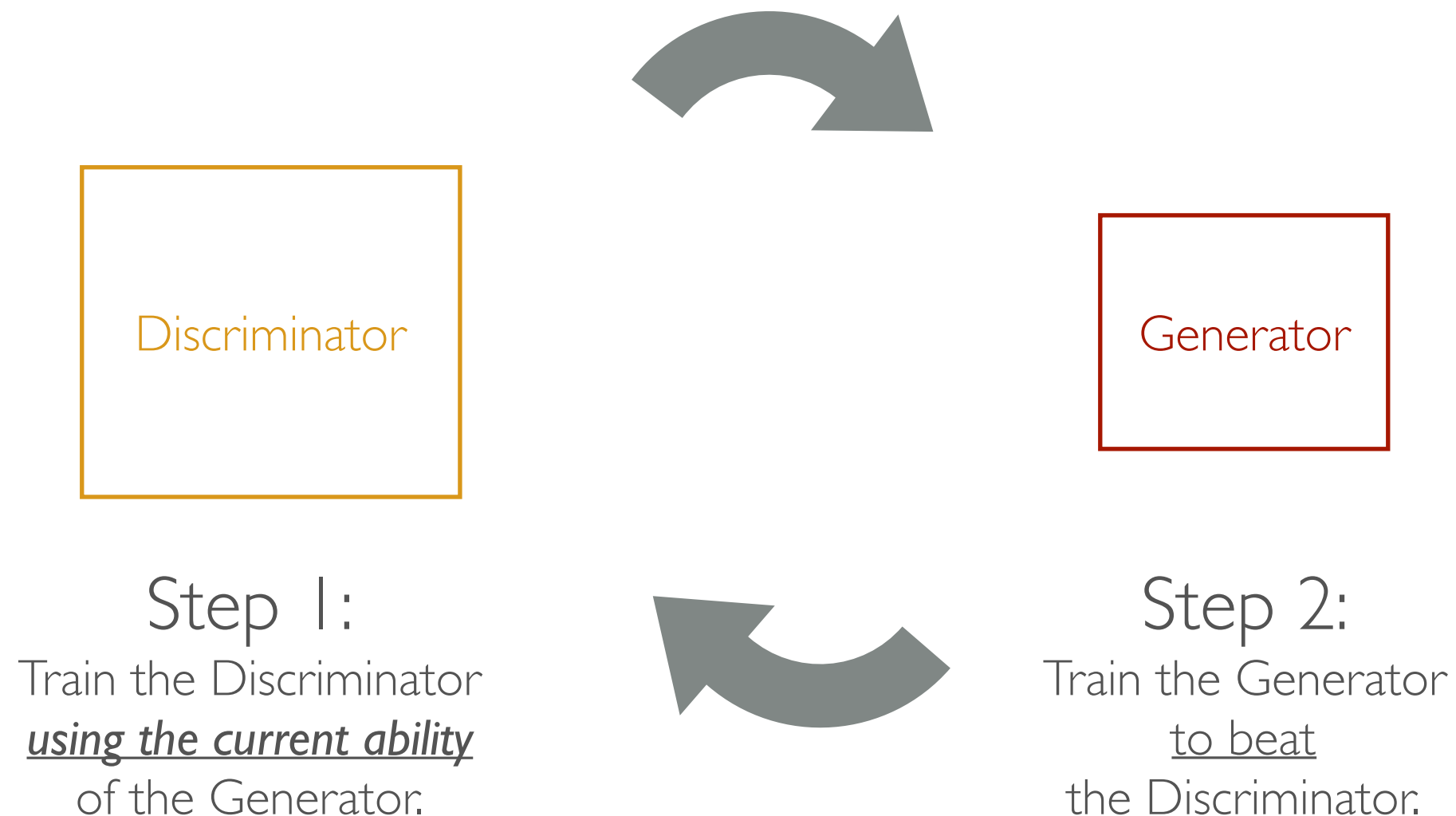
MIN-MAX STATIONARY POINT

- Stationary points need not be stable (depends on the exact GANs formulation and other factors)

MIN-MAX OPTIMIZATION

- Both generator and the discriminator need to be trained simultaneously
- If discriminator is undertrained, it provides sub-optimal feedback to the generator
- If the discriminator is overtrained, there is no local feedback for marginal improvements
- Discriminator and generator needs to be trained together

HOW TO TRAIN A GAN?



Objective: $\min_G \max_D V(D, G) = \mathbb{E}_X \log D(X) + \mathbb{E}_Z \log(1 - D(G(Z)))$

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- Human Evaluation
- Approximate Test Set likelihood
- Evaluate with Discriminative Network

GANS EVALUATION : INCEPTION SCORE

- Use a discriminative network (originally based on Inception v3 Architecture) to classify generated images
 - Inception should produce a variety of labels
 - Each label should have high confidence (low entropy)

QUESTIONS?