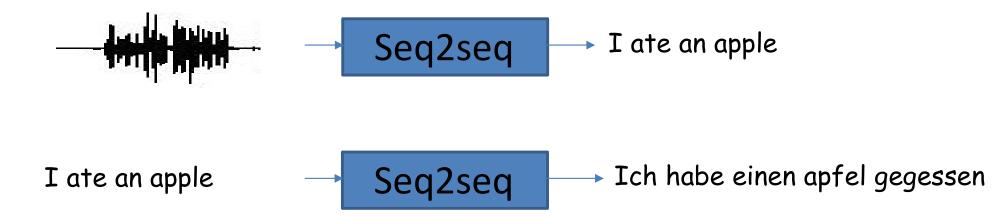
Deep Learning Sequence to Sequence models: Connectionist Temporal Classification

Sequence-to-sequence modelling

Problem:

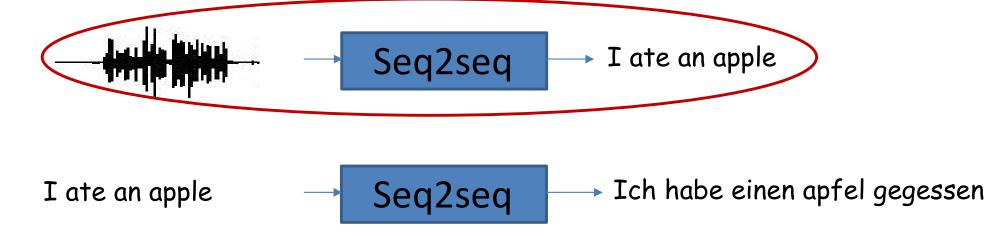
- A sequence $X_1 \dots X_N$ goes in
- A different sequence $Y_1 \dots Y_M$ comes out
- E.g.
 - Speech recognition: Speech goes in, a word sequence comes out
 - Alternately output may be phoneme or character sequence
 - Machine translation: Word sequence goes in, word sequence comes out
 - Dialog: User statement goes in, system response comes out
 - Question answering: Question comes in, answer goes out
- In general $N \neq M$
 - No synchrony between X and Y.

Sequence to sequence



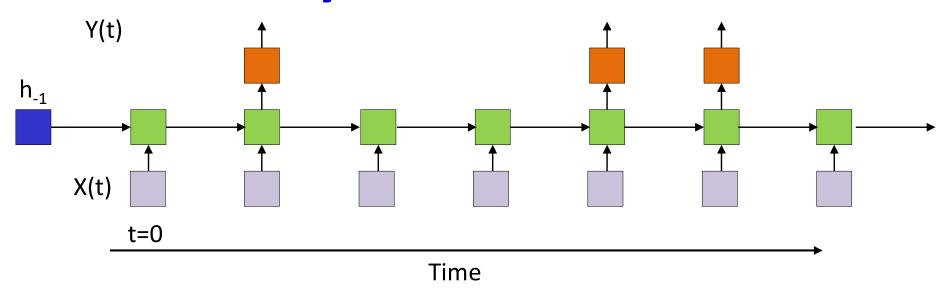
- Sequence goes in, sequence comes out
- No notion of "time synchrony" between input and output
 - May even not even maintain order of symbols
 - E.g. "I ate an apple" → "Ich habe einen apfel gegessen"
 - Or even seem related to the input
 - E.g. "My screen is blank" → "Please check if your computer is plugged in."

Sequence to sequence



- Sequence goes in, sequence comes out
- No notion of "time synchrony" between input and output
 - May even not even maintain order of symbols
 - E.g. "I ate an apple" → "Ich habe einen apfel gegessen"
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 - E.g. "My screen is blank" → "Can you check if your computer is plugged in?"

Case 1: Order-aligned but not time synchronous



- The input and output sequences happen in the same order
 - Although they may not be time synchronous, they can be "aligned" against one another
 - E.g. Speech recognition
 - The input speech can be aligned to the phoneme sequence output

Problems

- How do we perform inference on such a model
 - How to output time-asynchronous sequences

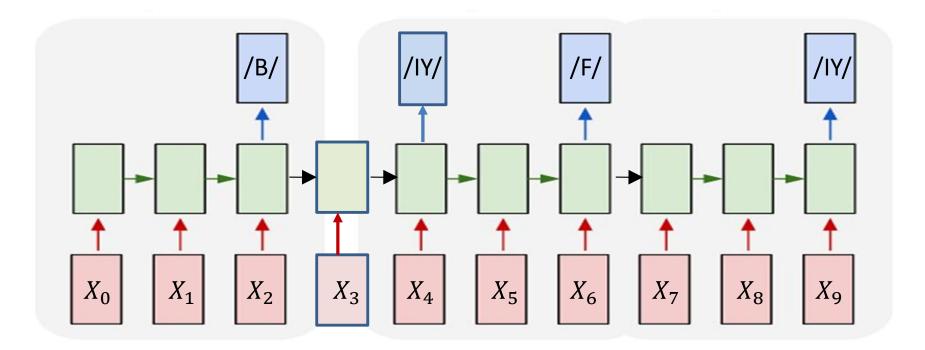
How do we train such models

Problems

- How do we perform inference on such a model
 Partially addressed
 - How to output time-asynchronous sequences

How do we train such models

The inference problem



- Objective: Given a sequence of inputs, asynchronously output a sequence of symbols
 - "Decoding"
- Find most likely symbol sequence given inputs

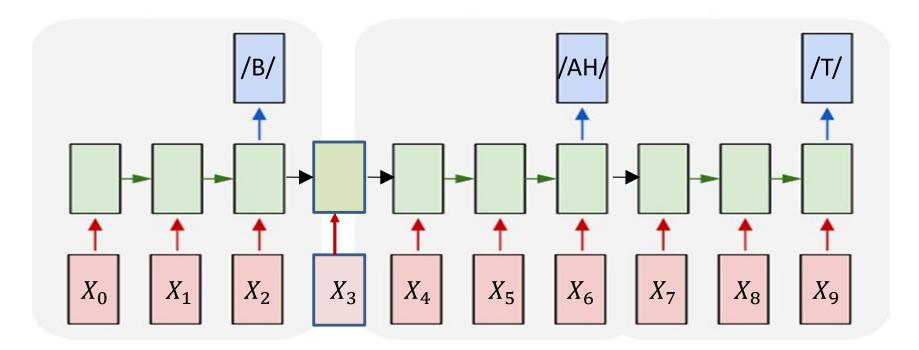
$$S_0 \dots S_{K-1} = \underset{S'_0 \dots S'_{K-1}}{\operatorname{argmax}} prob(S'_0 \dots S'_{K-1} | X_0 \dots X_{N-1})$$

Problems

- How do we perform inference on such a model
 - How to output time-asynchronous sequences

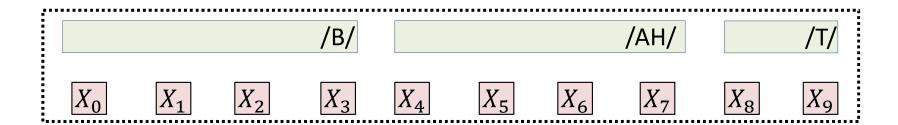
How do we train such models

Recap: Training with alignment



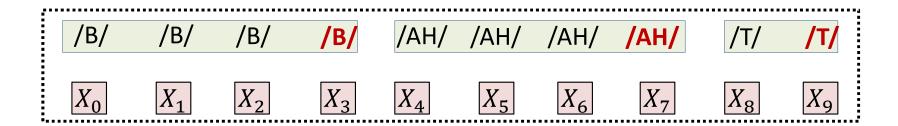
- Training data: input sequence + output sequence
 - Output sequence length <= input sequence length</p>
- Given the alignment of the output to the input
 - The phoneme /B/ ends at X_2 , /AH/ at X_6 , /T/ at X_9

Recap: Characterizing an alignment



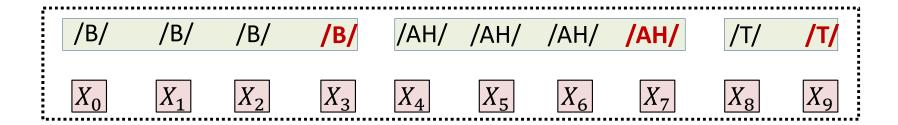
- Given only the order-synchronous sequence and its time stamps
 - $S_0(T_0), S_1(T_1), \dots, S_{K-1}(T_{K-1})$
 - E.g. $S_0 = /B/(3)$, $S_1 = /B/(7)$, $S_2 = /T/(9)$,

Recap: Characterizing an alignment



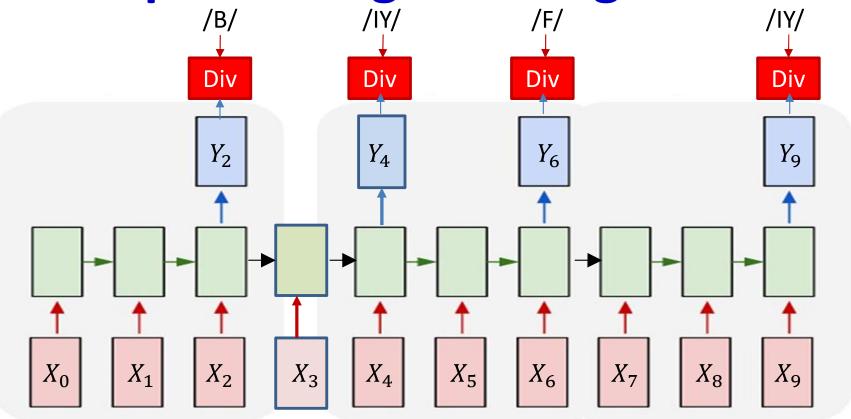
- Given only the order-synchronous sequence and its time stamps
 - $S_0(T_0), S_1(T_1), \dots, S_{K-1}(T_{K-1})$
 - E.g. $S_0 = /B/(3)$, $S_1 = /B/(7)$, $S_2 = /T/(9)$,
- Repeat symbols to convert it to a time-synchronous sequence
 - $s_0, s_1, ..., s_{N-1} = S_0, S_0, ..., (T_0 times), S_1, S_1, ..., (T_1 times), ..., S_{K-1}$
 - E.g. $s_0, s_1, ..., s_9 = \frac{B}{B} \frac{B}{B} \frac{B}{B} \frac{AH}{AH} \frac{AH}{AH} \frac{AH}{AH} \frac{AH}{AH} \frac{H}{AH}$

Recap: Characterizing an alignment

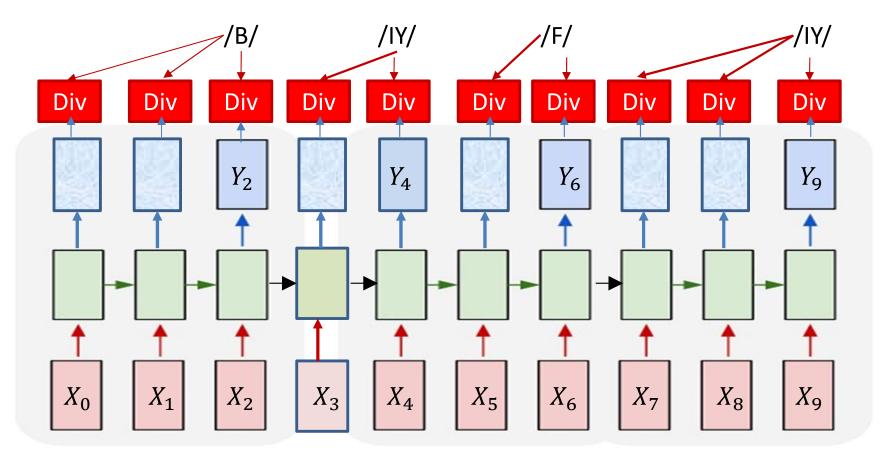


- Given only the order-synchronous sequence and its time stamps
 - $S_0(T_0), S_1(T_1), ..., S_{K-1}(T_{K-1})$
 - E.g. $S_0 = /B/(3)$, $S_1 = /B/(7)$, $S_2 = /T/(9)$,
- Repeat symbols to convert it to a time-synchronous sequence
 - $s_0 = S_0, s_1 = S_0, \dots, S_{T_0} = S_0, s_{T_0+1} = S_1, \dots, s_{T_1} = S_1, s_{T_1+1} = S_2, \dots, s_{N-1} = S_{K-1}$
 - E.g. $s_0, s_1, ..., s_9 = \frac{B}{B} \frac{B}{B} \frac{B}{B} \frac{AH}{AH} \frac{AH}{AH} \frac{AH}{AH} \frac{AH}{T}$
- For our purpose an alignment of S_0 ... S_{K-1} to an input of length N has the form $s_0, s_1, ..., s_{N-1} = S_0, S_0, ..., S_0, S_1, S_1, ..., S_1, S_2, ..., S_{K-1}$ (of length N)
- Any sequence of this kind of length N that contracts (by eliminating repetitions) to $S_0 \dots S_{K-1}$ is a candidate alignment of $S_0 \dots S_{K-1}$

Recap: Training with alignment

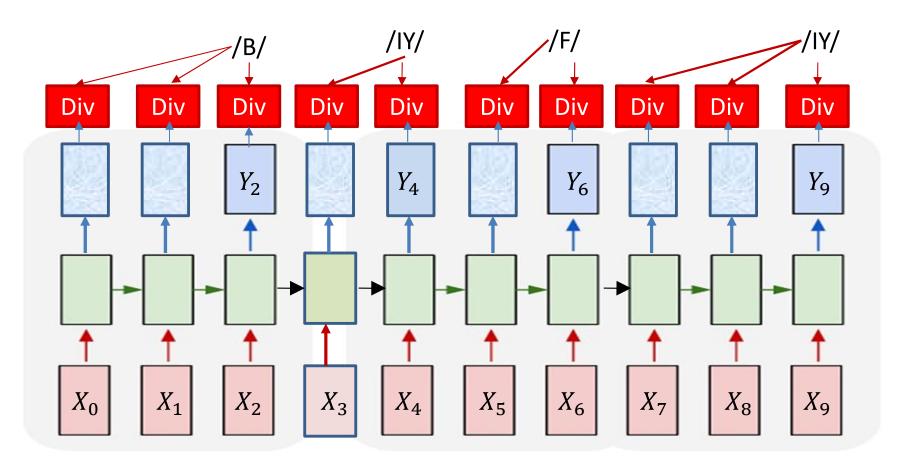


Given the order-aligned output sequence with timing



- Given the order aligned output sequence with timing
 - Convert it to a time-synchronous alignment by repeating symbols
- Compute the divergence from the time-aligned sequence

$$DIV = \sum_{t} KL(Y_{t}, symbol_{t}) = -\sum_{t} \log Y(t, symbol_{t})$$



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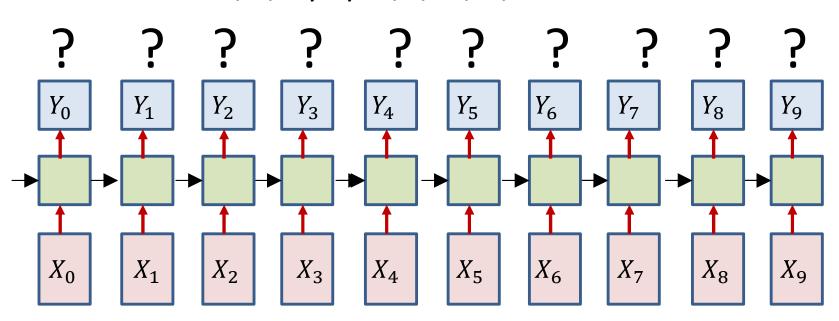
• The gradient w.r.t the t-th output vector Y_t

$$\nabla_{Y_t} DIV = \begin{bmatrix} 0 & 0 & \dots & \frac{-1}{Y(t, symbol_t)} & 0 & \dots & 0 \end{bmatrix}$$

 Zeros except at the component corresponding to the target aligned to that time

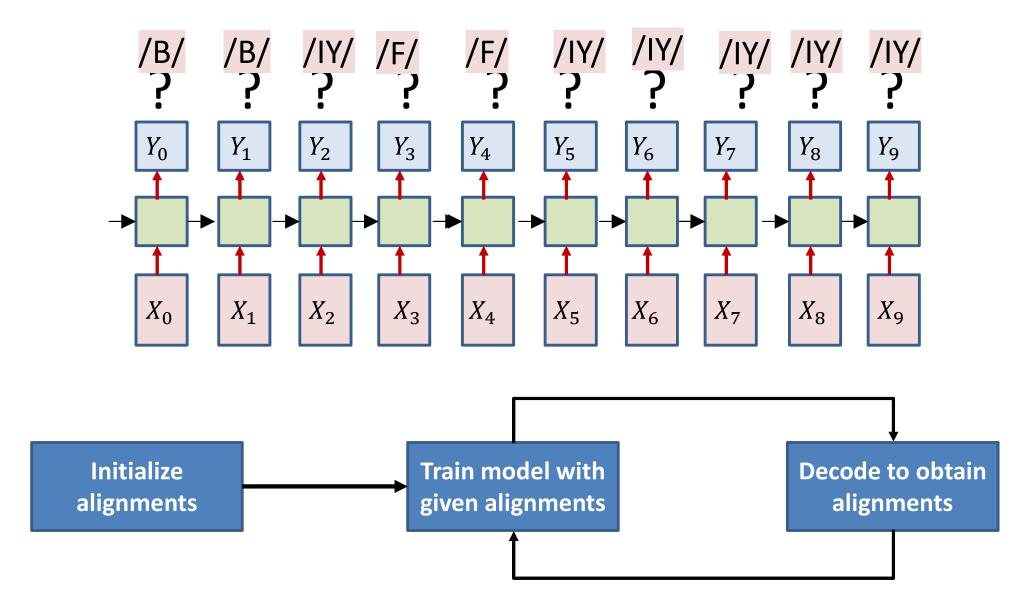
Problem: Alignment not provided

/B/ /IY/ /F/ /IY/



- Only the sequence of output symbols is provided for the training data
 - But no timing information

Solution 1: Guess the alignment



Poll 1 (@862, @863)

Viterbi training explicitly estimates the alignment of each training instance and computes the divergence for the estimated alignment (T/F)

- True
- False

Viterbi training requires reestimation of alignments in every iteration (T/F)

- True
- False

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Iterative update: Problem

 Approach heavily dependent on initial alignment

Prone to poor local optima

Alternate solution: Do not commit to an alignment during any pass..

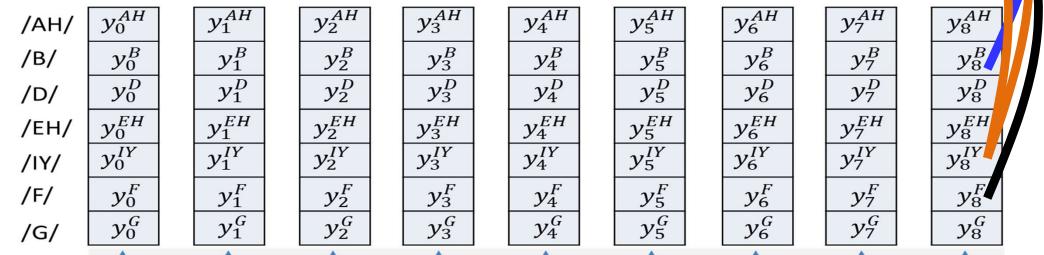
Recap: Training without alignment

- We know how to train if the alignment is provided
- Problem: Alignment is not provided

- Solution:
 - 1. Guess the alignment
 - 2. Consider all possible alignments

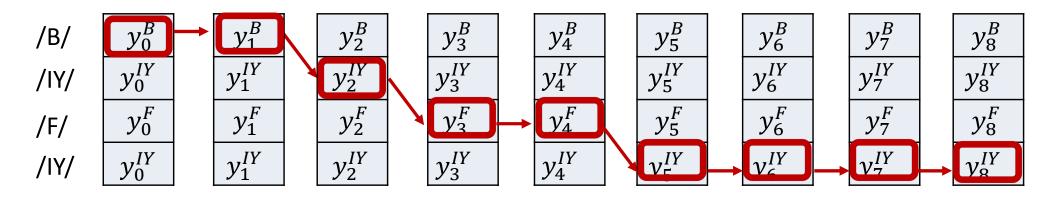
Recap: The "aligned" table

 y_1^B y_2^B y_0^B y_3^B y_4^B y_6^B y_7^B y_8^B y_5^B /B/ y_1^{IY} y_2^{IY} y_0^{IY} y_3^{IY} y_5^{IY} y_6^{IY} y_7^{IY} y_8^{IY} y_4^{IY} /IY/ y_2^F y_6^F y_0^F y_1^F y_3^F y_7^F y_4^F y_5^F y_8^F /F/ y_1^{IY} y_2^{IY} y_3^{IY} y_7^{IY} y_0^{IY} y_4^{IY} y_5^{IY} y_6^{IY} /IY/



Arrange the constructed table so that from top to bottom it has the exact sequence of symbols required

The reason for suboptimality

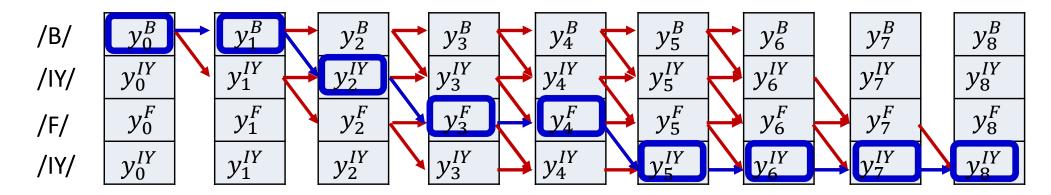


- We commit to the single "best" estimated alignment
 - The most likely alignment

$$DIV = -\sum_{t} \log Y\left(t, symbol_{t}^{bestpath}\right)$$

This can be way off, particularly in early iterations, or if the model is poorly initialized

The reason for suboptimality

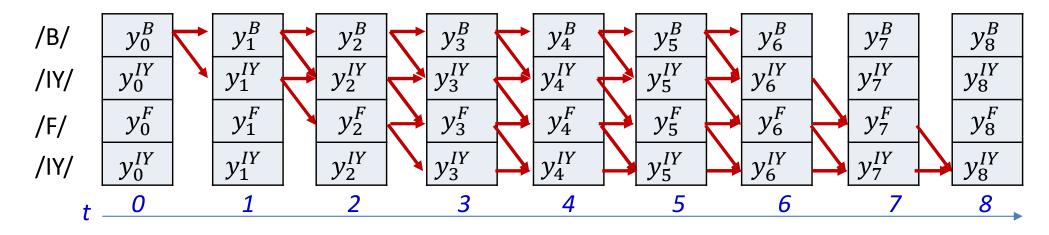


- We commit to the single "best" estimated alignment
 - The most likely alignment

$$DIV = -\sum_{t} \log Y\left(t, symbol_{t}^{bestpath}\right)$$

- This can be way off, particularly in early iterations, or if the model is poorly initialized
- Alternate view: there is a probability distribution over alignments of the target Symbol sequence (to the input)
 - Selecting a single alignment is the same as drawing a single sample from it
 - Selecting the most likely alignment is the same as deterministically always drawing the most probable value from the distribution

Averaging over all alignments



 Instead of only selecting the most likely alignment, use the statistical expectation over all possible alignments

$$DIV = E\left[-\sum_{t} \log Y(t, s_t)\right]$$

- Use the entire distribution of alignments
- This will mitigate the issue of suboptimal selection of alignment

Poll 2 (@864, @865)

The "training-without-alignment" procedure computes the average divergence over *all possible* alignments of the label sequence to the input (T/F)

- True
- False

The "training-without-alignment" requires explicit estimation of the alignment of the label sequence to the input

- True
- False

Poll 2

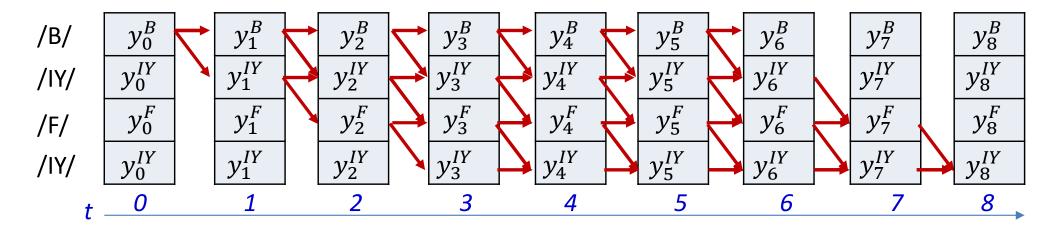
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- True
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The "training-without-alignment" requires explicit estimation of the alignment of the label sequence to the input

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The expectation over all alignments



$$DIV = E\left[-\sum_{t} \log Y(t, s_t)\right]$$

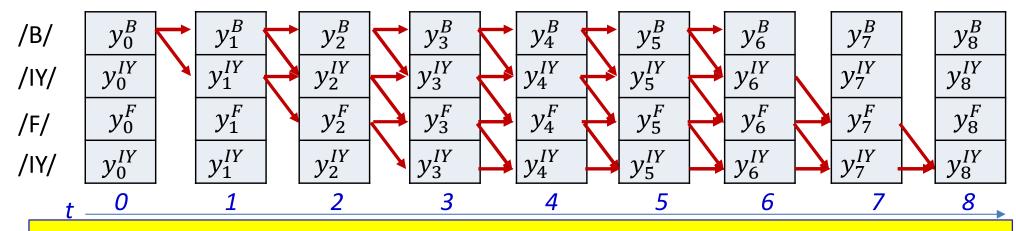
Using the linearity of expectation

$$DIV = -\sum_{t} E[\log Y(t, s_t)]$$

This reduces to finding the expected divergence at each input

$$DIV = -\sum_{t} \sum_{S \in S_1 \dots S_K} P(s_t = S | \mathbf{S}, \mathbf{X}) \log Y(t, s_t = S)$$

The expectation over all alignments



The probability of aligning the specific symbols at time t, given that unaligned sequence $\mathbf{S} = S_0 \dots S_{K-1}$ and given the input sequence $\mathbf{X} = X_0 \dots X_{N-1}$

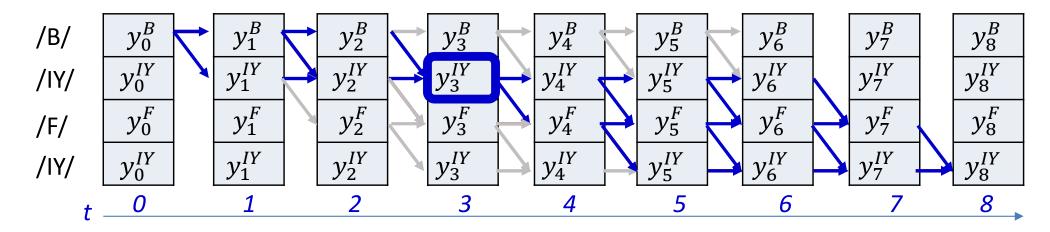
We need to be able to compute this

$$DIV = -\sum_{t} E[\log Y(t, s_t)]$$

This reduces to finding the expected divergence at each input

$$DIV = -\sum_{t} \sum_{S \in S_1 \dots S_K} P(s_t = S | \mathbf{S}, \mathbf{X}) \log Y(t, s_t = S)$$

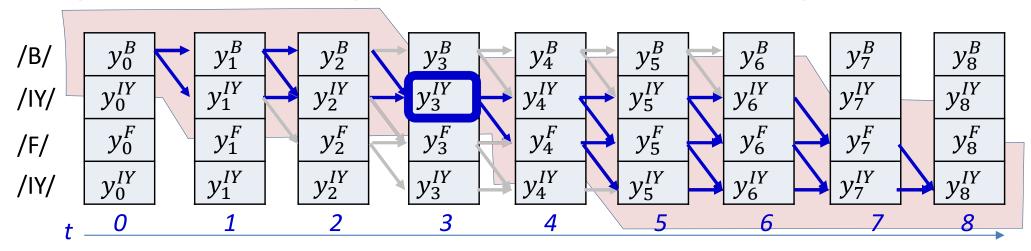
A posteriori probabilities of symbols



$$P(s_t = S_r | \mathbf{S}, \mathbf{X}) \propto P(s_t = S_r, \mathbf{S} | \mathbf{X})$$

- $P(s_t = S_r, \mathbf{S} | \mathbf{X})$ is the total probability of all valid paths in the graph for target sequence \mathbf{S} that go through the symbol S_r (the r^{th} symbol in the sequence $S_0 \dots S_{K-1}$) at time t
- We will compute this using the "forward-backward" algorithm

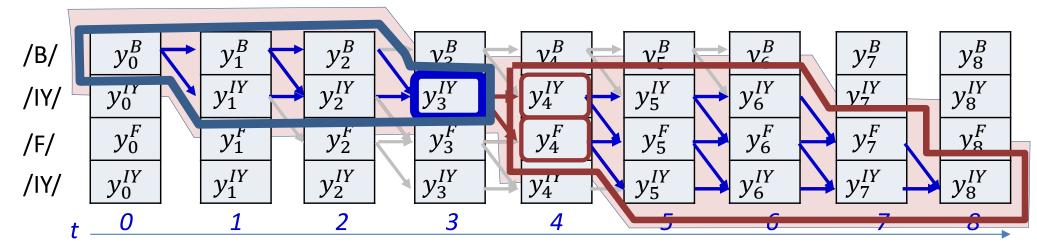
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A posteriori probabilities of symbols



• $P(s_t = S_r, \mathbf{S} | \mathbf{X})$ can be decomposed as

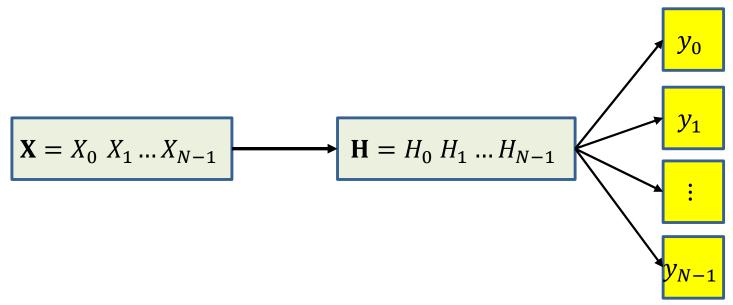
$$\begin{split} P(s_t = S_r, \mathbf{S} | \mathbf{X}) &= P(S_0, \dots, S_r, \dots, S_{K-1}, s_t = S_r | \mathbf{X}) \\ &= P(S_0 \dots S_r, s_t = S_r, s_{t+1} \in succ(S_r), succ(S_r), \dots, S_{K-1} | \mathbf{X}) \end{split}$$

Using Bayes Rule

$$= P(S_0 ... S_r, s_t = S_r | \mathbf{X}) P(s_{t+1} \in succ(S_r), succ(S_r), ..., S_{K-1} | S_0 ... S_r, s_t = S_r \mathbf{X})$$

 The probability of the subgraph in the blue outline, times the conditional probability of the red-encircled subgraph, given the blue subgraph

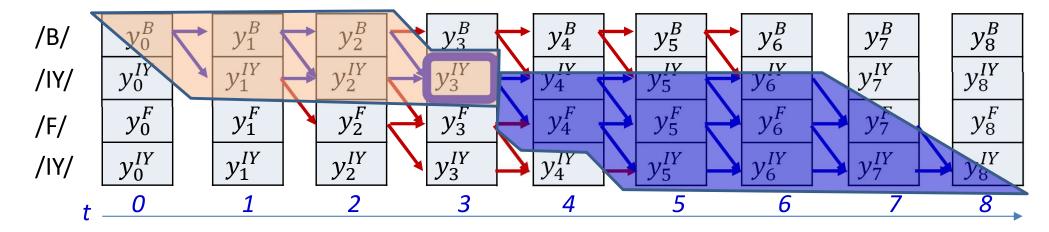
Conditional independence



- **Dependency graph:** Input sequence $\mathbf{X} = X_0 \ X_1 \dots X_{N-1}$ governs hidden variables $\mathbf{H} = H_0 \ H_1 \dots H_{N-1}$
- Hidden variables govern output predictions $y_0, y_1, ... y_{N-1}$ individually
- $y_0, y_1, ... y_{N-1}$ are conditionally independent given **H**
- Since **H** is deterministically derived from \mathbf{X} , y_0 , y_1 , ... y_{N-1} are also conditionally independent given \mathbf{X}
 - This wouldn't be true if the relation between \mathbf{X} and \mathbf{H} were not deterministic or if \mathbf{X} is unknown, or if the ys at any time went back into the net as inputs

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A posteriori symbol probability

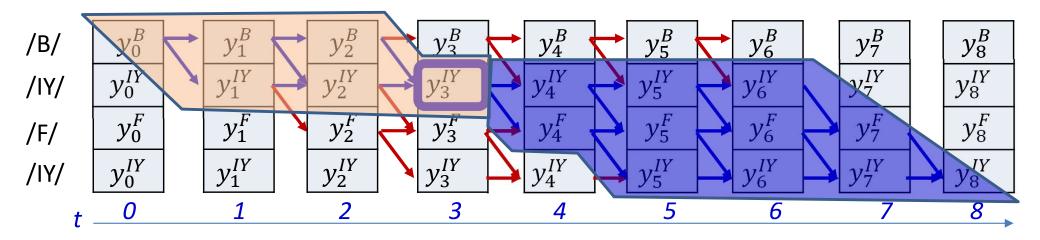


$$P(s_t = S_r, \mathbf{S} | \mathbf{X})$$

$$= P(S_0 \dots S_r, s_t = S_r | \mathbf{X}) P(s_{t+1} \in succ(S_r), succ(S_r), \dots, S_{K-1} | \mathbf{X})$$

- We will call the first term the forward probability $\alpha(t,r)$
- We will call the second term the backward probability $\beta(t,r)$

A posteriori symbol probability

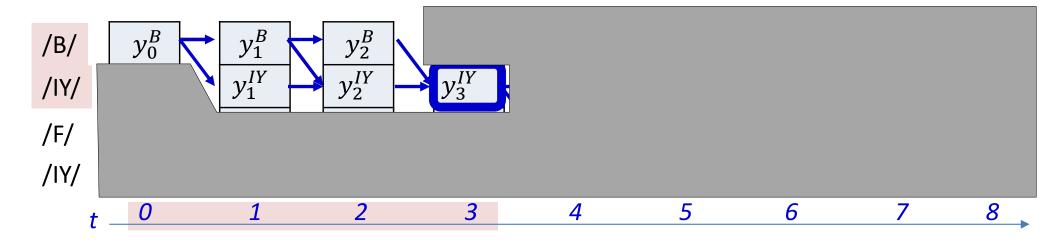


$$P(s_t = S_r, \mathbf{S} | \mathbf{X})$$

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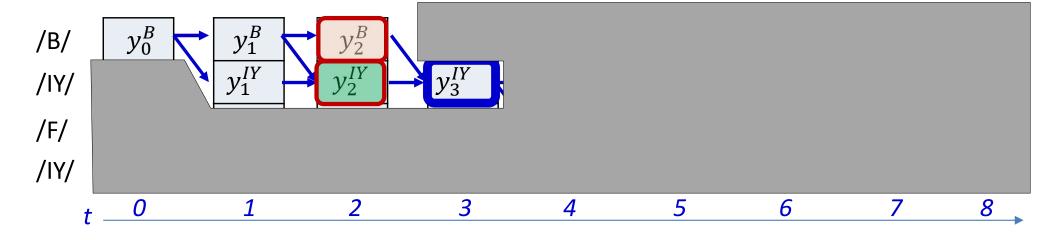
Computing $\alpha(t,r)$: Forward algorithm



$$\alpha(t,r) = P(S_0..S_r, S_t = S_r | \mathbf{X})$$

- The $\alpha(t,r)$ is the total probability of the subgraph shown
 - The total probability of all paths leading to the alignment of S_r to time t

Computing $\alpha(t,r)$: Forward algorithm





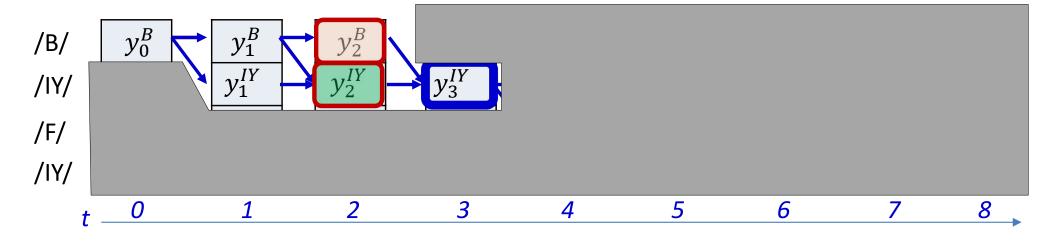
$$\alpha(3, IY) = P(S_0 ... S_r, s_t = S_r | \mathbf{X})$$

 $\alpha(3,IY) = P(subgraph\ ending\ at\ (2,B))y_3^{IY} + P(subgraph\ ending\ at\ (2,IY))y_3^{IY}$

$$\alpha(t,r) = \sum_{q:S_q \in pred(S_r)} P(subgraph \ ending \ at \ (t-1,q)) Y_t^{S(r)}$$

- Where $pred(S_r)$ is any symbol that is permitted to come before an S_r and may include S_r
- q is its row index, and can take values r and r-1 in this example

Computing $\alpha(t,r)$: Forward algorithm



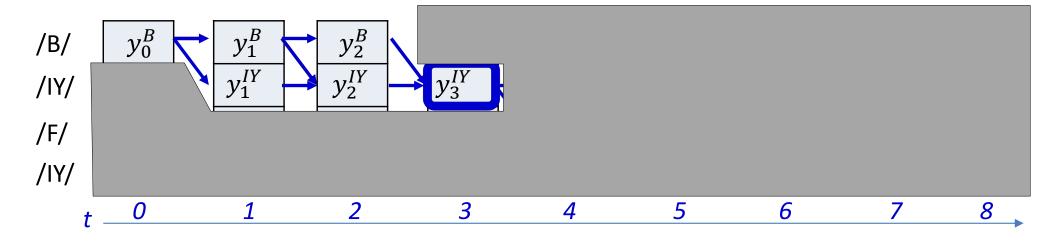


$$\alpha(t,r) = P(S_0..S_r, s_t = S_r | \mathbf{X})$$

$$\alpha(3, IY) = \alpha(2, B)y_3^{IY} + \alpha(2, IY)y_3^{IY}$$

$$\alpha(t,r) = \sum_{q: S_q \in pred(S_r)} \alpha(t-1,q) Y_t^{S(r)}$$

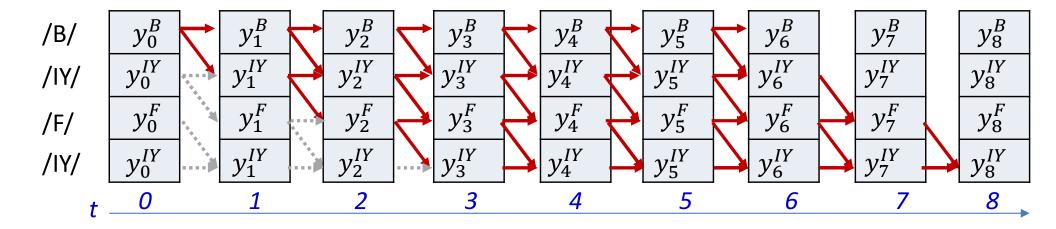
- Where $pred(S_r)$ is any symbol that is permitted to come before an S_r and may include S_r
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• The $\alpha(t,r)$ is the total probability of the subgraph shown

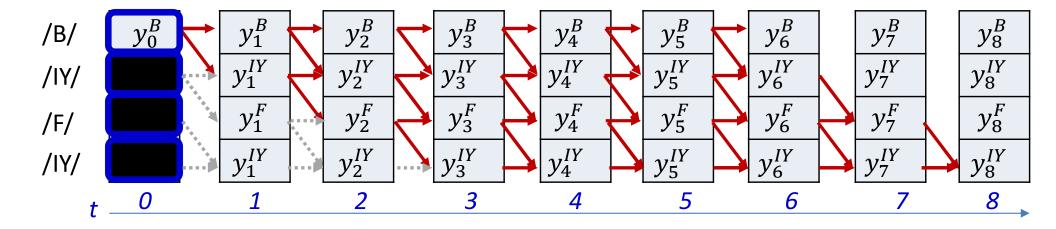
$$\alpha(t,r) = (\alpha(t-1,r) + \alpha(t-1,r-1))y_t^{S(r)}$$



• Initialization:

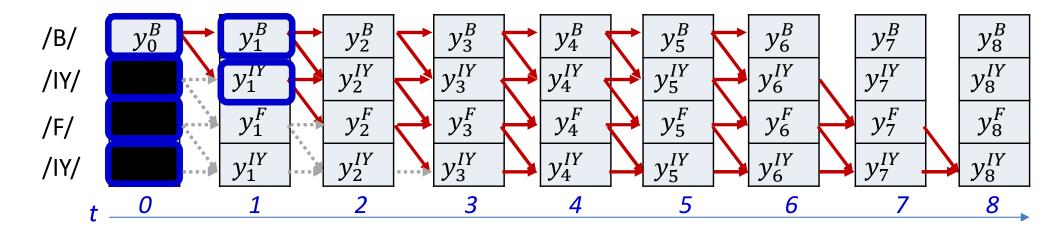
$$\alpha(0,0) = y_0^{S(0)}, \quad \alpha(0,r) = 0, r > 0$$

• for $t = 1 \dots T - 1$ $\alpha(t,0) = \alpha(t-1,0)y_t^{S(0)}$ for $l = 1 \dots K - 1$ $\alpha(t,l) = (\alpha(t-1,l) + \alpha(t-1,l-1))y_t^{S(l)}$



• Initialization:

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Initialization:

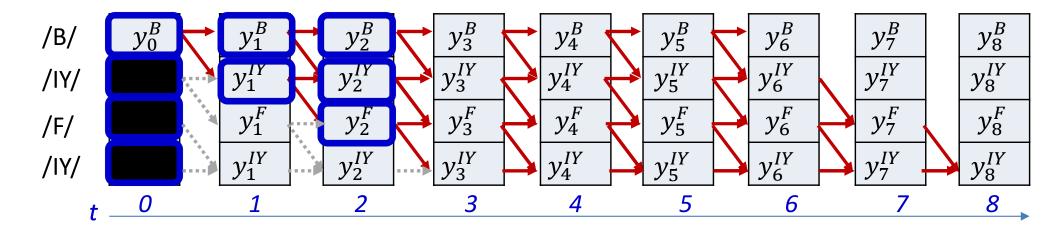
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for $l = 1 ... K - 1$

•
$$\alpha(t,l) = (\alpha(t-1,l) + \alpha(t-1,l-1))y_t^{S(l)}$$



• Initialization:

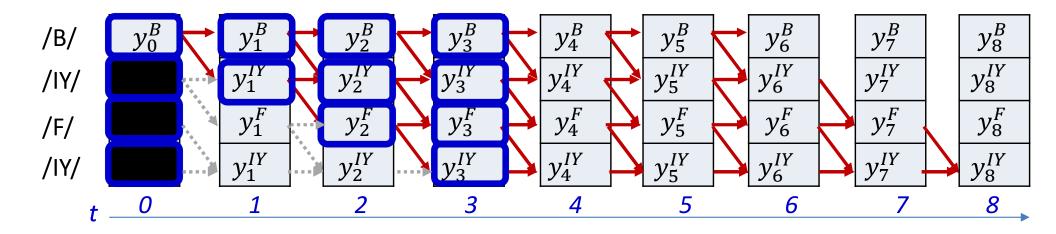
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Initialization:

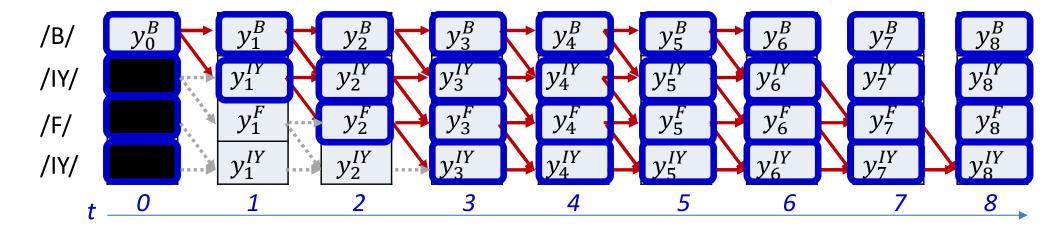
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• for
$$t = 1 ... T - 1$$

$$\alpha(t,0) = \alpha(t-1,0)y_t^{S(0)}$$

for $l = 1 \dots K-1$

•
$$\alpha(t,l) = (\alpha(t-1,l) + \alpha(t-1,l-1))y_t^{S(l)}$$

In practice...

The recursion

$$\alpha(t,l) = (\alpha(t-1,l) + \alpha(t-1,l-1))y_t^{S(l)}$$
 will generally underflow

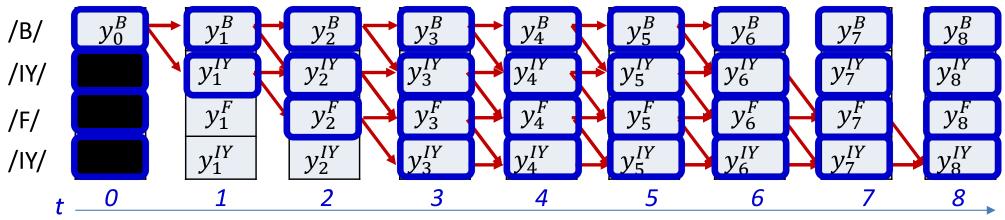
• Instead we can do it in the log domain $\log \alpha(t,l)$

$$= \log(e^{\log \alpha(t-1,l)} + e^{\log \alpha(t-1,l-1)}) + \log y_t^{S(l)}$$

This can be computed entirely without underflow

Forward algorithm: Alternate

statement



- The algorithm can also be stated as follows which separates the graph probability from the observation probability. This is needed to compute derivatives
- Initialization:

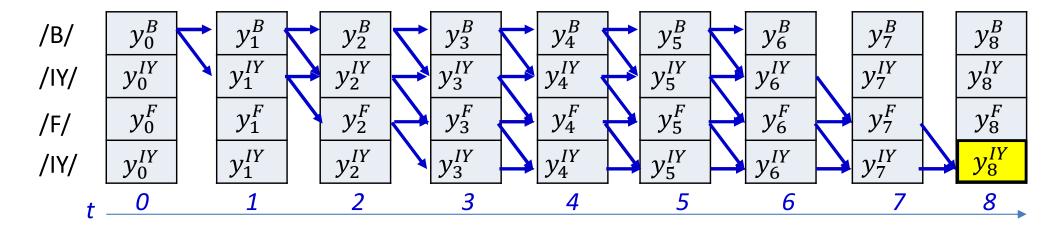
$$\hat{\alpha}(0,0) = 1, \quad \hat{\alpha}(0,r) = 0, \quad r > 0$$

$$\alpha(0,r) = \hat{\alpha}(0,r)y_0^{S(r)}, \quad 0 \le r \le K - 1$$

• for
$$t = 1 \dots T - 1$$

 $\hat{\alpha}(t,0) = \alpha(t-1,0)$
for $l = 1 \dots K - 1$
• $\hat{\alpha}(t,l) = \alpha(t-1,l) + \alpha(t-1,l-1)$
 $\alpha(t,r) = \hat{\alpha}(t,r)y_t^{S(r)}, \quad 0 \le r \le K-1$

The final forward probability $\alpha(t,r)$



$$\alpha(T-1,K-1) = P(S_0...S_{K-1}|X)$$

 The probability of the entire symbol sequence is the alpha at the bottom right node

SIMPLE FORWARD ALGORITHM

```
#N is the number of symbols in the target output
#S(i) is the ith symbol in target output
#y(t,i) is the output of the network for the ith symbol at time t
#T = length of input
#First create output table
For i = 1:N
    s(1:T,i) = v(1:T, S(i))
#The forward recursion
# First, at t = 1
alpha(1,1) = s(1,1)
alpha(1,2:N) = 0
for t = 2:T
    alpha(t,1) = alpha(t-1,1)*s(t,1)
    for i = 2:N
        alpha(t,i) = alpha(t-1,i-1) + alpha(t-1,i)
        alpha(t,i) *= s(t,i)
```

Can actually be done without explicitly composing the output table

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

SIMPLE FORWARD ALGORITHM

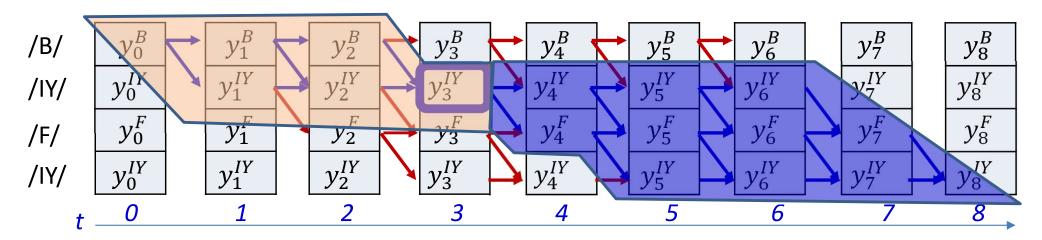
```
#N is the number of symbols in the target output
#S(i) is the ith symbol in target output
#y(t,i) is the network output for the ith symbol at time t
#T = length of input
```

#The forward recursion

```
# First, at t = 1
alpha(1,1) = y(1,S(1))
alpha(1,2:N) = 0
for t = 2:T
    alpha(t,1) = alpha(t-1,1)*y(t,S(1))
    for i = 2:N
        alpha(t,i) = alpha(t-1,i-1) + alpha(t-1,i)
        alpha(t,i) *= y(t,S(i))
```

Without explicitly composing the output table

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

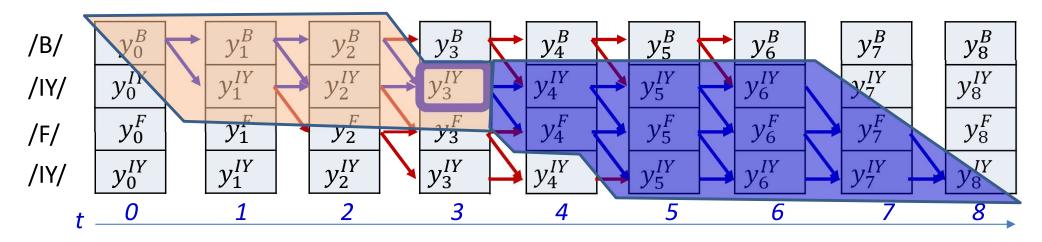


$$P(s_t = S_r, \mathbf{S} | \mathbf{X})$$

$$= P(S_0 \dots S_r, s_t = S_r | \mathbf{X}) P(s_{t+1} \in succ(S_r), succ(S_r), \dots, S_{K-1} | \mathbf{X})$$

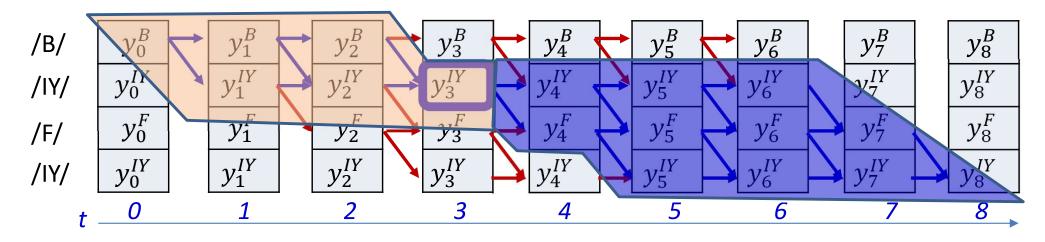
- We will call the first term the forward probability $\alpha(t,r)$
- We will call the note that the backward probability $\beta(t,r)$

We have seen how to compute this



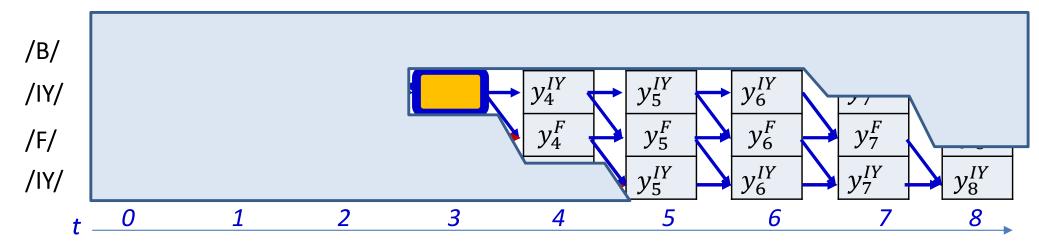
$$P(s_t = S_r, \mathbf{S} | \mathbf{X}) = \alpha(t, r) P(s_{t+1} \in succ(S_r), succ(S_r), \dots, S_{K-1} | \mathbf{X})$$

- We will call the first term the forward probability $\alpha(t,r)$
- We will call the sond term the *backward* probability $\beta(t,r)$

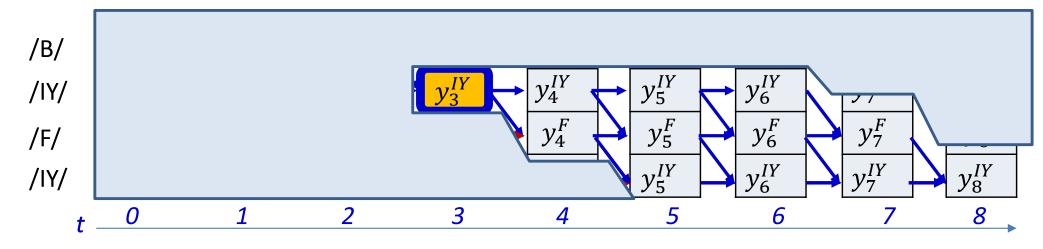


$$P(s_t = S_r, \mathbf{S} | \mathbf{X}) = \alpha(t, r) P(s_{t+1} \in succ(S_r), succ(S_r), \dots, S_{K-1} | \mathbf{X})$$

- We will call the first term the forward probability $\alpha(t,r)$
- We will call the second term the *backward* probability $\beta(t,r)$



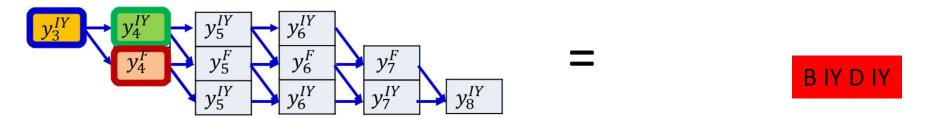
• $\beta(t,r)$ is the probability of the exposed subgraph, not including the orange shaded box

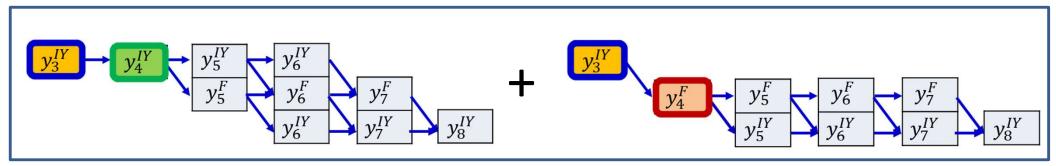


- $\beta(t,r)$ is the probability of the exposed subgraph, not including the orange shaded box
- For convenience, let us include the box in the graph, and factor it out later $\hat{\beta}(t,r)$ = probability of graph including node at (t,r)

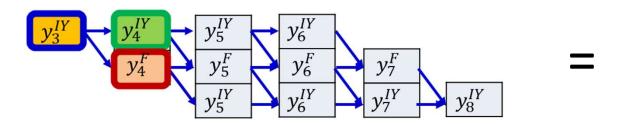
$$\beta(t,r) = \frac{1}{y_t^{S_r}} \hat{\beta}(t,r)$$

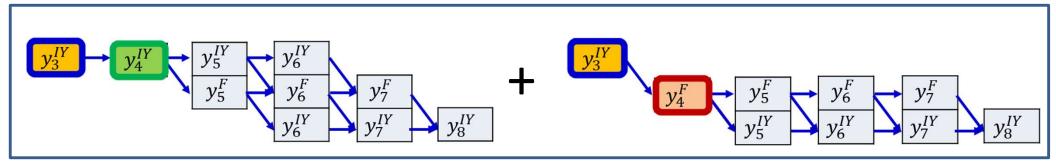
• We will develop an algorithm to compute $\hat{\beta}(t,r)$ and compute $\beta(t,r)$ from it by dividing out $y_t^{S_r}$ later





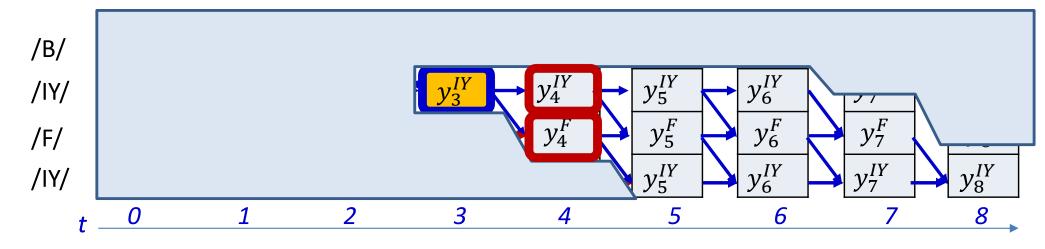
- Using the same logic as in the forward algorithm:
 - $\hat{\beta}(3,IY)$
 - = $y_3^{IY}P(subgraph starting at (4,IY)) + y_3^{IY}P(subgraph starting at (4,F))$





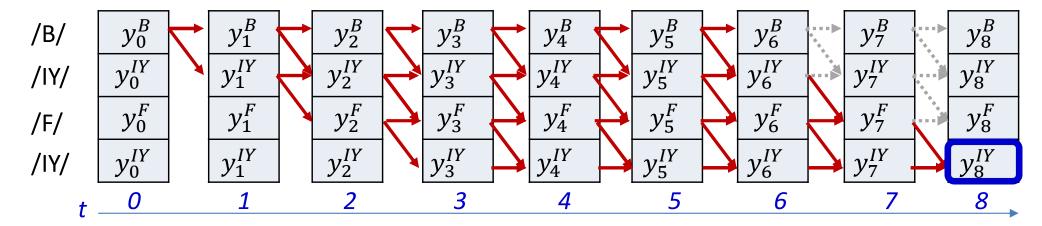
- Using the same logic as in the forward algorithm:
 - $\hat{\beta}(3,IY)$
 - = $y_3^{IY}P(subgraph starting at (4,IY)) + y_3^{IY}P(subgraph starting at (4,F))$
- We recognize these terms:

$$\hat{\beta}(3, IY) = y_3^{IY} \left(\hat{\beta}(3, IY) + \hat{\beta}(4, F) \right)$$



$$\hat{\beta}(t,r) = y_t^{S_r} \sum_{q \in succ(r)} \hat{\beta}(t+1,q)$$

- The $\hat{\beta}(t,r)$ is the total probability of the subgraph shown
 - Including the node at (t,r)
- The $\hat{\beta}(t,r)$ terms at any time t are defined recursively in terms of the $\hat{\beta}(t+1,q)$ terms at the next time

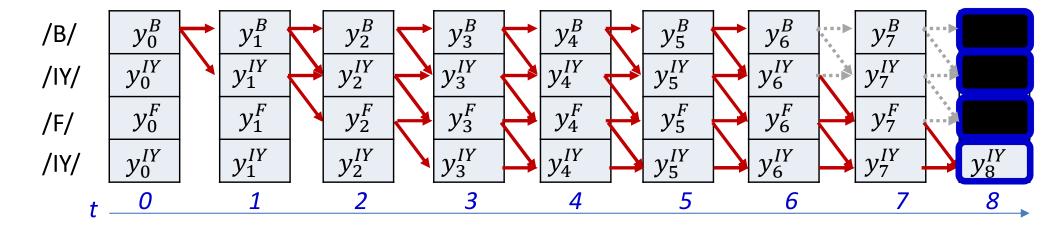


- Entire backward algorithm:
 - Note: some nodes (bottom row) have more successors than others
- Initialization:

$$\hat{\beta}(T-1,K-1) = y_{T-1}^{S(K-1)}, \ \hat{\beta}(T-1,r) = 0, \ r < K-1$$

• for t = T - 2 downto 0for $r = K - 1 \dots 0$

$$\hat{\beta}(t,r) = y_t^{S(r)} \sum_{q \in succ(r)} \hat{\beta}(t+1,q)$$

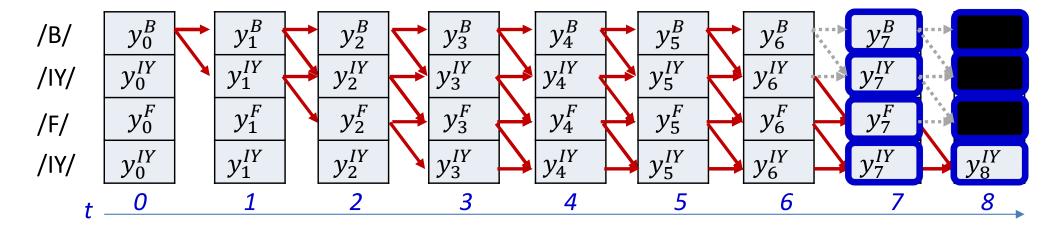


Initialization:

$$\hat{\beta}(T-1,K-1) = y_{T-1}^{S(K-1)}, \ \hat{\beta}(T-1,r) = 0, \ r < K-1$$

• for t = T - 2 downto 0for $r = K - 1 \dots 0$

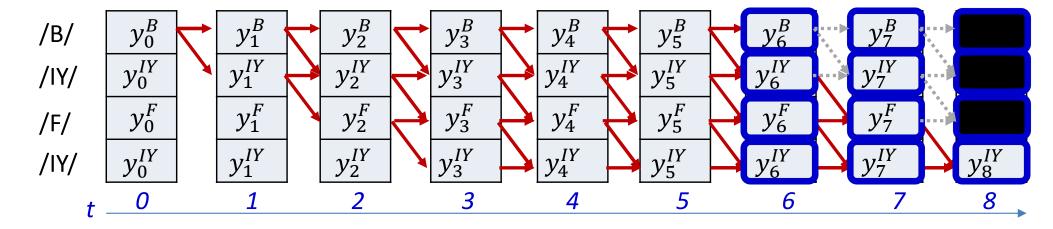
$$\hat{\beta}(t,r) = y_t^{S(r)} \sum_{q \in succ(r)} \hat{\beta}(t+1,q)$$



• Initialization:

$$\hat{\beta}(T-1,K-1) = y_{t+1}^{S(K-1)}, \hat{\beta}(T-1,r) = 0, r < K-1$$

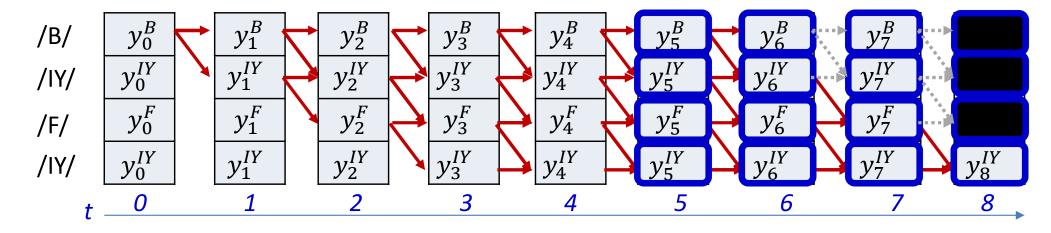
• for
$$t=T-2$$
 downto 0 for $r=K-1\dots 0$
$$\hat{\beta}(t,r)=y_t^{S(r)}\sum_{q\in succ(r)}\hat{\beta}(t+1,q)$$



Initialization:

$$\hat{\beta}(T-1,K-1) = y_{t+1}^{S(K-1)}, \hat{\beta}(T-1,r) = 0, r < K-1$$

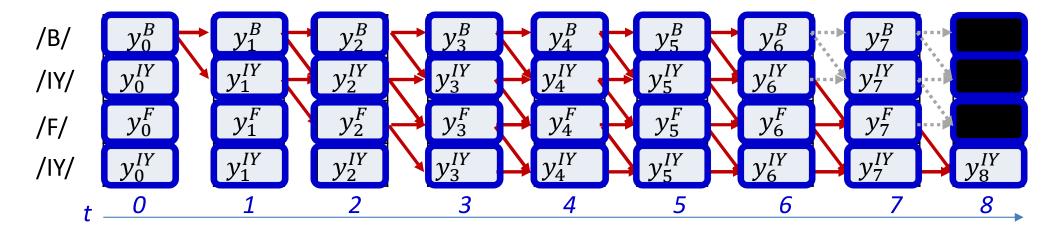
• for
$$t=T-2$$
 downto 0 for $r=K-1\dots 0$
$$\hat{\beta}(t,r)=y_t^{S(r)}\sum_{q\in succ(r)}\hat{\beta}(t+1,q)$$



• Initialization:

$$\hat{\beta}(T-1,K-1) = y_{t+1}^{S(K-1)}, \hat{\beta}(T-1,r) = 0, r < K-1$$

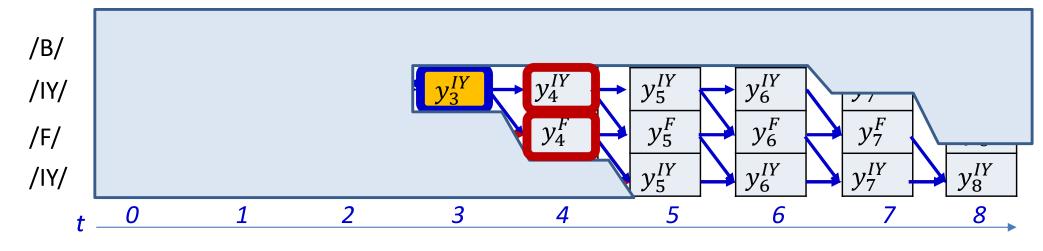
• for
$$t=T-2$$
 downto 0 for $r=K-1\dots 0$
$$\hat{\beta}(t,r)=y_t^{S(r)}\sum_{q\in succ(r)}\hat{\beta}(t+1,q)$$



• Initialization:

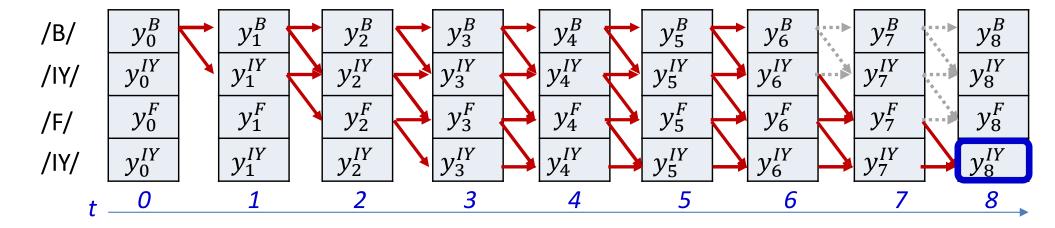
$$\hat{\beta}(T-1,K-1) = y_{t+1}^{S(K-1)}, \hat{\beta}(T-1,r) = 0, \ r < K-1$$

• for
$$t=T-2$$
 downto 0 for $r=K-1\dots 0$
$$\hat{\beta}(t,r)=y_t^{S(r)}\sum_{q\in succ(r)}\hat{\beta}(t+1,q)$$



- This recursion gives us $\hat{\beta}(t,r)$ which includes the node at (t,r)
- The actual backward probability is obtained as

$$\beta(t,r) = \frac{1}{y_t^{S_r}} \hat{\beta}(t,r)$$

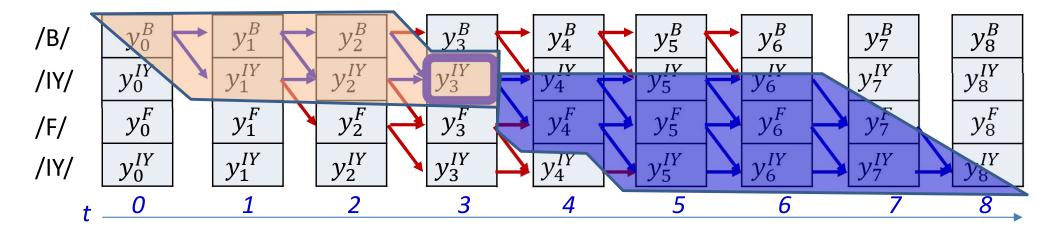


Initialization:

$$\hat{\beta}(T-1,K-1) = y_{T-1}^{S(K-1)}, \ \hat{\beta}(T-1,r) = 0, \ r < K-1$$

• for t = T - 2 downto 0for $r = K - 1 \dots 0$

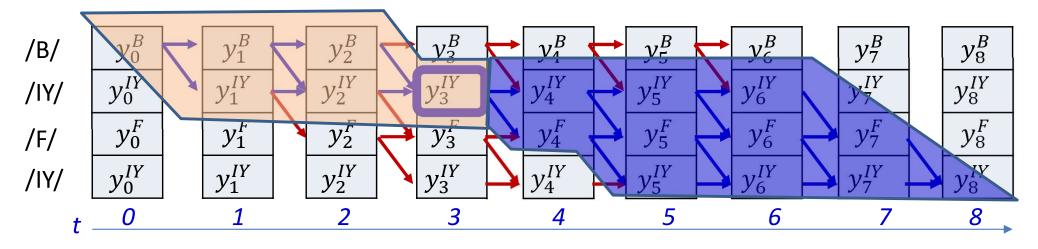
$$\hat{\beta}(t,r) = y_t^{S(r)} \sum_{q \in succ(r)} \hat{\beta}(t+1,q)$$
$$\beta(t,r) = \frac{1}{y_t^{S(r)}} \hat{\beta}(t,r)$$



$$P(s_t = S_r, \mathbf{S}|\mathbf{X}) = \alpha(t, r) \frac{P(blue\ graph)}{P(t)}$$

- We will call the first term the forward probability $\alpha(t,r)$
- We will call the second term the *backward* probability $\beta(t,r)$

The joint probability



$$P(s_t = S_r, \mathbf{S} | \mathbf{X}) = \alpha(t, r) \beta(t, r)$$

- We will call the first term the f and pre vility $\alpha(t,r)$
- We will call the second term th eta ackwar robability eta(t,r)

Forward algo

Backward algo

SIMPLE BACKWARD ALGORITHM

```
#N is the number of symbols in the target output
#S(i) is the ith symbol in target output
#y(t,i) is the output of the network for the ith symbol at time t
#T = length of input
#First create output table
For i = 1:N
    s(1:T,i) = v(1:T, S(i))
#The backward recursion to compute betahat
# First, at t = T
betahat (T, N) = s(T, N)
betahat(T,1:N-1) = 0
for t = T-1 downto 1
    betahat (t,N) = s(t,N) *betahat (t+1,N)
    for i = N-1 downto 1
          betahat(t,i) = s(t,i)*(betahat(t+1,i) + betahat(t+1,i+1))
#Compute beta from betahat
for t = T downto 1
    for i = N downto 1
        beta(t,i) = betahat(t,i)/s(t,i)
```

Can actually be done without explicitly composing the output table

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

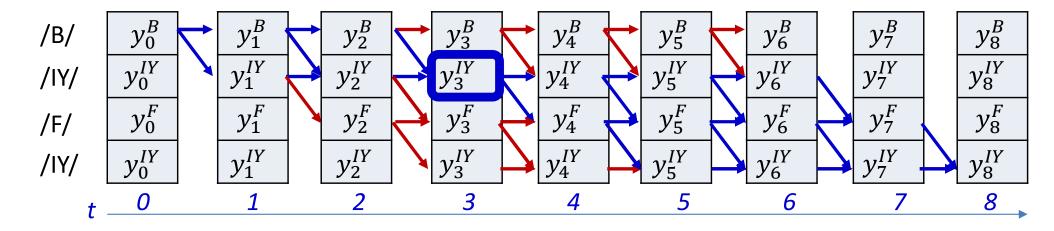
BACKWARD ALGORITHM

```
#N is the number of symbols in the target output
#S(i) is the ith symbol in target output
#y(t,i) is the output of the network for the ith symbol at time t
#T = length of input
#The backward recursion for betahat
# First, at t = T
betahat (T,N) = y(T,S(N))
betahat(T,1:N-1) = 0
for t = T-1 downto 1
    betahat (t,N) = v(t,S(N)) *betahat (t+1,N)
    for i = N-1 downto 1
          betahat(t,i) = v(t,S(i))*(betahat(t+1,i) + betahat(t+1,i+1))
#Compute beta from betahat
for t = T downto 1
    for i = N downto 1
        beta(t,i) = betahat(t,i)/v(t,S(i))
```

Without explicitly composing the output table

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

The posterior probability

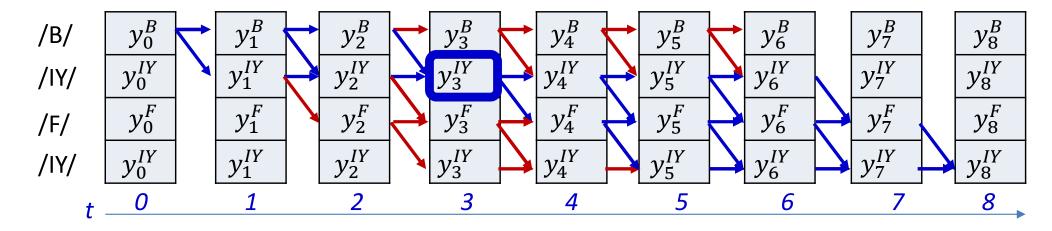


$$P(s_t = S_r, \mathbf{S}|\mathbf{X}) = \alpha(t, r)\beta(t, r)$$

The posterior is given by

$$P(s_t = S_r | \mathbf{S}, \mathbf{X}) = \frac{P(s_t = S_r, \mathbf{S} | \mathbf{X})}{\sum_{S_r'} P(s_t = S_r', \mathbf{S} | \mathbf{X})} = \frac{\alpha(t, r)\beta(t, r)}{\sum_{r'} \alpha(t, r')\beta(t, r')}$$

The posterior probability

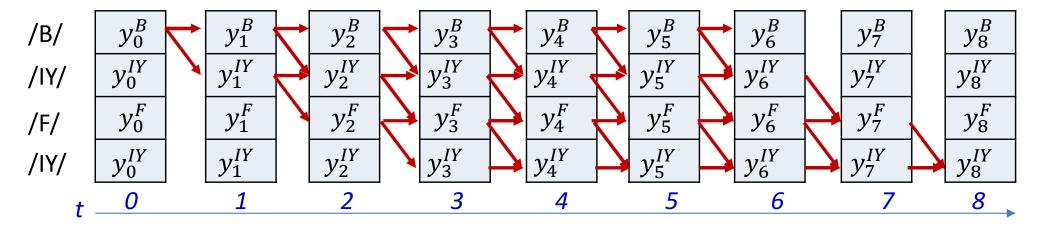


• Let the posterior $P(s_t = S_r | \mathbf{S}, \mathbf{X})$ be represented by $\gamma(t, r)$

$$\gamma(t,r) = \frac{\alpha(t,r)\beta(t,r)}{\sum_{r'} \alpha(t,r')\beta(t,r')}$$

COMPUTING POSTERIORS

```
#N is the number of symbols in the target output
#S(i) is the ith symbol in target output
#y(t,i) is the output of the network for the ith symbol at time t
#T = length of input
#Assuming the forward are completed first
alpha = forward(y, S) # forward probabilities computed
beta = backward(y, S) # backward probabilities computed
#Now compute the posteriors
for t = 1.T
    sumgamma(t) = 0
    for i = 1:N
        gamma(t,i) = alpha(t,i) * beta(t,i)
        sumgamma(t) += gamma(t,i)
    end
    for i=1:N
        gamma(t,i) = gamma(t,i) / sumgamma(t)
```



$$DIV = -\sum_{t} \sum_{s \in S_0 \dots S_{K-1}} P(s_t = s | \mathbf{S}, \mathbf{X}) \log Y(t, s_t = s)$$

$$DIV = -\sum_{t} \sum_{r} \gamma(t, r) \log y_t^{S(r)}$$

Poll 3 (@866)

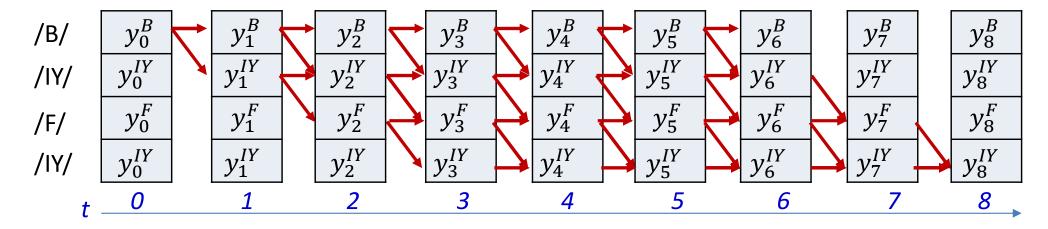
Select all that are true

- The forward-backward algorithm is used to compute the a posteriori probability of aligning each symbol in the compressed sequence to each input
- These probabilities are required to compute the expected divergence across all alignments of the compressed symbol sequence to the input

Poll 3

Select all that are true

- The forward-backward algorithm is used to compute the a posteriori probability of aligning each symbol in the compressed sequence to each input
- These probabilities are required to compute the expected divergence across all alignments of the compressed symbol sequence to the input

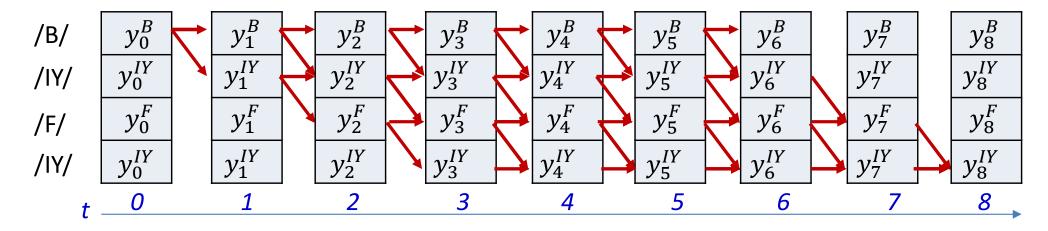


$$DIV = -\sum_{t} \sum_{s \in S_0 \dots S_{K-1}} P(s_t = s | \mathbf{S}, \mathbf{X}) \log Y(t, s_t = s)$$

$$DIV = -\sum_{t} \sum_{r} \gamma(t, r) \log y_t^{S(r)}$$

• The derivative of the divergence w.r.t the output Y_t of the net at any time:

$$\nabla_{Y_t} DIV = \begin{bmatrix} \frac{dDIV}{dy_t^{s_0}} & \frac{dDIV}{dy_t^{s_1}} & \dots & \frac{dDIV}{dy_t^{s_{L-1}}} \end{bmatrix}$$

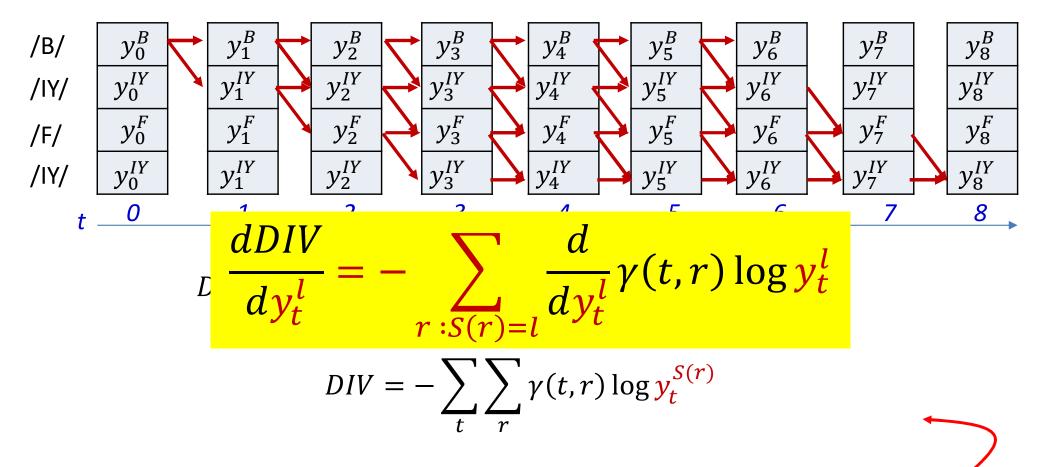


$$DIV = -\sum_{t} \sum_{s \in S_0 \dots S_{K-1}} P(s_t = s | \mathbf{S}, \mathbf{X}) \log Y(t, s_t = s)$$

$$DIV = -\sum_{t} \sum_{r} \gamma(t, r) \log y_t^{S(r)}$$

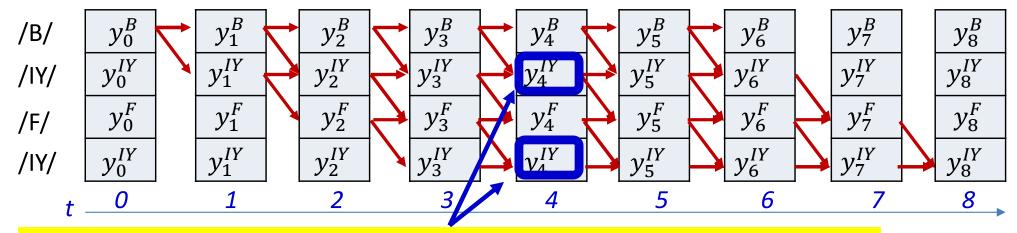
• The derivative of the divergence w.r.t the output Y_t of the net at any time:

$$\nabla_{Y_t} DIV = \begin{bmatrix} \frac{dDIV}{dy_t^{s_0}} \end{bmatrix} \underbrace{\frac{dDIV}{dy_t^{s_1}}} \dots \underbrace{\begin{bmatrix} \frac{dDIV}{dy_t^{s_1}} \end{bmatrix}}_{\text{from here}} \dots$$



• The derivative of the divergence w.r.t the output Y_t of the net at any time:

$$\nabla_{Y_t} DIV = \begin{bmatrix} \frac{dDIV}{dy_t^{s_0}} \end{bmatrix} \underbrace{\frac{dDIV}{dy_t^{s_1}}} \dots \underbrace{\begin{bmatrix} \frac{dDIV}{dy_t^{s_1}} \end{bmatrix}}_{\text{from here}} \dots$$

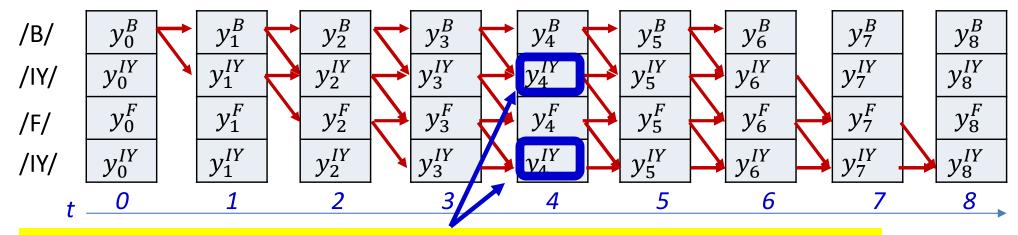


The derivatives at both these locations must be summed to get $\frac{dDIV}{dy_4^{IY}}$

$$\frac{dDIV}{dy_t^l} = -\sum_{r:S(r)=l} \frac{d}{dy_t^l} \gamma(t,r) \log y_t^l$$

• The derivative of the divergence w.r.t the output Y_t of the net at any time:

$$\nabla_{Y_t} DIV = \left[\frac{dDIV}{dy_t^{s_0}} \right) \frac{dDIV}{dy_t^{s_1}} \dots \left(\frac{dDIV}{dy_t^{s_{L-1}}} \right)$$

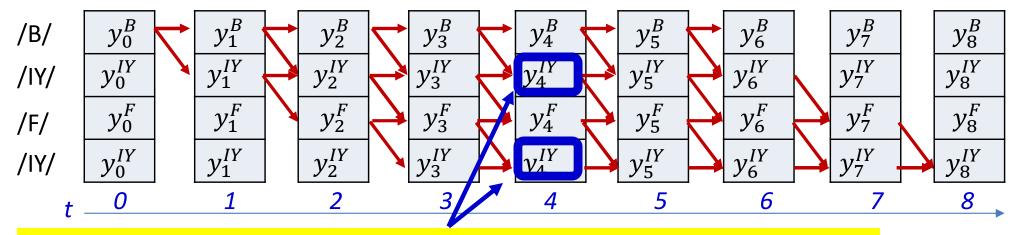


The derivatives at both these locations must be summed to get $\frac{dDIV}{dv_A^{IY}}$

$$\frac{dDIV}{dy_t^l} = -\sum_{r:S(r)=l} \frac{d}{dy_t^l} \gamma(t,r) \log y_t^l$$

• The derivative of the divergence w.r.t the output Y_t of the net at any time:

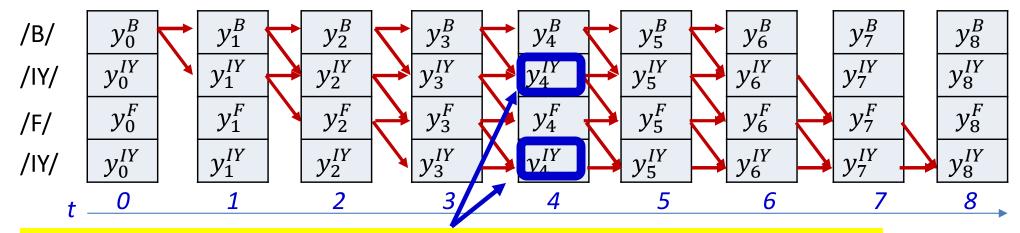
$$\nabla_{Y_t} DIV = \left[\frac{dDIV}{dy_t^{s_0}} \right) \frac{dDIV}{dy_t^{s_1}} \dots \left(\frac{dDIV}{dy_t^{s_{L-1}}} \right)$$



The derivatives at both these locations must be summed to get $\frac{dDIV}{dy_4^{IY}}$

$$\frac{dDIV}{dy_t^l} = -\sum_{r:S(r)=l} \frac{d}{dy_t^l} \gamma(t,r) \log y_t^l$$

$$\frac{d}{dy_t^l}\gamma(t,r)\log y_t^l = \frac{\gamma(t,r)}{y_t^l} + \frac{d\gamma(t,r)}{dy_t^l}\log y_t^l$$
 any time:



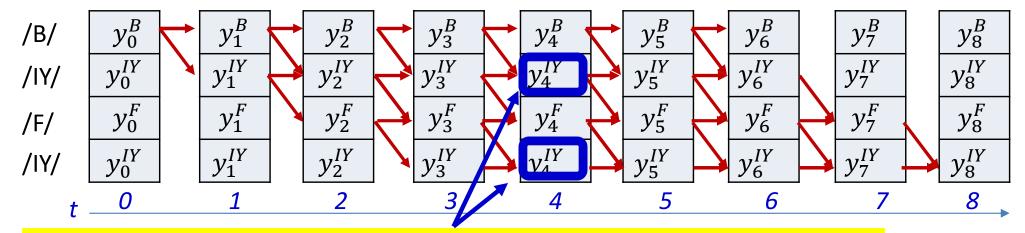
The derivatives at both these locations must be summed to get $\frac{dDIV}{dy_4^{IY}}$

$$\frac{dDIV}{dy_t^l} = -\sum_{r:S(r)=l} \frac{d}{dy_t^l} \gamma(t,r) \log y_t^l$$

• The derivative of t $\frac{d}{dy_t^l} \gamma(t,r) \log y_t^l \approx \frac{\gamma(t,r)}{y_t^l}$ net at any time:

The approximation is exact if we think of this as a maximum-likelihood estimate

Derivative of the expected divergence



The derivatives at both these locations must be summed to get $\frac{dDIV}{dy_4^{IY}}$

$$DIV = -\sum_{t} \sum_{r} \gamma(t, r) \log y_{t}^{S(r)}$$

 The derivative of the divergence w.r.t any particular output of the network must sum over all instances of that symbol in the target sequence

$$\frac{dDIV}{dy_t^l} = -\frac{1}{y_t^l} \sum_{r: S(r)=l} \gamma(t,r)$$

– E.g. the derivative w.r.t y_t^{IY} will sum over both rows representing /IY/ in the above figure

COMPUTING DERIVATIVES

```
#N is the number of symbols in the target output
#S(i) is the ith symbol in target output
#y(t,i) is the output of the network for the ith symbol at time t
#T = length of input
#Assuming the forward are completed first
alpha = forward(y, S) # forward probabilities computed
beta = backward(y, S) # backward probabilities computed
# Compute posteriors from alpha and beta
gamma = computeposteriors(alpha, beta)
#Compute derivatives
for t = 1:T
    dy(t,1:L) = 0 # Initialize all derivatives at time t to 0
    for i = 1:N
       dy(t,S(i)) = qamma(t,i) / y(t,S(i))
```

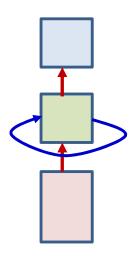
Overall training procedure for Seq2Seq case 1

/B/ /IY/ /F/ /IY/ *Y*₃ Y_0 Y_1 Y_2 Y_4 *Y*₅ *Y*₇ *Y*₈ *Y*₉ X_5 X_4 X_1 X_2 X_3 X_7 X_9 X_0

 Problem: Given input and output sequences without alignment, train models

Overall training procedure for Seq2Seq case 1

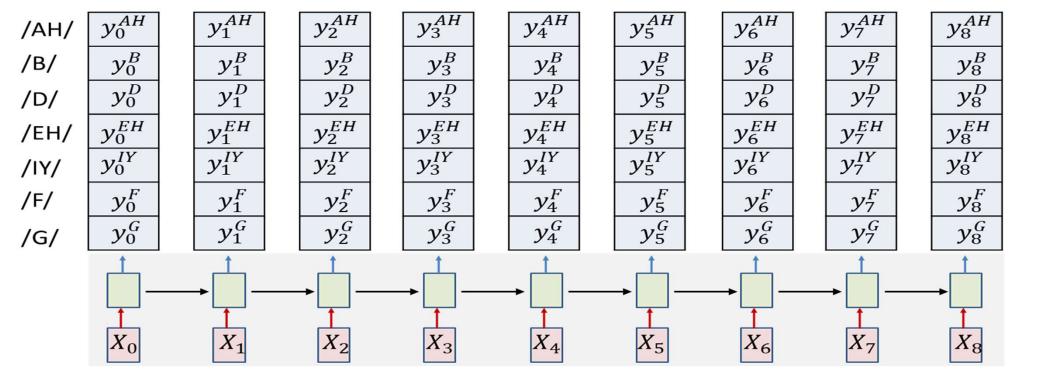
- **Step 1**: Setup the network
 - Typically many-layered LSTM



• Step 2: Initialize all parameters of the network

Overall Training: Forward pass

- Foreach training instance
 - Step 3: Forward pass. Pass the training instance through the network and obtain all symbol probabilities at each time



Overall training: Backward pass

 y_3^B y_4^B y_0^B y_1^B y_2^B y_6^B y_7^B /B/ y_5^B y_8^B y_1^{IY} y_2^{IY} y_3^{IY} y_5^{IY} y_6^{IY} y_7^{IY} y_0^{IY} y_4^{IY} y_8^{IY} /IY/ y_2^F y_6^F y_0^F y_1^F y_3^F y_7^F y_4^F y_5^F /F/ y_7^{IY} y_1^{IY} y_2^{IY} y_3^{IY} y_4^{IY} y_5^{IY} y_6^{IY} y_0^{IY} /IY/

/AH/ y_0^{AH}

 y_1^{AH}

 y_2^{AH}

 y_3^{AH}

 y_4^{AH}

 y_5^{AH}

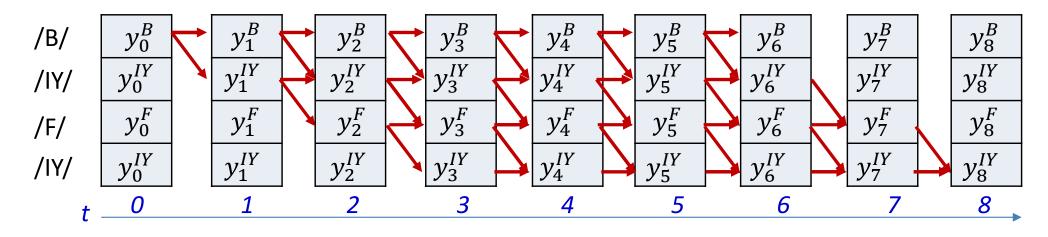
 y_6^{AH}

 y_7^{AH}

 y_8^{AH}

- Foreach training instance
 - Step 3: Forward pass. Pass the training instance through the network and obtain all symbol probabilities at each time
 - **Step 4:** Construct the graph representing the specific symbol sequence in the instance. This may require having multiple rows of nodes with the same symbol scores

Overall training: Backward pass



- Foreach training instance:
 - **Step 5:** Perform the forward backward algorithm to compute $\alpha(t,r)$ and $\beta(t,r)$ at each time, for each row of nodes in the graph. Compute $\gamma(t,r)$.
 - **Step 6:** Compute derivative of divergence $\nabla_{Y_t}DIV$ for each Y_t

Overall training: Backward pass

- Foreach instance
 - Step 6: Compute derivative of divergence $\nabla_{Y_t}DIV$ for each Y_t

$$\nabla_{Y_t} DIV = \begin{bmatrix} \frac{dDIV}{dy_t^0} & \frac{dDIV}{dy_t^1} & \dots & \frac{dDIV}{dy_t^{L-1}} \end{bmatrix}$$

$$\frac{dDIV}{dy_t^l} = -\sum_{r:S(r)=l} \frac{\gamma(t,r)}{y_t^l}$$

• Step 7: Backpropagate $\frac{dDIV}{dy_t^l}$ and aggregate derivatives over minibatch and update parameters

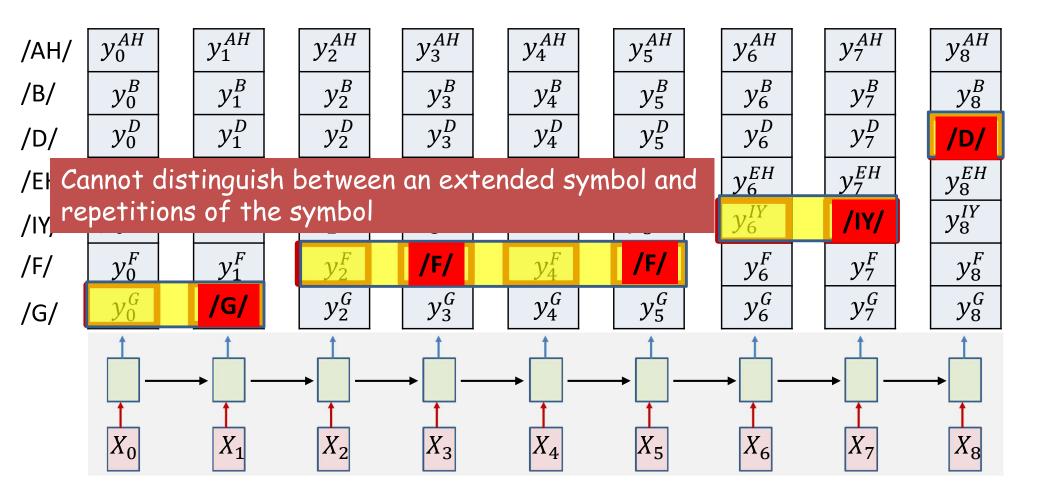
Story so far: CTC models

- Sequence-to-sequence networks which irregularly output symbols can be "decoded" by Viterbi decoding
 - Which assumes that a symbol is output at each time and merges adjacent symbols
- They require alignment of the output to the symbol sequence for training
 - This alignment is generally not given
- Training can be performed by iteratively estimating the alignment by Viterbi-decoding and time-synchronous training
- Alternately, it can be performed by optimizing the expected error over all possible alignments
 - Posterior probabilities for the expectation can be computed using the forward backward algorithm

A key decoding problem

- Consider a problem where the output symbols are characters
- We have a decode: RRREEEED
- Is this the compressed symbol sequence RED or REED?

We've seen this before



/G//F//F//IY//D/ or /G//F//IY//D/?

A key decoding problem

- We have a decode: RRREEEED
- Is this the symbol sequence RED or REED?
- Solution: Introduce an explicit extra symbol which serves to separate discrete versions of a symbol
 - A "blank" (represented by "-")
 - RRR---EE---DDD = RED
 - RR-E--EED = REED
 - RR-R---EE---D-DD = RREDD
 - R-R-R---E-EDD-DDDD-D =
 - The next symbol at the end of a sequence of blanks is always a new character
 - When a symbol repeats, there must be at least one blank between the repetitions
- The symbol set recognized by the network must now include the extra blank symbol
 - Which too must be trained

A key decoding problem

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Poll 4 (@867)

Which of the following are valid expansions of the character string "BILLY"?

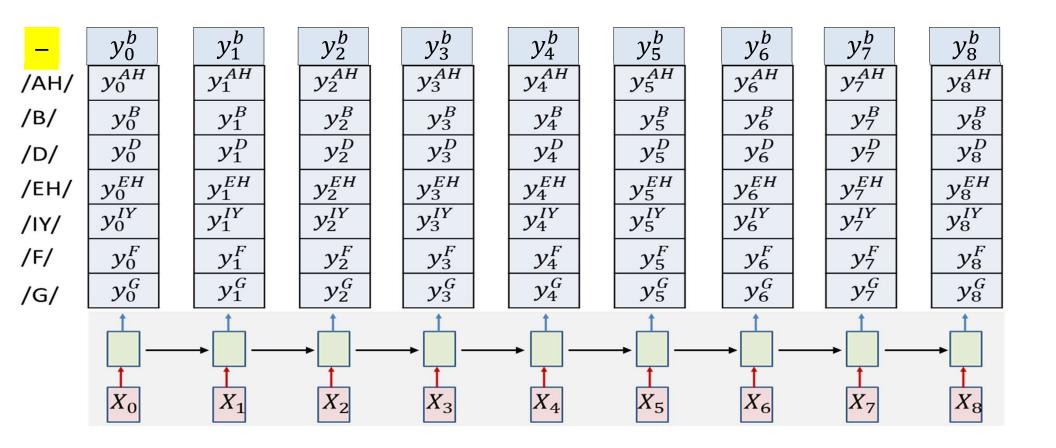
- BBIILLY
- B-BIL-LY
- B-I-LLY
- \bullet B-I-L-LYY

Poll 4

Which of the following are valid expansions of the character string "BILLY"?

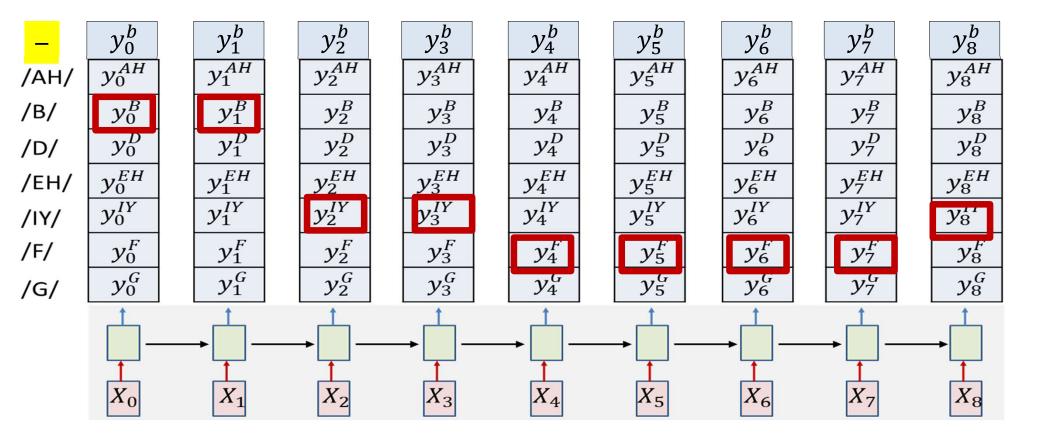
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Note the extra "blank" at the output

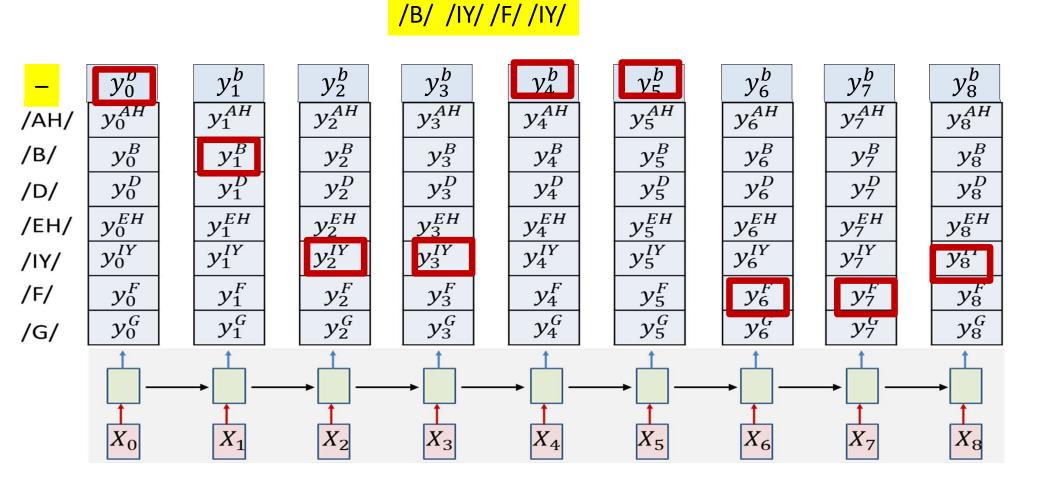


Note the extra "blank" at the output

/B/ /IY/ /F/ /IY/

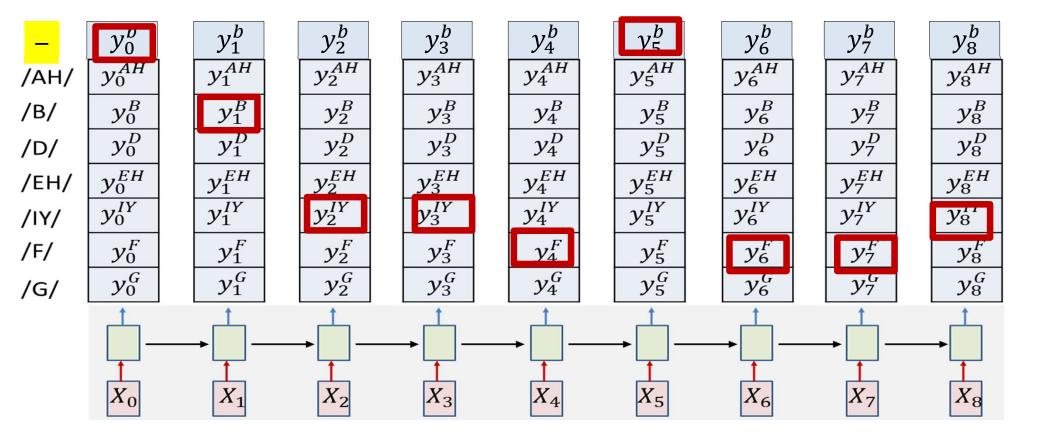


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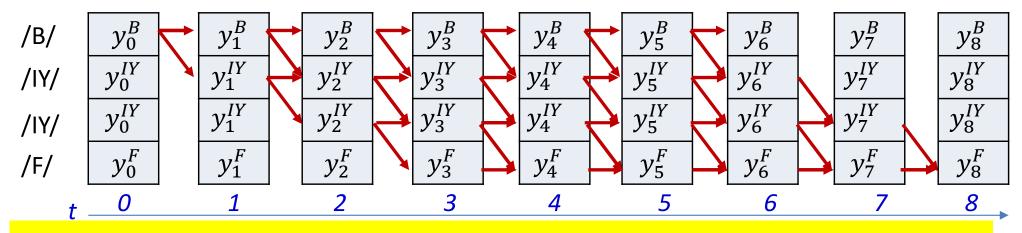


Note the extra "blank" at the output

/B/ /IY/ /F/ /F/ /IY/



Composing the graph for training



- The original method without blanks
- Changing the example to /B/ /IY/ /IY/ /F/ from /B/ /IY/ /F/ /IY/ for illustration

How blanks change the graph

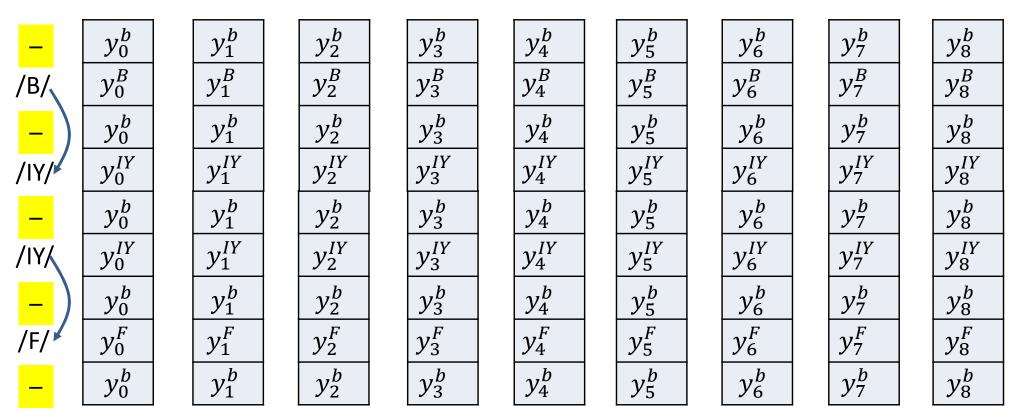
$$/B/ \longrightarrow /IY/ \longrightarrow /F/ \longrightarrow /IY/$$

 Regular order: Each symbol must be followed by the next one



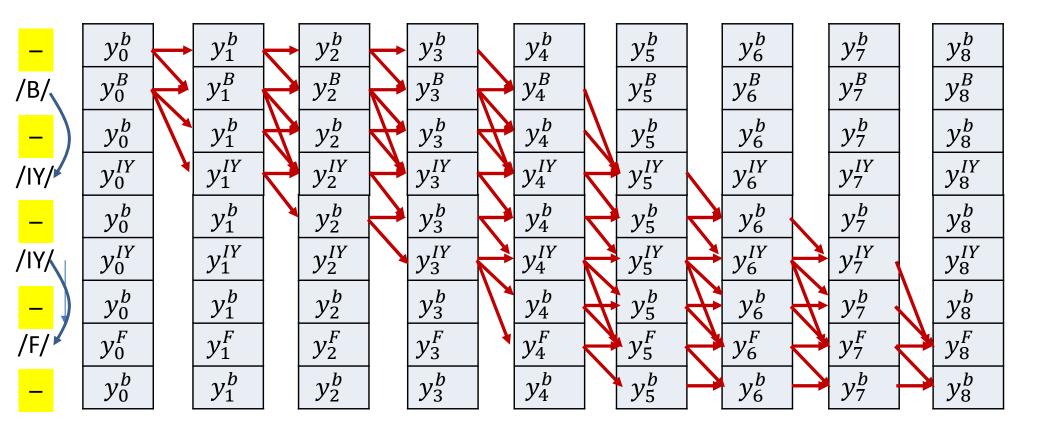
- New pattern: Each symbol may optionally be followed by a blank (explicitly shown)
- Unless the next symbol is the same
 - E.g. /IY/ /IY/
 - In this case an intermediate black is mandatory
 - Blanks may also occur in the first and last positions

Composing the graph for training



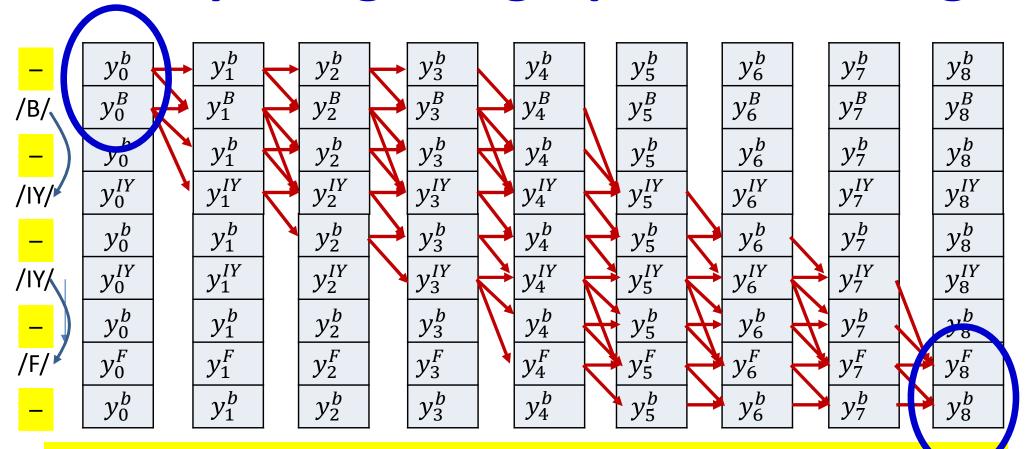
- With blanks
- Follows the graph we just saw
 - Note: a row of blanks between any two symbols
 - Also blanks at the very beginning and the very end

Composing the graph for training



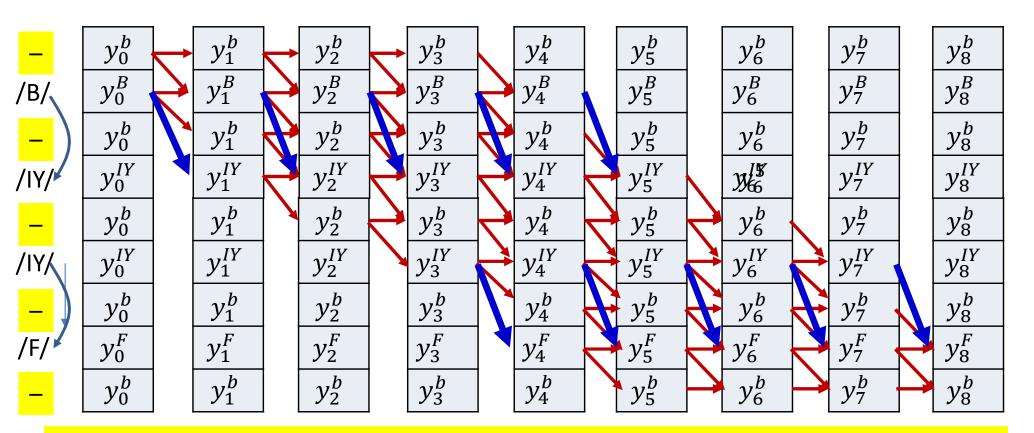
- Add edges such that all paths from initial node(s) to final node(s) unambiguously represent the target symbol sequence
- If there is an edge on the left graph, there is a corresponding arrow between columns

Composing the graph for training



 The first and last column are allowed to also end at initial and final blanks

Composing the graph for training



- The first and last column are allowed to also end at initial and final blanks
- Skips are permitted across a blank, but only if the symbols on either side are different
 - Because a blank is *mandatory between repetitions of a symbol* but *not required between distinct symbols*

Composing the graph

```
#N is the number of symbols in the target output
#S(i) is the ith symbol in target output
#Compose an extended symbol sequence Sext from S, that has the blanks
#in the appropriate place
#Also keep track of whether an extended symbol Sext(j) is allowed to
connect
#directly to Sext(j-2) (instead of only to Sext(j-1)) or not
function [Sext] = extendedsequencewithblanks(S)
    i = 1
    for i = 1:N
        Sext(j) = b' # blank
        i = i+1
        Sext(i) = S(i)
        i = i+1
    end
    Sext(j) = b'
    return Sext
```

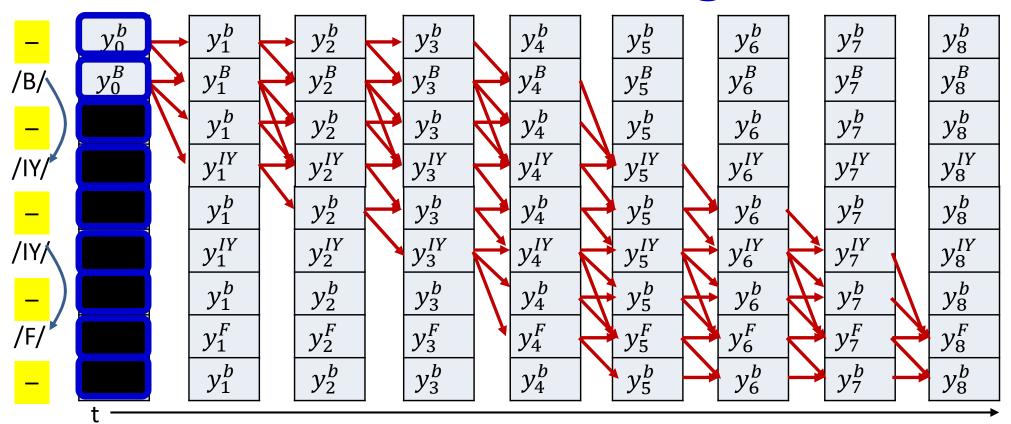
Example of using blanks for alignment: Viterbi alignment with blanks

MODIFIED VITERBI ALIGNMENT WITH BLANKS

```
[Sext] = extendedsequencewithblanks(S)
N = length(Sext) # length of extended sequence
# Viterbi starts here
                                  Without explicit construction of output table
BP(1,1) = -1
Bscr(1,1) = y(1, Sext(1)) # Blank
Bscr(1,2) = y(1, Sext(2))
Bscr(1,2:N) = -infty
for t = 2:T
    BP(t,1) = BP(t-1,1);
    Bscr(t,1) = Bscr(t-1,1)*y(t, Sext(1))
    for i = 2:N
        if (i > 2 \&\& Sext(i) != Sext(i-2))
           BP(t,i) = argmax i(Bscr(t-1,i), Bscr(t-1,i-1), Bscr(t-1,i-2))
        else
           BP(t,i) = argmax i(Bscr(t-1,i), Bscr(t-1,i-1))
        Bscr(t,i) = Bscr(t-1,BP(t,i))*y(t,Sext(i))
# Backtrace
AlignedSymbol(T) = Bscr(T,N) > Bscr(T,N-1) ? N, N-1;
for t = T downto 1
    AlignedSymbol(t-1) = BP(t,AlignedSymbol(t))
```

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

Modified Forward Algorithm

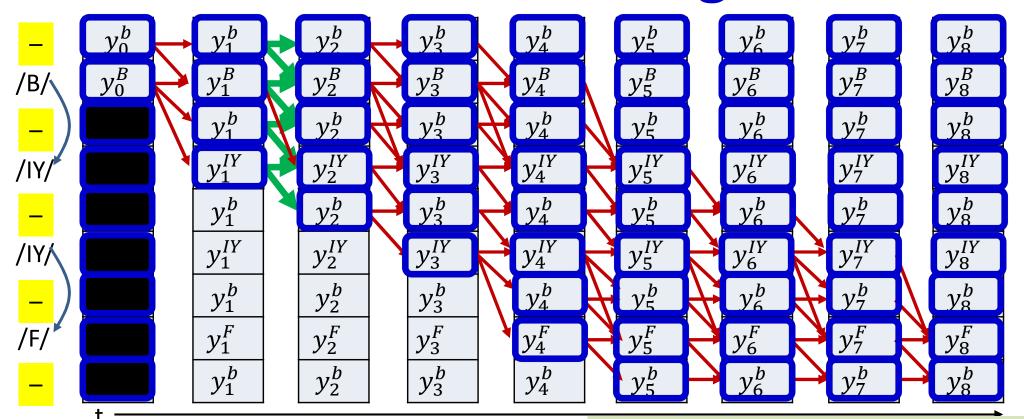


Initialization:

$$-\alpha(0,0) = y_0^b, \alpha(0,1) = y_0^{S(1)}, \alpha(0,r) = 0 \quad r > 1$$

S(k) refers to the *extended* sequence with blanks included

Modified Forward Algorithm

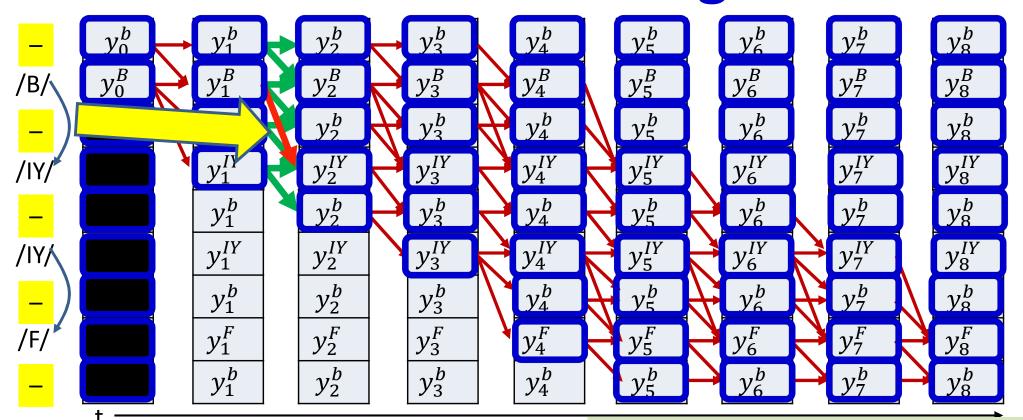


• Iteration t = 1:N:

$$\alpha(t,r) = \alpha(t-1,r) + \alpha(t-1,r-1)$$

$$\alpha(t,r) = Y_t^{S(r)} \sum_{q: S_q \in pred(S_r)} \alpha(t-1,q)$$

Modified Forward Algorithm



• Iteration t = 1:N:

$$\alpha(t,r) = \alpha(t-1,r) + \alpha(t-1,r-1)$$

• If $S(r) \neq S(r-2)$

$$\alpha(t,r) += \alpha(t-1,r-2)$$

$$\alpha(t,r) *= y_t^{S(r)}$$

 $\alpha(t,r) = Y_t^{S(r)}$ $\alpha(t-1,q)$

 $q:S_q \in \overline{pred}(S_r)$

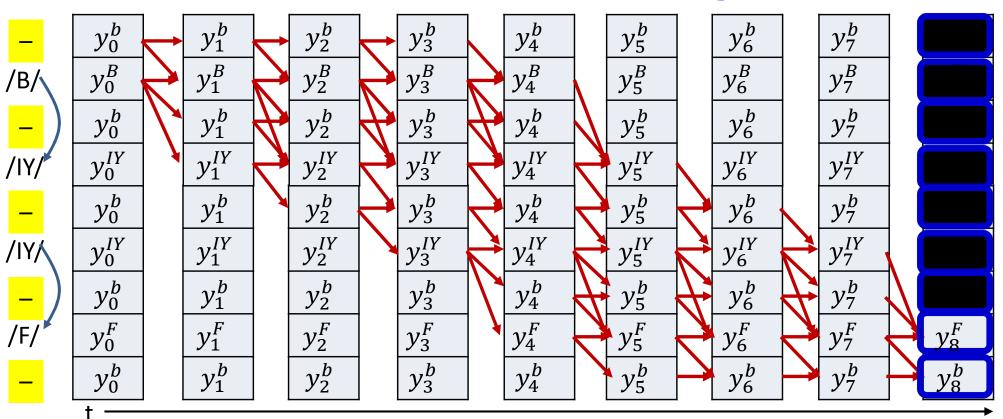
FORWARD ALGORITHM (with blanks)

[Sext] = extendedsequencewithblanks(S) N = length(Sext) # Length of extended sequence #The forward recursion # First, at t = 1alpha(1,1) = y(1,Sext(1)) #This is the blank alpha(1,2) = y(1, Sext(2))alpha(1, 3:N) = 0for t = 2:Talpha(t,1) = alpha(t-1,1)*y(t,Sext(1))for i = 2:Nalpha(t,i) = alpha(t-1,i) + alpha(t-1,i-1)if (i > 2 && Sext(i) != Sext(i-2))alpha(t,i) += alpha(t-1,i-2)alpha(t,i) *= v(t,Sext(i))

Without explicitly composing the output table

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

Modified Backward Algorithm

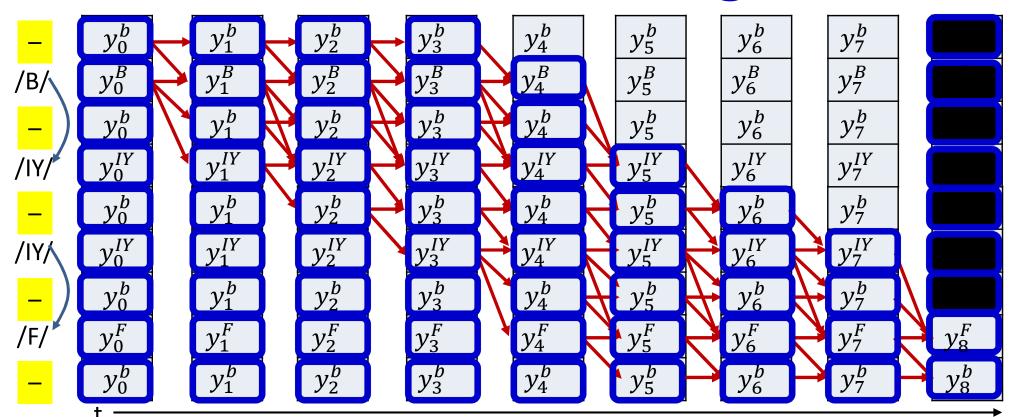


• Initialization:

$$\hat{\beta}(T-1,2K-1) = y_{T-1}^b; \hat{\beta}(T-1,2K-2) = y_{T-1}^{S(2K-1)}$$
$$\hat{\beta}(T-1,r) = 0 \quad r < 2K-2$$

S(k) refers to the extended sequence with blanks included

Modified Backward Algorithm



• Iteration:

$$\hat{\beta}(t,r) = \hat{\beta}(t+1,r) + \hat{\beta}(t+1,r+1)$$
• If $S(r) \neq S(r+2)$

$$\hat{\beta}(t,r) += \hat{\beta}(t+1,r+2)$$

$$\hat{\beta}(t,r) *= y_t^{S(r)}$$

•
$$\beta(t,r) = \hat{\beta}(t,r)/y_t^{S(r)}$$

$$\hat{\beta}(t,r) = y_t^{S_r} \sum_{q: S_q \in succ(S_r)} \hat{\beta}(t+1,q)$$

BACKWARD ALGORITHM WITH BLANKS

```
[Sext] = extendedsequencewithblanks(S)
N = length(Sext) # Length of extended sequence
#The backward recursion
# First, at t = T
betahat (T,N) = y(T, Sext(N))
betahat (T, N-1) = y(T, Sext(N-1))
betahat (T, 1:N-2) = 0
for t = T-1 downto 1
    betahat (t,N) = betahat (t+1,N) *y (t, Sext (N))
    for i = N-1 downto 1
        betahat(t,i) = betahat(t+1,i) + betahat(t+1,i+1))
        if (i \le N-2 \&\& Sext(i) != Sext(i+2))
            betahat(t,i) += betahat(t+1,i+2)
        betahat(t,i) *= y(t, Sext(i))
#Compute beta from betahat
for t = T downto 1
    for i = N downto 1
        beta(t,i) = betahat(t,i)/y(t, Sext(i))
```

Without explicitly composing the output table

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

The rest of the computation

Posteriors and derivatives are computed exactly as before

But using the extended graphs with blanks

COMPUTING POSTERIORS

```
[Sext, skipconnect] = extendedsequencewithblanks(S)
N = length(Sext) # Length of extended sequence
#Assuming the forward are completed first
alpha = forward(y, Sext) # forward probabilities computed
beta = backward(y, Sext) # backward probabilities computed
#Now compute the posteriors
for t = 1:T
    sumgamma(t) = 0
    for i = 1:N
        gamma(t,i) = alpha(t,i) * beta(t,i)
        sumgamma(t) += gamma(t, i)
    end
    for i=1:N
        gamma(t,i) = gamma(t,i) / sumgamma(t)
```

COMPUTING DERIVATIVES

```
[Sext, skipconnect] = extendedsequencewithblanks(S)
N = length(Sext) # Length of extended sequence
#Assuming the forward are completed first
alpha = forward(y, Sext) # forward probabilities computed
beta = backward(y, Sext) # backward probabilities computed
# Compute posteriors from alpha and beta
qamma = computeposteriors(alpha, beta)
#Compute derivatives
for t = 1:T
    dy(t,1:L) = 0 #Initialize all derivatives at time t to 0
    for i = 1:N
        dy(t, Sext(i)) = gamma(t, i) / y(t, Sext(i))
```

Using 1..N and 1..T indexing, instead of 0..N-1, 0..T-1, for convenience of notation

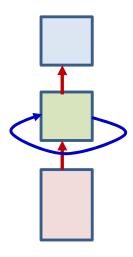
Overall training procedure for Seq2Seq with blanks

/B/ /IY/ /F/ /IY/ *Y*₃ Y_0 Y_1 Y_2 Y_4 *Y*₅ *Y*₈ *Y*₉ X_4 X_1 X_2 X_3 X_5 X_7 X_9 X_0

 Problem: Given input and output sequences without alignment, train models

Overall training procedure

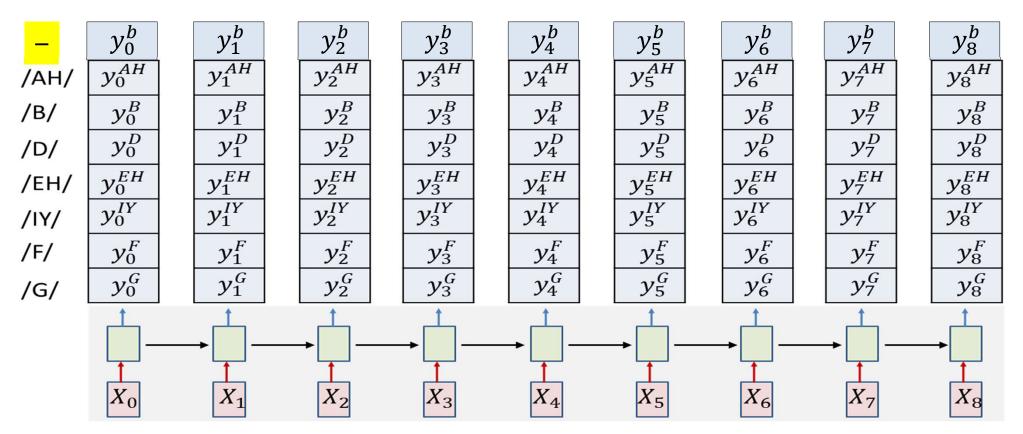
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 - Typically many-layered LSTM



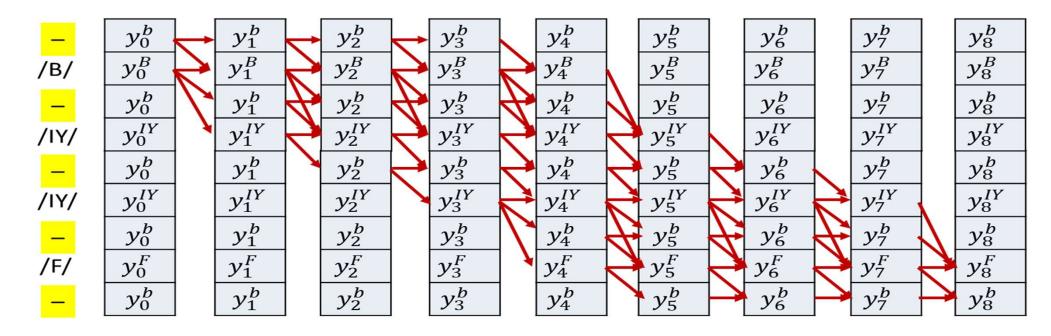
- Step 2: Initialize all parameters of the network
 - Include a "blank" symbol in vocabulary

Overall Training: Forward pass

- Foreach training instance
 - Step 3: Forward pass. Pass the training instance through the network and obtain all symbol probabilities at each time, including blanks

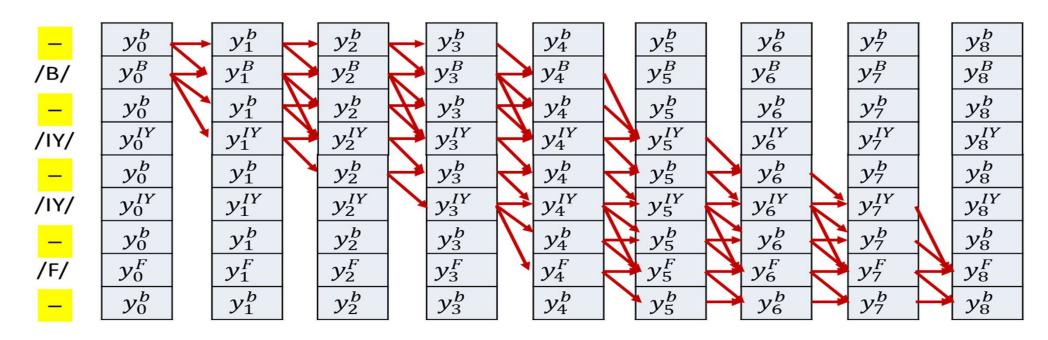


Overall training: Backward pass



- Foreach training instance
 - Step 3: Forward pass. Pass the training instance through the network and obtain all symbol probabilities at each time
 - **Step 4:** Construct the graph representing the specific symbol sequence in the instance. Use appropriate connections if blanks are included

Overall training: Backward pass



- Foreach training instance:
 - **Step 5:** Perform the forward backward algorithm to compute $\alpha(t,r)$ and $\beta(t,r)$ at each time, for each row of nodes in the graph using the modified forward-backward equations. Compute a posteriori probabilities $\gamma(t,r)$ from them
 - Step 6: Compute derivative of divergence $\nabla_{Y_t}DIV$ for each Y_t

Overall training: Backward pass

- Foreach instance
 - Step 6: Compute derivative of divergence $\nabla_{Y_t}DIV$ for each Y_t

$$\nabla_{Y_t} DIV = \begin{bmatrix} \frac{dDIV}{dy_t^0} & \frac{dDIV}{dy_t^1} & \dots & \frac{dDIV}{dy_t^{L-1}} \end{bmatrix}$$

$$\frac{dDIV}{dy_t^l} = -\sum_{r:S(r)=l} \frac{\gamma(t,r)}{y_t^{S(r)}}$$

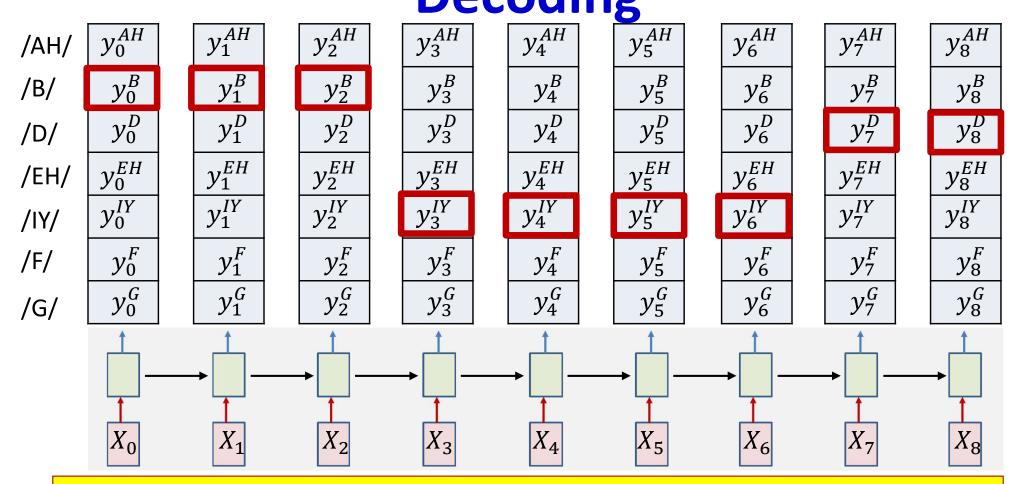
• Step 7: Backpropagate $\frac{dDIV}{dy_t^l}$ and aggregate derivatives over minibatch and update parameters

CTC: Connectionist Temporal Classification

 The overall framework we saw is referred to as CTC

 Applies to models that output order-aligned, but time-asynchronous outputs

Returning to an old problem: Decoding



- The greedy decode computes its output by finding the most likely symbol at each time and merging repetitions in the sequence
- This is in fact a *suboptimal* decode that actually finds the most likely *time-synchronous* output sequence
 - Which is not necessarily the most likely order-synchronous sequence

Greedy decodes are suboptimal

Consider the following candidate decodes

```
RR-EED (RED, 0.7)
RR-ED (RED, 0.68)
RREEED (RED, 0.69)
TTEEED (TED, 0.71)
TT-EED (TED, 0.3)
TT-ED (TED, 0.29)
```

- A greedy decode picks the most likely output: TED
- A decode that considers the sum of all alignments of the same final output will select RED
- Which is more reasonable?

Greedy decodes are suboptimal

Consider the following candidate decodes

```
RR-EED (RED, 0.7)
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TT-ED (TED, 0.29)
```

- A greedy decode picks the most likely output: TED
- A decode that considers the sum of all alignments of the same final output will select RED
- Which is more reasonable?
- And yet, remarkably, greedy decoding can be surprisingly effective, when using decoding with blanks

What a CTC system outputs

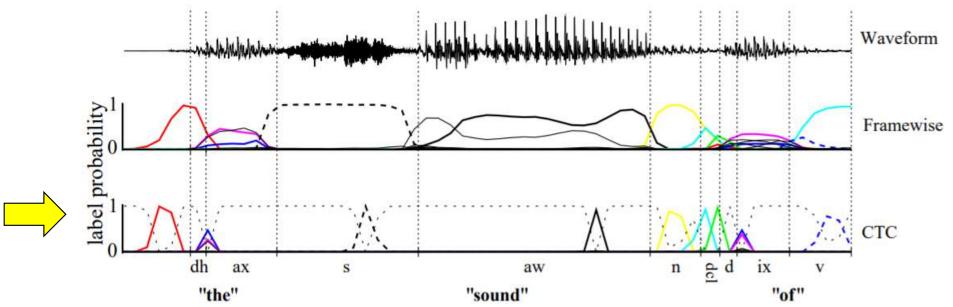


Figure 1. Framewise and CTC networks classifying a speech signal. The shaded lines are the output activations, corresponding to the probabilities of observing phonemes at particular times. The CTC network predicts only the sequence of phonemes (typically as a series of spikes, separated by 'blanks', or null predictions), while the framewise network attempts to align them with the manual segmentation (vertical lines). The framewise network receives an error for misaligning the segment boundaries, even if it predicts the correct phoneme (e.g. 'dh'). When one phoneme always occurs beside another (e.g. the closure 'dcl' with the stop 'd'), CTC tends to predict them together in a double spike. The choice of labelling can be read directly from the CTC outputs (follow the spikes), whereas the predictions of the framewise network must be post-processed before use.

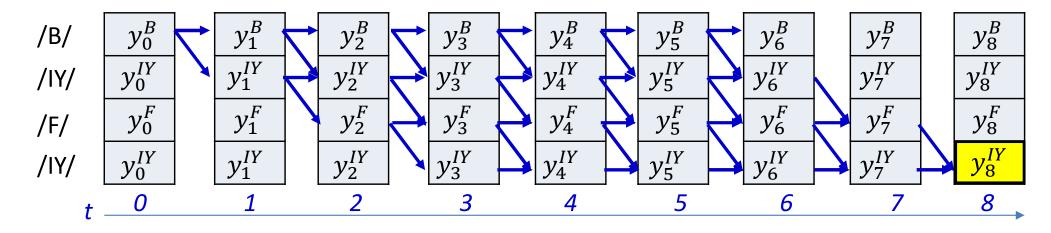
- Ref: Graves
- Symbol outputs peak at the ends of the sounds
 - Typical output: -- R --- E --- D
 - Model output naturally eliminates alignment ambiguities
- But this is still suboptimal..

Actual objective of decoding

- Want to find most likely order-aligned symbol sequence
 - RED
 - What greedy decode finds: most likely time synchronous symbol sequence
 - -/R//R/--/EH//EH//D/
 - Which must be compressed
- Find the order-aligned symbol sequence $S = S_0, \dots, S_{K-1}$, given an input $X = X_0, \dots, X_{T-1}$, that is most likely

$$= \underset{S}{\operatorname{argmax}} P(S_0, \dots, S_{K-1} | X)$$

Recall: The forward probability $\alpha(t,r)$



$$\alpha_{S_0..S_{K-1}}(T-1,K-1) = P(S_0..S_{K-1}|\mathbf{X})$$

 The probability of the entire symbol sequence is the alpha at the bottom right node

Actual decoding objective

Find the most likely (asynchronous) symbol sequence

$$\hat{\mathbf{S}} = \underset{\mathbf{S}}{\operatorname{argmax}} \alpha_{\mathbf{S}}(S_{K-1}, T-1)$$

Poll 5 (@868, @869)

The actual objective of decoding is to identify the compressed/unaligned sequence that has the highest probability given the input

- True
- False

This is the same as finding the compressed sequence with the highest forward probability (alpha) for aligning the final symbol in the sequence to the final input

- True
- False

Poll 5

The actual objective of decoding is to identify the compressed/unaligned sequence that has the highest probability given the input

- True
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This is the same as finding the compressed sequence with the highest forward probability (alpha) for aligning the final symbol in the sequence to the final input

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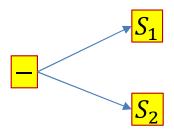
Actual decoding objective

Find the most likely (asynchronous) symbol sequence

$$\hat{\mathbf{S}} = \underset{\mathbf{S}}{\operatorname{argmax}} \alpha_{\mathbf{S}}(S_{K-1}, T-1)$$

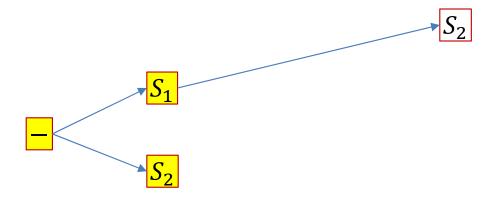
- Unfortunately, explicit computation of this will require evaluate of an exponential number of symbol sequences
- Solution: Organize all possible symbol sequences as a (semi)tree

Highlighted boxes represent possible symbols for first frame

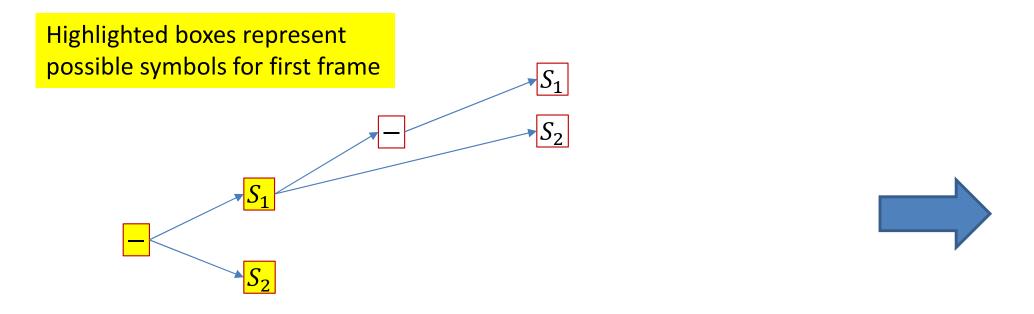


- The semi tree of hypotheses (assuming only 3 symbols in the vocabulary)
- Every symbol connects to every symbol other than itself
 - It also connects to a blank, which connects to every symbol including itself
- The simple structure repeats recursively
- Each node represents a unique (partial) symbol sequence!

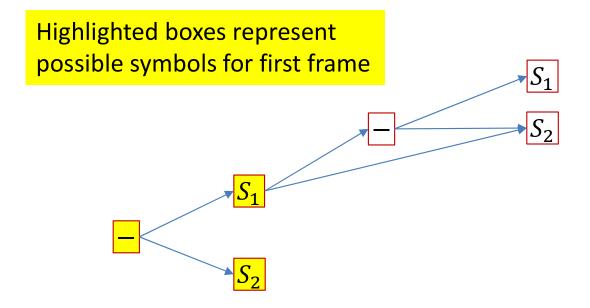
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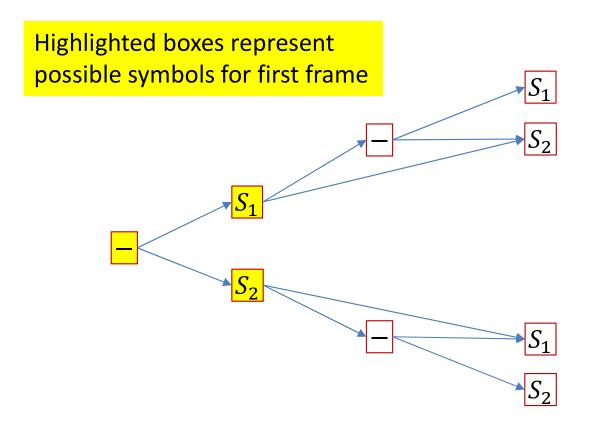
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- Every symbol connects to every symbol other than itself
 - It also connects to a blank, which connects to every symbol including itself
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- Each node represents a unique (partial) symbol sequence!



- The semi tree of hypotheses (assuming only 3 symbols in the vocabulary)
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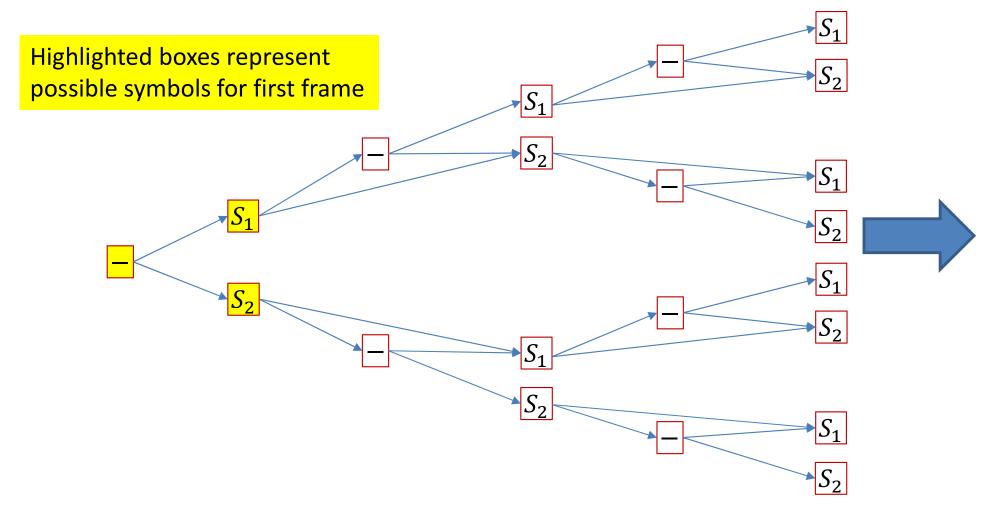


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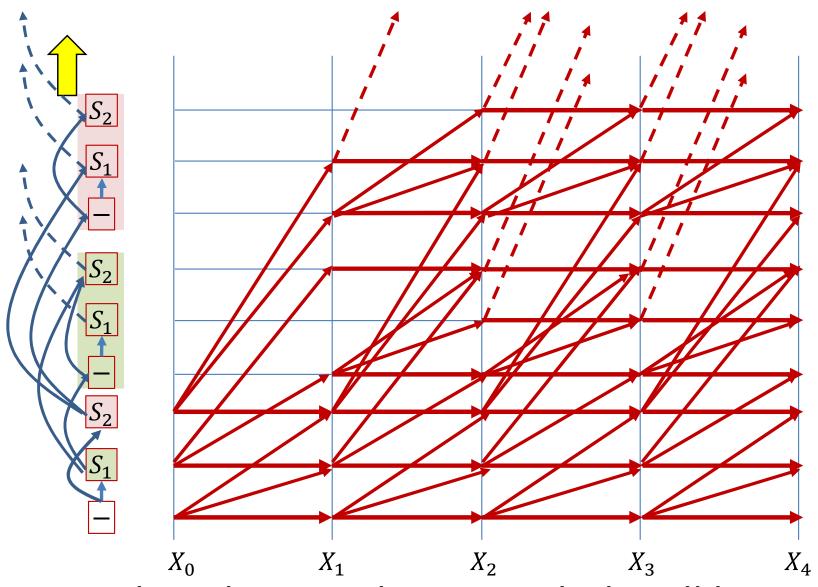


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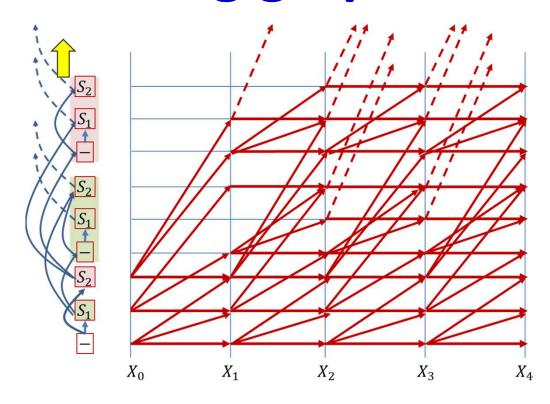
Hypothesis semi-tree



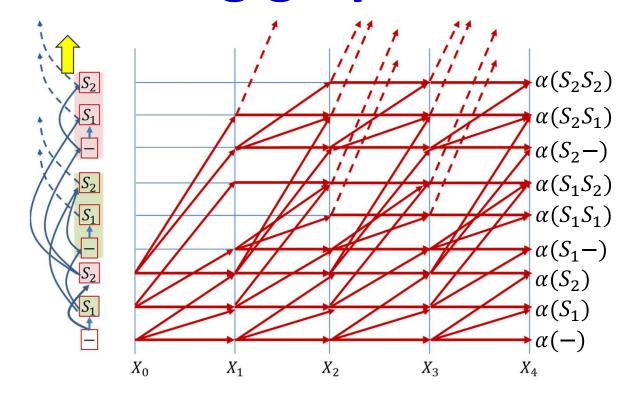
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 Graph with more than 2 symbols will be similar but much more cluttered and complicated

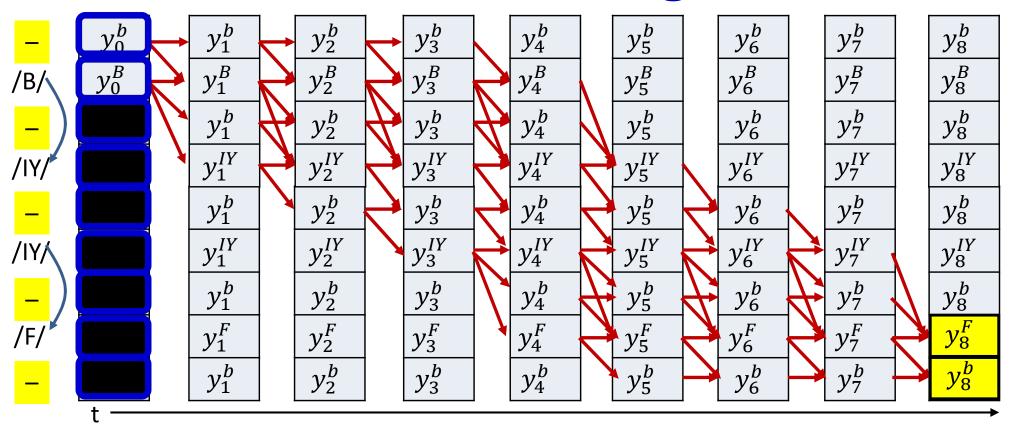


- The figure to the left is the tree, drawn in a vertical line
- The graph is just the tree unrolled over time
 - For a vocabulary of V symbols, every node connects out to V other nodes at the next time
- Every node in the graph represents a unique symbol sequence

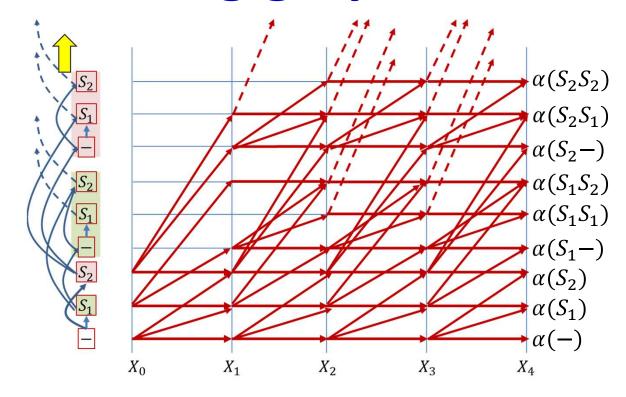


- The forward score $\alpha(r,T)$ at the final time represents the full forward score for a unique symbol sequence (including sequences terminating in blanks)
- Select the symbol sequence with the largest alpha at the final time

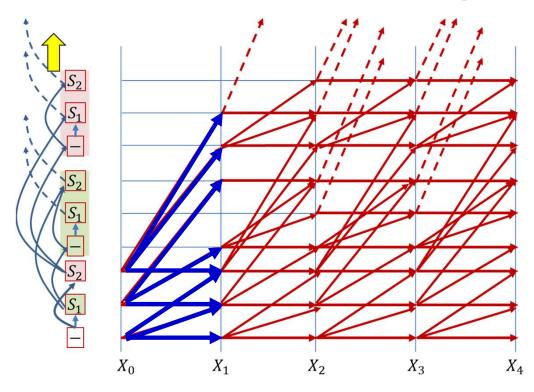
Recall: Forward Algorithm



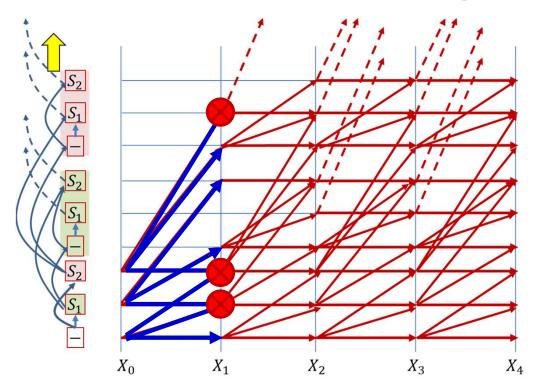
•
$$P(S_0, ..., S_{K-1}|X) = \alpha(T-1,2K) + \alpha(T-1,2K+1)$$



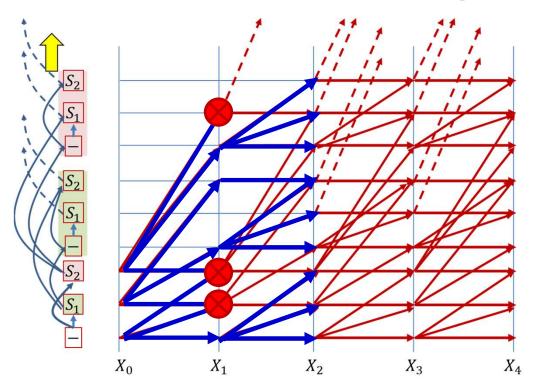
- The forward score $\alpha(r,T)$ at the final time represents the full forward score for a unique symbol sequence (including sequences terminating in blanks)
- Select the symbol sequence with the largest alpha
 - Sequences may two alphas, one for the sequence itself, one for the sequence followed by a blank
 - Add the alphas before selecting the most likely



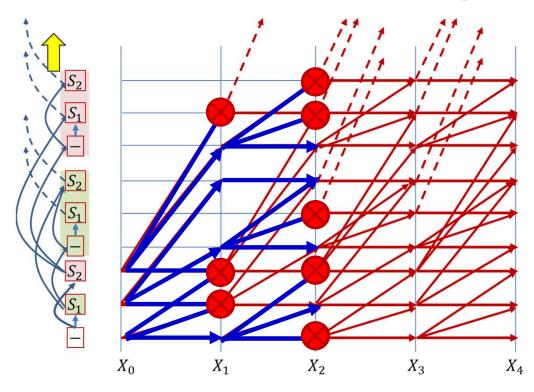
- This is the "theoretically correct" CTC decoder
- In practice, the graph gets exponentially large very quickly
- To prevent this pruning strategies are employed to keep the graph (and computation) manageable
 - This may cause suboptimal decodes, however
 - The fact that CTC scores peak at symbol terminations minimizes the damage due to pruning



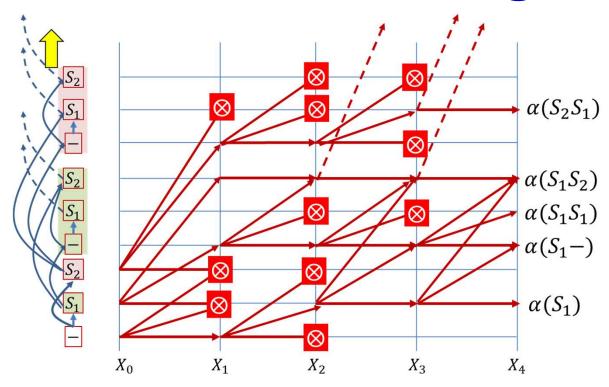
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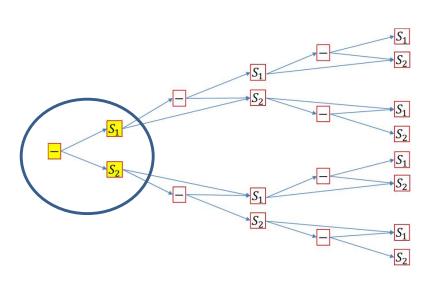
Beamsearch Pseudocode Notes

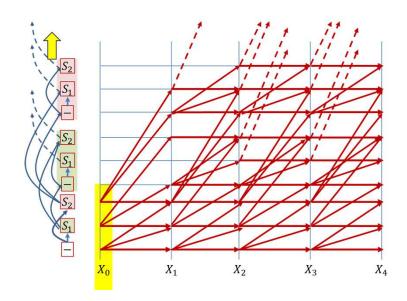
- Retaining separate lists of paths and pathscores for paths terminating in blanks, and those terminating in valid symbols
 - Since blanks are special
 - Do not explicitly represent blanks in the partial decode strings
- Pseudocode takes liberties (particularly w.r.t null strings)
 - I.e. you must be careful if you convert this to code
- Key
 - PathScore: array of scores for paths ending with symbols
 - BlankPathScore : array of scores for paths ending with blanks
 - SymbolSet: A list of symbols not including the blank

```
Global PathScore = [], BlankPathScore = []
# First time instant: Initialize paths with each of the symbols,
# including blank, using score at time t=1
NewPathsWithTerminalBlank, NewPathsWithTerminalSymbol, NewBlankPathScore, NewPathScore =
                           InitializePaths (SymbolSet, y[:,0])
# Subsequent time steps
for t = 1:T
    # Prune the collection down to the BeamWidth
    PathsWithTerminalBlank, PathsWithTerminalSymbol, BlankPathScore, PathScore =
                   Prune (NewPathsWithTerminalBlank, NewPathsWithTerminalSymbol,
                                             NewBlankPathScore, NewPathScore, BeamWidth)
    # First extend paths by a blank
   NewPathsWithTerminalBlank, NewBlankPathScore = ExtendWithBlank(PathsWithTerminalBlank,
                                                                   PathsWithTerminalSymbol, y[:,t])
    # Next extend paths by a symbol
   NewPathsWithTerminalSymbol, NewPathScore = ExtendWithSymbol (PathsWithTerminalBlank,
                                                         PathsWithTerminalSymbol, SymbolSet, y[:,t])
end
# Merge identical paths differing only by the final blank
MergedPaths, FinalPathScore = MergeIdenticalPaths (NewPathsWithTerminalBlank, NewBlankPathScore
                                                  NewPathsWithTerminalSymbol, NewPathScore)
# Pick best path
BestPath = argmax(FinalPathScore) # Find the path with the best score
```

Global PathScore = [], BlankPathScore = []

First time instant: Initialize paths with each of the symbols,
including blank, using score at time t=1





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First time instant: Initialize paths with each of the symbols,
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Subsequent time steps

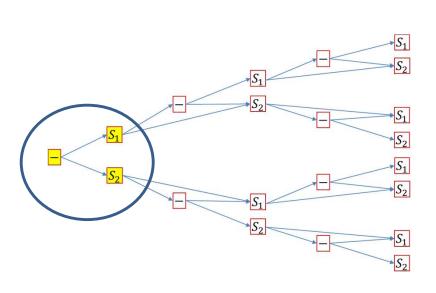
for t = 1:T

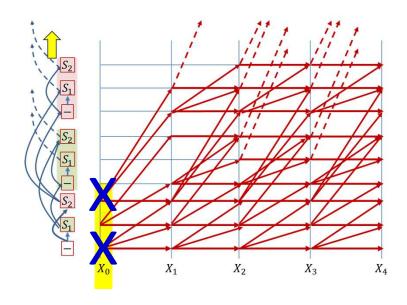
Prune the collection down to the BeamWidth

PathsWithTerminalBlank, PathsWithTerminalSymbol, BlankPathScore, PathScore =

Prune (NewPathsWithTerminalBlank, NewPathsWithTerminalSymbol,

NewBlankPathScore, NewPathScore, BeamWidth)





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First time instant: Initialize paths with each of the symbols,
including blank, using score at time t=1

Subsequent time steps

for t = 1:T

Prune the collection down to the BeamWidth

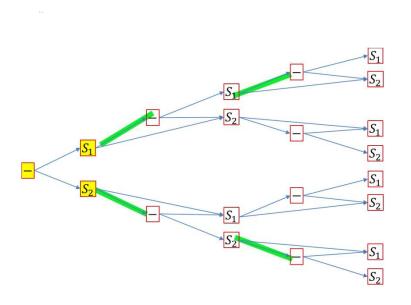
PathsWithTerminalBlank, PathsWithTerminalSymbol, BlankPathScore, PathScore =

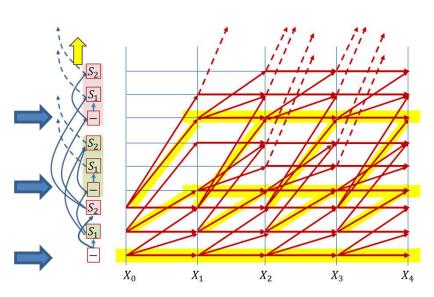
Prune (NewPathsWithTerminalBlank, NewPathsWithTerminalSymbol,

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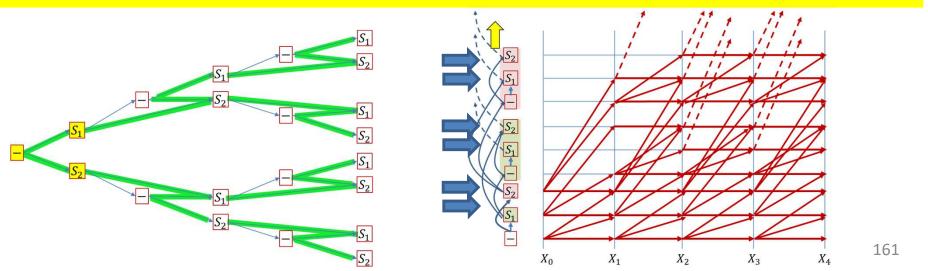
First extend paths by a blank

NewPathsWithTerminalBlank, NewBlankPathScore = ExtendWithBlank(PathsWithTerminalBlank, PathsWithTerminalSymbol, y[:,t])





Global PathScore = [], BlankPathScore = [] # First time instant: Initialize paths with each of the symbols, # including blank, using score at time t=1 NewPathsWithTerminalBlank, NewPathsWithTerminalSymbol, NewBlankPathScore, NewPathScore = InitializePaths (SymbolSet, y[:,0]) # Subsequent time steps for t = 1:T# Prune the collection down to the BeamWidth PathsWithTerminalBlank, PathsWithTerminalSymbol, BlankPathScore, PathScore = Prune (NewPathsWithTerminalBlank, NewPathsWithTerminalSymbol, NewBlankPathScore, NewPathScore, BeamWidth) # First extend paths by a blank NewPathsWithTerminalBlank, NewBlankPathScore = ExtendWithBlank(PathsWithTerminalBlank, PathsWithTerminalSymbol, y[:,t]) # Next extend paths by a symbol NewPathsWithTerminalSymbol, NewPathScore = ExtendWithSymbol(PathsWithTerminalBlank, PathsWithTerminalSymbol, SymbolSet, v[:,t])



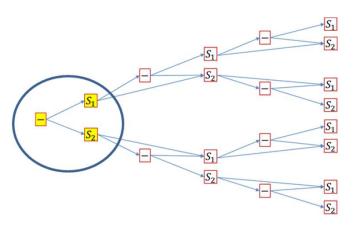
BEAM SEARCH InitializePaths: FIRST TIME INSTANT

```
function InitializePaths(SymbolSet, y)

InitialBlankPathScore = [],    InitialPathScore = []
# First push the blank into a path-ending-with-blank stack. No symbol has been invoked yet
path = null
InitialBlankPathScore[path] = y[blank]  # Score of blank at t=1
InitialPathsWithFinalBlank = {path}

# Push rest of the symbols into a path-ending-with-symbol stack
InitialPathsWithFinalSymbol = {}
for c in SymbolSet  # This is the entire symbol set, without the blank
    path = c
    InitialPathScore[path] = y[c]  # Score of symbol c at t=1
    InitialPathsWithFinalSymbol += path  # Set addition
end

return InitialPathsWithFinalBlank, InitialPathsWithFinalSymbol,
    InitialBlankPathScore, InitialPathScore
```



BEAM SEARCH: Extending with blanks

Global PathScore, BlankPathScore

```
function ExtendWithBlank (PathsWithTerminalBlank, PathsWithTerminalSymbol, y)
   UpdatedPathsWithTerminalBlank = {}
   UpdatedBlankPathScore = []
   # First work on paths with terminal blanks
   #(This represents transitions along horizontal trellis edges for blanks)
   for path in PathsWithTerminalBlank:
       # Repeating a blank doesn't change the symbol sequence
       UpdatedPathsWithTerminalBlank += path # Set addition
       UpdatedBlankPathScore[path] = BlankPathScore[path]*y[blank]
   end
   # Then extend paths with terminal symbols by blanks
   for path in PathsWithTerminalSymbol:
       # If there is already an equivalent string in UpdatesPathsWithTerminalBlank
       # simply add the score. If not create a new entry
       if path in UpdatedPathsWithTerminalBlank
           UpdatedBlankPathScore[path] += Pathscore[path] * y[blank]
       else
           UpdatedPathsWithTerminalBlank += path # Set addition
           UpdatedBlankPathScore[path] = PathScore[path] * y[blank]
       end
   end
   return UpdatedPathsWithTerminalBlank,
           UpdatedBlankPathScore
```

BEAM SEARCH: Extending with symbols

Global PathScore, BlankPathScore

```
function ExtendWithSymbol (PathsWithTerminalBlank, PathsWithTerminalSymbol, SymbolSet, y)
    UpdatedPathsWithTerminalSymbol = {}
    UpdatedPathScore = []
    # First extend the paths terminating in blanks. This will always create a new sequence
    for path in PathsWithTerminalBlank:
        for c in SymbolSet: # SymbolSet does not include blanks
            newpath = path + c # Concatenation
            UpdatedPathsWithTerminalSymbol += newpath # Set addition
           UpdatedPathScore[newpath] = BlankPathScore[path] * y(c)
        end
    end
    # Next work on paths with terminal symbols
    for path in PathsWithTerminalSymbol:
        # Extend the path with every symbol other than blank
        for c in SymbolSet: # SymbolSet does not include blanks
            newpath = (c == path[end]) ? path : path + c # Horizontal transitions don't extend the sequence
            if newpath in UpdatedPathsWithTerminalSymbol: # Already in list, merge paths
                UpdatedPathScore[newpath] += PathScore[path] * y[c]
           else # Create new path
                UpdatedPathsWithTerminalSymbol += newpath # Set addition
                UpdatedPathScore[newpath] = PathScore[path] * y[c]
           end
        end
    end
    return UpdatedPathsWithTerminalSymbol,
           UpdatedPathScore
```

BEAM SEARCH: Pruning low-scoring entries

Global PathScore, BlankPathScore

```
function Prune (PathsWithTerminalBlank, PathsWithTerminalSymbol, BlankPathScore, PathScore, BeamWidth)
    PrunedBlankPathScore = []
    PrunedPathScore = []
   # First gather all the relevant scores
   i = 1
   for p in PathsWithTerminalBlank
        scorelist[i] = BlankPathScore[p]
        i++
   end
    for p in PathsWithTerminalSymbol
        scorelist[i] = PathScore[p]
        i++
   end
    # Sort and find cutoff score that retains exactly BeamWidth paths
   sort(scorelist) # In decreasing order
   cutoff = BeamWidth < length(scorelist) ? scorelist[BeamWidth] : scorelist[end]</pre>
    PrunedPathsWithTerminalBlank = {}
   for p in PathsWithTerminalBlank
        if BlankPathScore[p] >= cutoff
            PrunedPathsWithTerminalBlank += p # Set addition
            PrunedBlankPathScore[p] = BlankPathScore[p]
        end
   end
    PrunedPathsWithTerminalSymbol = {}
    for p in PathsWithTerminalSymbol
        if PathScore[p] >= cutoff
            PrunedPathsWithTerminalSymbol += p # Set addition
            PrunedPathScore[p] = PathScore[p]
        end
    end
```

return PrunedPathsWithTerminalBlank, PrunedPathsWithTerminalSymbol, PrunedBlankPathScore, PrunedPathScore

BEAM SEARCH: Merging final paths

```
# Note : not using global variable here
function MergeIdenticalPaths (PathsWithTerminalBlank, BlankPathScore,
                             PathsWithTerminalSymbol, PathScore)
    # All paths with terminal symbols will remain
    MergedPaths = PathsWithTerminalSymbol
    FinalPathScore = PathScore
    # Paths with terminal blanks will contribute scores to existing identical paths from
    # PathsWithTerminalSymbol if present, or be included in the final set, otherwise
    for p in PathsWithTerminalBlank
        if p in MergedPaths
            FinalPathScore[p] += BlankPathScore[p]
        else
            MergedPaths += p # Set addition
            FinalPathScore[p] = BlankPathScore[p]
        end
    end
    return MergedPaths, FinalPathScore
```

Story so far: CTC models

- Sequence-to-sequence networks which irregularly produce output symbols can be trained by
 - Iteratively aligning the target output to the input and time-synchronous training
 - Optimizing the expected error over all possible alignments: CTC training
- Distinct repetition of symbols can be disambiguated from repetitions representing the extended output of a single symbol by the introduction of blanks
- Decoding the models can be performed by
 - Best-path decoding, i.e. Viterbi decoding
 - Optimal CTC decoding based on the application of the forward algorithm to a tree-structured representation of all possible output strings

CTC caveats

 The "blank" structure (with concurrent modifications to the forward-backward equations) is only one way to deal with the problem of repeating symbols

Possible variants:

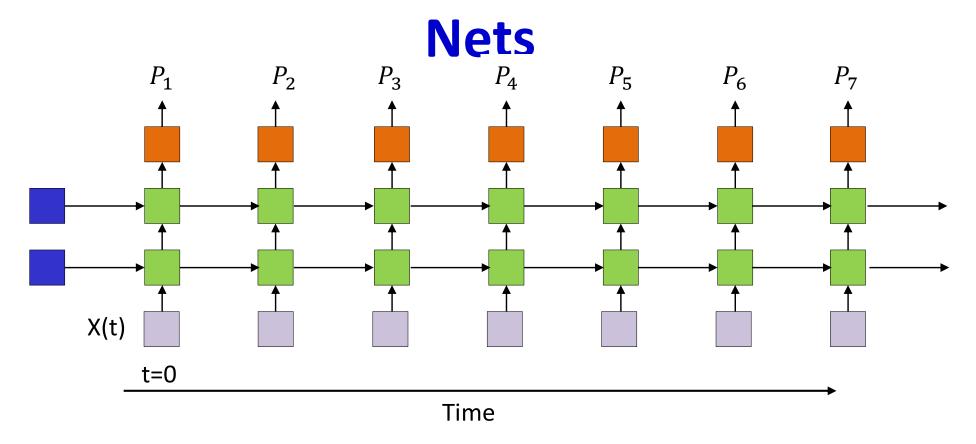
- Symbols partitioned into two or more sequential subunits
 - No blanks are required, since subunits must be visited in order
- Symbol-specific blanks
 - Doubles the "vocabulary"
- CTC can use bidirectional recurrent nets
 - And frequently does
- Other variants possible...

Most common CTC applications

- Speech recognition
 - Speech in, phoneme sequence out
 - Speech in, character sequence (spelling out)

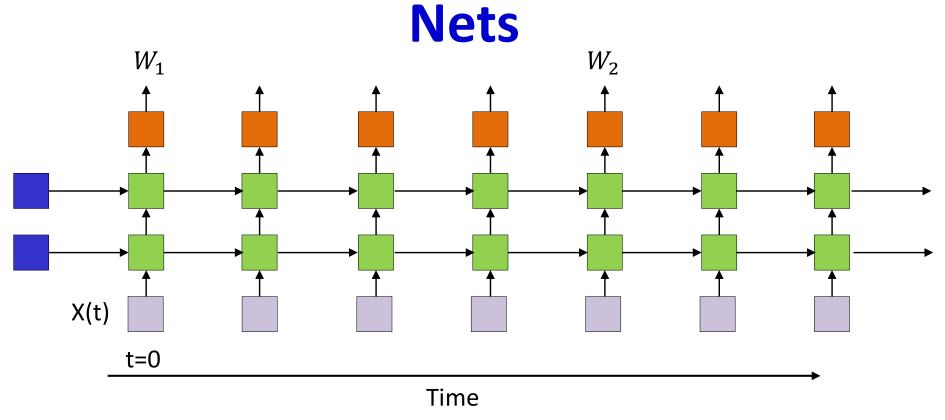
Handwriting recognition

Speech recognition using Recurrent



- Recurrent neural networks (with LSTMs) can be used to perform speech recognition
 - Input: Sequences of audio feature vectors
 - Output: Phonetic label of each vector

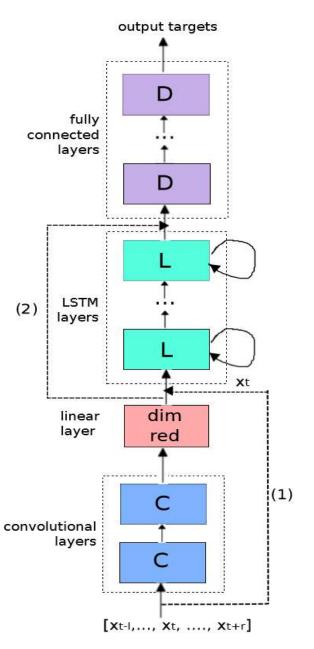
Speech recognition using Recurrent



 Alternative: Directly output phoneme, character or word sequence

Next up: Attention models

CNN-LSTM-DNN for speech recognition

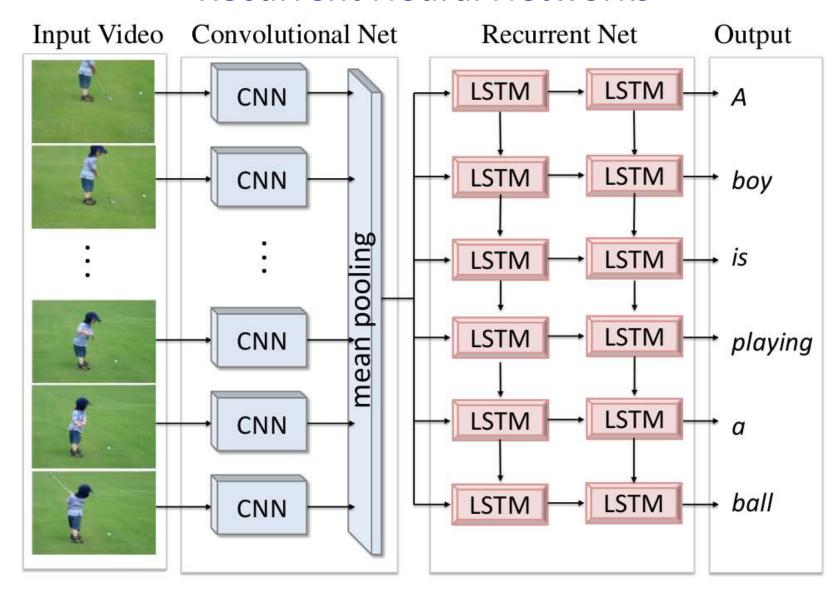


Ensembles of RNN/LSTM, DNN, & Conv Nets (CNN):

T. Sainath, O. Vinyals, A. Senior, H. Sak. "Convolutional, Long Short-Term Memory, Fully Connected Deep Neural Networks," ICASSP 2015.

Fig. 1. CLDNN Architecture

Translating Videos to Natural Language Using Deep Recurrent Neural Networks



Translating Videos to Natural Language Using Deep Recurrent Neural Networks Subhashini Venugopalan, Huijun Xu, Jeff Donahue, Marcus Rohrbach, Raymond Mooney, Kate Saenko $_{174}$ North American Chapter of the Association for Computational Linguistics, Denver, Colorado, June 2015.



"man in black shirt is playing guitar."



"construction worker in orange safety vest is working on road."



"two young girls are playing with lego toy."



boy is doing backflip on wakeboard."



"a young boy is holding a baseball bat."



"a cat is sitting on a couch with a remote control."



"a woman holding a teddy bear in front of a mirror."



"a horse is standing in the middle of a road."

Not explained

- Can be combined with CNNs
 - Lower-layer CNNs to extract features for RNN

- Can be used in tracking
 - Incremental prediction