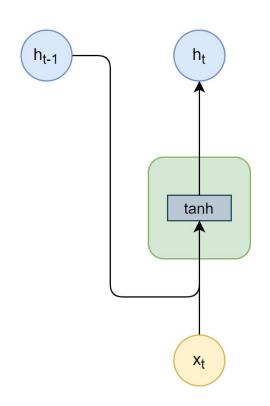
HW3P1

RNN, GRU, CTC, and Greedy / Beam Search

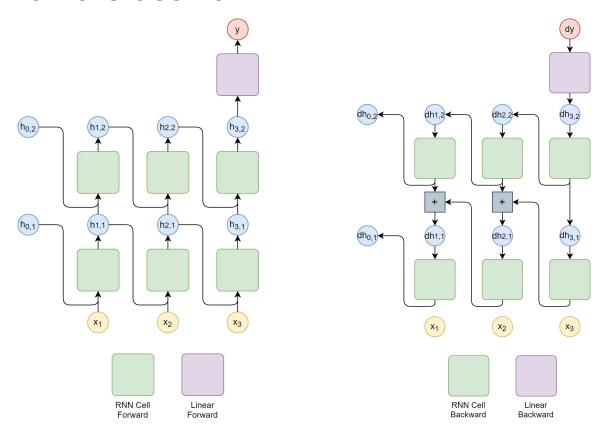
By Diksha Agarwal(Spring 2022)

RNN Cell Forward / Backward

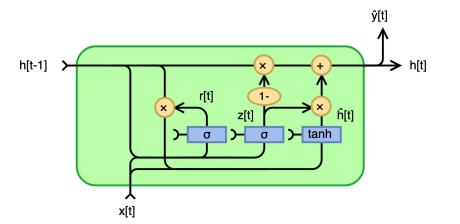


$$h_t = tanh(W_{ih}x_t + b_{ih} + W_{hh}h_{t-1} + b_{hh})$$

RNN Phoneme Classifier



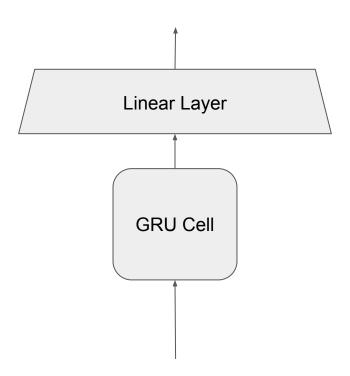
GRU Cell Forward / Backward



$$egin{aligned} \mathbf{r}_t &= \sigma(\mathbf{W}_{ir}\mathbf{x}_t + \mathbf{b}_{ir} + \mathbf{W}_{hr}\mathbf{h}_{t-1} + \mathbf{b}_{hr}) \ \mathbf{z}_t &= \sigma(\mathbf{W}_{iz}\mathbf{x}_t + \mathbf{b}_{iz} + \mathbf{W}_{hz}\mathbf{h}_{t-1} + \mathbf{b}_{hz}) \ \mathbf{n}_t &= anh(\mathbf{W}_{in}\mathbf{x}_t + \mathbf{b}_{in} + \mathbf{r}_t \otimes (\mathbf{W}_{hn}\mathbf{h}_{t-1} + \mathbf{b}_{hn})) \ \mathbf{h}_t &= (1 - \mathbf{z}_t) \otimes \mathbf{n}_t + \mathbf{z}_t \otimes \mathbf{h}_{t-1} \end{aligned}$$

https://colah.github.io/posts/2015-08-Backprop

GRU Inference



CTC - mytorch/ctc.py

```
def targetWithBlank(self, target):
    """Extend target sequence with blank.
def forwardProb(self, logits, extSymbols, skipConnect):
    """Compute forward probabilities.
def backwardProb(self, logits, extSymbols, skipConnect):
    """Compute backward probabilities.
def postProb(self, alpha, beta):
     """Compute posterior probabilities.
```

FORWARD ALGORITHM (with blanks)

```
[Sext, skipconnect] = extendedsequencewithblanks(S)
N = length(Sext) # Length of extended sequence
#The forward recursion
# First, at t = 1
alpha(1,1) = y(1, Sext(1)) #This is the blank
alpha(1,2) = v(1, Sext(2))
alpha(1,3:N) = 0
for t = 2:T
    alpha(t,1) = alpha(t-1,1)*v(t,Sext(1))
    for i = 2:N
        alpha(t,i) = alpha(t-1,i-1) + alpha(t-1,i)
        if (skipconnect(i))
            alpha(t,i) += alpha(t-1,i-2)
        alpha(t,i) *= y(t,Sext(i))
```

Without explicitly composing the output table

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

BACKWARD ALGORITHM WITH BLANKS

Without explicitly composing the output table

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

COMPUTING POSTERIORS

```
[Sext, skipconnect] = extendedsequencewithblanks(S)
N = length(Sext) # Length of extended sequence

#Assuming the forward are completed first
alpha = forward(y, Sext) # forward probabilities computed
beta = backward(y, Sext) # backward probabilities computed

#Now compute the posteriors
for t = 1:T
    sumgamma(t) = 0
    for i = 1:N
        gamma(t,i) = alpha(t,i) * beta(t,i)
        sumgamma(t) += gamma(t,i)
    end
    for i=1:N
        gamma(t,i) = gamma(t,i) / sumgamma(t)
```

COMPUTING DERIVATIVES

```
[Sext, skipconnect] = extendedsequencewithblanks(S)
N = length(Sext) # Length of extended sequence
#Assuming the forward are completed first
alpha = forward(y, Sext) # forward probabilities computed
beta = backward(y, Sext) # backward probabilities computed
# Compute posteriors from alpha and beta
gamma = computeposteriors(alpha, beta)
#Compute derivatives
for t = 1:T
   dy(t,1:L) = 0 #Initialize all derivatives at time t to 0
   for i = 1:N
       dv(t, Sext(i)) = gamma(t, i) / v(t, Sext(i))
```

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

CTC loss - mytorch/ctc_loss.py

```
def forward(self, logits, target, input_lengths, target_lengths):
    """CTC loss forward.
```

Computes the CTC Loss.

```
def backward(self):
    """CTC loss backard.
```

This must calculate the gradients wrt the parameters and return the derivative wrt the inputs, xt and ht, to the cell.

```
for b in range(B):
   # ----->
   # Computing CTC Loss for single batch
   # Process:
         Truncate the target to target length
         Truncate the logits to input length
         Extend target sequence with blank
         Compute forward probabilities
         Compute backward probabilities
         Compute posteriors using total probability function
         Compute expected divergence and store it in totalLoss
   # Your Code goes here
   raise NotImplementedError
```

```
for b in range(B):
      Computing CTC Derivative for single batch
    # Process:
          Truncate the target to target length
          Truncate the logits to input length
          Extend target sequence with blank
          Compute derivative of divergence and store them in dY
    # Your Code goes here
    raise NotImplementedError
```

Beam Search - mytorch/search.py

```
def BeamSearch(SymbolSets, y_probs, BeamWidth):
                                                                                            """Beam Search.
def GreedySearch(SymbolSets, y_probs):
    """Greedy Search.
                                                                                            Input
    Input
                                                                                           SymbolSets: list
                                                                                                       all the symbols (the vocabulary without blank)
    SymbolSets: list
                 all the symbols (the vocabulary without blank)
                                                                                           y_probs: (# of symbols + 1, Seq_length, batch_size)
                                                                                                   Your batch size for part 1 will remain 1, but if you plan to use your
    y_probs: (# of symbols + 1, Seg_length, batch_size)
                                                                                                   implementation for part 2 you need to incorporate batch size.
            Your batch size for part 1 will remain 1, but if you plan to use your
            implementation for part 2 you need to incorporate batch_size.
                                                                                            BeamWidth: int
                                                                                                       Width of the beam.
    Returns
                                                                                            Return
    forward path: str
                                                                                            bestPath: str
                 the corresponding compressed symbol sequence i.e. without blanks
                                                                                                   the symbol sequence with the best path score (forward probability)
                 or repeated symbols.
                                                                                            mergedPathScores: dictionary
    forward prob: scalar (float)
                                                                                                               all the final merged paths with their scores.
                 the forward probability of the greedy path
                                                                                            ....
    11 11 11
```

BEAM SEARCH

```
Global PathScore = [], BlankPathScore = []
# First time instant: Initialize paths with each of the symbols,
# including blank, using score at time t=1
NewPathsWithTerminalBlank, NewPathsWithTerminalSymbol, NewBlankPathScore, NewPathScore =
                           InitializePaths (SymbolSet, y[:,0])
# Subsequent time steps
for t = 1:T
    # Prune the collection down to the BeamWidth
    PathsWithTerminalBlank, PathsWithTerminalSymbol, BlankPathScore, PathScore =
                   Prune (NewPathsWithTerminalBlank, NewPathsWithTerminalSymbol,
                                             NewBlankPathScore, NewPathScore, BeamWidth)
    # First extend paths by a blank
    NewPathsWithTerminalBlank, NewBlankPathScore = ExtendWithBlank (PathsWithTerminalBlank,
                                                                  PathsWithTerminalSymbol, v[:,t])
    # Next extend paths by a symbol
    NewPathsWithTerminalSymbol, NewPathScore = ExtendWithSymbol (PathsWithTerminalBlank,
                                                         PathsWithTerminalSymbol, SymbolSet, y[:,t])
end
# Merge identical paths differing only by the final blank
MergedPaths, FinalPathScore = MergeIdenticalPaths (NewPathsWithTerminalBlank, NewBlankPathScore
                                                  NewPathsWithTerminalSymbol, NewPathScore)
# Pick best path
BestPath = argmax(FinalPathScore) # Find the path with the best score
```

BEAM SEARCH InitializePaths: FIRST TIME INSTANT

```
function InitializePaths(SymbolSet, y)
InitialBlankPathScore = [], InitialPathScore = []
# First push the blank into a path-ending-with-blank stack. No symbol has been invoked yet
path = null
InitialBlankPathScore[path] = y[blank] # Score of blank at t=1
InitialPathsWithFinalBlank = {path}
# Push rest of the symbols into a path-ending-with-symbol stack
InitialPathsWithFinalSymbol = {}
for c in SymbolSet # This is the entire symbol set, without the blank
   path = c
   InitialPathScore[path] = y[c] # Score of symbol c at t=1
   InitialPathsWithFinalSymbol += path # Set addition
end
return InitialPathsWithFinalBlank, InitialPathsWithFinalSymbol,
      InitialBlankPathScore, InitialPathScore
```

BEAM SEARCH: Extending with blanks

Global PathScore, BlankPathScore

```
function ExtendWithBlank (PathsWithTerminalBlank, PathsWithTerminalSymbol, y)
   UpdatedPathsWithTerminalBlank = {}
   UpdatedBlankPathScore = []
   # First work on paths with terminal blanks
   #(This represents transitions along horizontal trellis edges for blanks)
   for path in PathsWithTerminalBlank:
        # Repeating a blank doesn't change the symbol sequence
       UpdatedPathsWithTerminalBlank += path # Set addition
       UpdatedBlankPathScore[path] = BlankPathScore[path]*y[blank]
    end
   # Then extend paths with terminal symbols by blanks
   for path in PathsWithTerminalSymbol:
        # If there is already an equivalent string in UpdatesPathsWithTerminalBlank
       # simply add the score. If not create a new entry
       if path in UpdatedPathsWithTerminalBlank
           UpdatedBlankPathScore[path] += Pathscore[path] * v[blank]
        else
           UpdatedPathsWithTerminalBlank += path # Set addition
           UpdatedBlankPathScore[path] = PathScore[path] * v[blank]
        end
    end
   return UpdatedPathsWithTerminalBlank,
          UpdatedBlankPathScore
```

BEAM SEARCH: Extending with symbols

Global PathScore, BlankPathScore

```
function ExtendWithSymbol (PathsWithTerminalBlank, PathsWithTerminalSymbol, SymbolSet, y)
   UpdatedPathsWithTerminalSymbol = {}
   UpdatedPathScore = []
   # First extend the paths terminating in blanks. This will always create a new sequence
   for path in PathsWithTerminalBlank:
        for c in SymbolSet: # SymbolSet does not include blanks
           newpath = path + c # Concatenation
           UpdatedPathsWithTerminalSymbol += newpath # Set addition
           UpdatedPathScore[newpath] = BlankPathScore[path] * y(c)
        end
   end
   # Next work on paths with terminal symbols
   for path in PathsWithTerminalSymbol:
        # Extend the path with every symbol other than blank
        for c in SymbolSet: # SymbolSet does not include blanks
           newpath = (c == path[end]) ? path : path + c # Horizontal transitions don't extend the sequence
           if newpath in UpdatedPathsWithTerminalSymbol: # Already in list, merge paths
               UpdatedPathScore[newpath] += PathScore[path] * v[c]
            else # Create new path
               UpdatedPathsWithTerminalSymbol += newpath # Set addition
               UpdatedPathScore[newpath] = PathScore[path] * y[c]
            end
        end
   end
   return UpdatedPathsWithTerminalSymbol,
          UpdatedPathScore
```

BEAM SEARCH: Pruning low-scoring entries

Global PathScore, BlankPathScore

```
function Prune (PathsWithTerminalBlank, PathsWithTerminalSymbol, BlankPathScore, PathScore, BeamWidth)
    PrunedBlankPathScore = []
    PrunedPathScore = []
    # First gather all the relevant scores
    i = 1
    for p in PathsWithTerminalBlank
        scorelist[i] = BlankPathScore[p]
        i++
    end
    for p in PathsWithTerminalSymbol
        scorelist[i] = PathScore[p]
        i++
    end
    # Sort and find cutoff score that retains exactly BeamWidth paths
    sort(scorelist) # In decreasing order
    cutoff = BeamWidth < length(scorelist) ? scorelist[BeamWidth] : scorelist[end]</pre>
    PrunedPathsWithTerminalBlank = {}
    for p in PathsWithTerminalBlank
        if BlankPathScore[p] >= cutoff
            PrunedPathsWithTerminalBlank += p # Set addition
            PrunedBlankPathScore[p] = BlankPathScore[p]
        end
    end
    PrunedPathsWithTerminalSymbol = {}
    for p in PathsWithTerminalSymbol
        if PathScore[p] >= cutoff
            PrunedPathsWithTerminalSymbol += p # Set addition
            PrunedPathScore[p] = PathScore[p]
        end
    end
    return PrunedPathsWithTerminalBlank, PrunedPathsWithTerminalSymbol, PrunedBlankPathScore, PrunedPathScore
```

BEAM SEARCH: Merging final paths

```
# Note : not using global variable here
function MergeIdenticalPaths (PathsWithTerminalBlank, BlankPathScore,
                             PathsWithTerminalSymbol, PathScore)
    # All paths with terminal symbols will remain
    MergedPaths = PathsWithTerminalSymbol
    FinalPathScore = PathScore
    # Paths with terminal blanks will contribute scores to existing identical paths from
    # PathsWithTerminalSymbol if present, or be included in the final set, otherwise
    for p in PathsWithTerminalBlank
        if p in MergedPaths
            FinalPathScore[p] += BlankPathScore[p]
        else
            MergedPaths += p # Set addition
            FinalPathScore[p] = BlankPathScore[p]
        end
    end
    return MergedPaths, FinalPathScore
```

Thank you! Q & A